ELEMENTARY LESSONS IN LOGIC:

DEDUCTIVE AND INDUCTIVE.

WITH COPIOUS QUESTIONS AND EXAMPLES,

AND

A VOCABULARY OF LOGICAL TERMS.

BY

W. STANLEY JEVONS,

LL.D. (EDINE.), M.A. (LOND.), F.R.S.



London

MACMILLAN AND CO., LIMITED NEW YORK: THE MACMILLAN COMPANY
1900

171910 R

First Edition, 1870.

Reprinted 1871, 1872, 1874, 1875, 1877, 1878, 1880, 1881, 1882, 1883, 1884, 1885, 1886, 1889, 1890, 1893, 1895, 1896, 1897,

PREFACE.

In preparing these Lessons I have attempted to show that Logic, even in its traditional form, can be made a highly useful subject of study, and a powerful means of mental exercise. With this view I have avoided the use of superfluous technical terms, and have abstained from entering into questions of a purely speculative or metaphysical character. For the puerile illustrations too often found in works on Logic I have generally substituted examples drawn from the distinct objects and ideas treated in the natural and experimental sciences; and in this and other respects have aimed at rendering these Lessons a suitable companion to a series of science schoolbooks.

2. "我就就

Logic is not only an exact science, but is the most simple and elementary of all sciences; it ought therefore undoubtedly to find some place in every course of education. The relations of propositions and the forms of argument present as precise a subject of instruction and as vigorous an exercise of thought, as the properties of geometrical figures, or the rules of Algebra. Yet every school-boy is made to learn mathematical problems which he will never employ in after life, and is left in total ignorance of those simple principles and forms of reasoning which will enter into the thoughts of every hour. Logic should no longer be considered an elegant and learned accomplishment; it should take its place as an indispensable study for every well-informed person. These Lessons I trust will introduce to the science many who have not leisure or inclination to read more elaborate treatises, and many who would not be attracted by the numerous but somewhat dry and brief compendiums published in past years.

It is desirable that Lessons in Logic should be made the basis of many exercises, and for this purpose I have supplied abundance of questions and examples at the end of the book, some of which are selected from the examination papers of the Oxford, London, and Edinburgh Universities. In my own classes I have constantly found that the working and solution of logical questions, the examination of arguments and the detection of fallacies, is a not less practicable and useful exercise of mind than is the performance of calculations, and the solution of problems in a mathematical class.

Except in a few places, where special notice is given, I have abstained from putting forward any views not commonly accepted by teachers of logic; and I have throughout devoted more attention to describing clearly and simply the doctrines in which logicians generally agree, than discussing the points in which there is a difference of opinion. The recent logical discoveries of Sir W. Hamilton, Mr George Bentham, Prof. de Morgan, and especially the late Prof. Boole, cannot yet be fully adopted in an elementary work, but I have attempted to give a clear notion of the results to which they inevitably lead.

In the latter Lessons which treat of Induction I have generally followed Sir John Herschel, Dr Whewell and Mr J. S. Mill, as the recognised authorities on the subject. These Lessons in fact may be regarded as an easy introduction to some of the most important parts of Mr Mill's treatise on Logic.

At the end of almost every Lesson will be found references to the works in which the student will most profitably continue his reading of the subject treated, so that this little volume may serve as a guide to a more extended course of study.

Hampstrad, November, 1876.

TABLE OF CONTENTS.

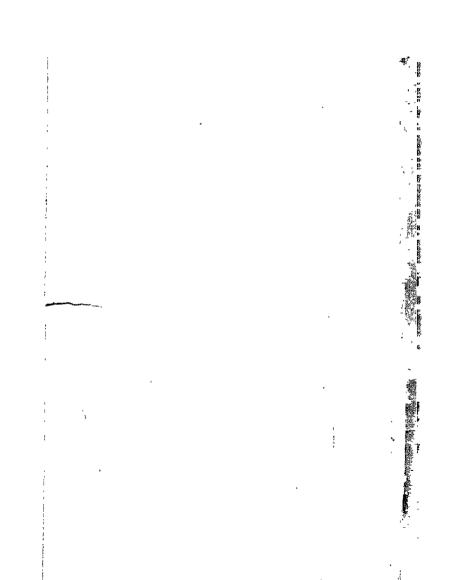
JE SON	P	AGB
I.	DEFINITION and Sphere of the Science	I
JI.	The Three Parts of Logical Doctrine	9
	TERMS.	
11I,	Terms, and their various Kinds	16
rv.	Of the Ambiguity of Terms	27
V.	Of the twofold meaning of terms-in Extension	
	and Intension	37
VΙ.	The Growth of Language	44
VII.	Leibnitz on Knowledge	53
	PROPOSITIONS.	
VIII.	Kinds of Propositions	60
1X.	The Opposition of Propositions	71
ж.	Conversion of Propositions, and Immediate In-	
	ference	81
XI.	Logical Analysis of Sentences	88
XII.	The Predicables, Division, and Definition	98
CIII.	Pascal and Descartes on Method	111

SVLLOGISM.

	SYLLUGISM.
LESSON	PAGE
XIV.	The Laws of Thought 117
XV.	The Rules of the Syllogism 126
XVI.	The Moods and Figures of the Syllogism 135
XVII.	Reduction of the Imperfect Figures 144
XVIII.	Irregular and Compound Syllogisms 152
XIX.	Of Conditional Arguments 160
	FALLACIES.
XX.	Logical Fallacies 169
XXI,	Material Fallacies
	RECENT LOGICAL VIEWS.
XXII,	The Quantification of the Predicate 183
XIII.	Boole's System of Logic 191
	METHOD.
XIV.	Of Method, Analysis, and Synthesis 201
	INDUCTION.
XXV.	Perfect Induction and the Inductive Syllogism 210
XXVI.	Geometrical and Mathematical Induction, Analogy, and Example 218
XVII.	Observation and Experiment 228
XVIII.	Methods of Induction
XXIX.	Methods of Quantitative Induction 247
	The state of the s

	TABLE OF CONTENTS.	χi
(USSON)		PAGE
XXX.	Empirical and Deductive Methods	255
XXXI.	Explanation, Tendency, Hypothesis, Theory and Fact	261
9	SUBSIDIARIES OF INDUCTION.	
XXXII.	Classification, and Abstraction	276
XXXIII.	Requisites of a Philosophical Language	287
	Questions and Exercises	296
	Examples of Terms 297-	-299
	Examples of Propositions	303
	Examples of Arguments 312	





INTRODUCTION.

LESSON I.

h

DEFINITION AND SPHERE OF THE SCIENCE.

LOGIC may be most briefly defined as the Science of Reasoning. It is more commonly defined, however, as the Science of the Laws of Thought, and some logicians think it desirable to specify still more accurately that it is the Science of the Formal, or of the Necessary Laws of Thought. Before these definitions can be of any real use to us we must come to a clear understanding as to the meaning of the expressions; and it will probably appear that there is no great difference between them.

By a Law of Thought we mean a certain uniformity or agreement which exists and must exist in the modes in which all persons think and reason, so long as they do not make what we call mistakes, or fall into self-contradiction and fallacy. The laws of thought are natural laws with which we have no power to interfere, and which are of course not to be in any way confused with the artificial laws of a country, which are invented by men and can be altered by them. Every science is occupied in detecting and describing the natural laws which are inflexibly observed

by the objects treated in the Science. The science of astronomy investigates the uniform or similar way in which the heavenly bodies, and in fact all material substances, tend to fall towards each other as a stone falls towards the earth, or to move round each other under the influence of this tendency. The universal law of gravitation is thus the natural law or uniformity treated in physical astronomy.

In chemistry the law of equivalent proportions describes the well ascertained fact that each chemical substance enters into combination with every other chemical substance only in certain definite proportions; as when exactly eight parts by weight of oxygen unite with one part of hydrogen to form water, or sixteen parts of oxygen and six parts of carbon unite to form carbonic acid in the ordinary burning of a flame or fire. Whenever we can detect uniformities or similarities we so far create science and arrive at natural laws. But there may be, and are, many things so fickle, complicated, and uncertain, that we can never be sure we have detected laws that they will uniformly obey; in such cases no science, in the proper sense of the word, is possible, There is no such thing, for instance, as a real science of human character, because the human mind is too variable and complicated a subject of investigation. There are no two persons so much alike that you may be sure of one acting in all circumstances as the other would; it thus becomes impossible to arrange persons in classes so that all who are in the same class shall act uniformly in the same manner in any given circumstances.

But there is a science of human reason or thought apart from the many other acts of mind which belong to human character, because there are modes in which all persons do uniformly think and reason, and must think and reason. Thus if two things are identical with a third common thing they are identical with each other. This is a law of thought of a very simple and obvious character, and we may observe concerning it,—

1. That all people think in accordance with it, and agree that they do so as soon as they understand its meaning.

2. That they think in accordance with it whatever may be the subject about which they are thinking.

Thus if the things considered are-

London,

The Metropolis,

The most populous city in Great Britain, since "the Metropolis is identical with London," and "London is identical with the most populous city in Great Britain," it follows necessarily in all minds that "the metropolis is identical with the most populous city in Great Britain."

Again, if we compare the three following things-

fron.

The most useful metal, The cheapest metal,—

and it be allowed that "The most useful metal is Iron," and "Iron is the cheapest metal," it follows necessarily in all minds that "the most useful metal is the cheapest," We here have two examples of the general truth that things identical with the same thing are identical with each other; and this we may say is a general or necessary form of thought and reasoning.

Compare, again, the following three things, -

The earth, Planets.

Bodies revolving in elliptic orbits,

We cannot say, as before, that "the earth is identical with the planets:" it is identical only with one of the

planets, and we therefore say that "it is a planet." Similarly we may say that "the planets are bodies revolving in elliptic orbits," but only a part of the whole number so revolving. Nevertheless it follows that if the earth is among the planets, and the planets among bodies revolving in elliptic orbits, then the earth is among the latter.

A very elementary knowledge of chemistry enables us to argue similarly concerning the following;—

Iron,
Metals,
Elementary substances.

Iron is one of the metals, and metals are elements or simple undecomposable substances, in the sense of being among them or a part of them, but not as composing the whole. It follows necessarily that "Iron is one of the elementary substances." We have had then two examples of a fixed and necessary form of thought which is necessary and true whatever the things may be to which it is applied. The form of argument may be expressed in several different ways, and we shall have to consider it minutely in the lessons on the syllogism; we may express it, for instance, by saying that "part of a part is part of the whole." Iron is part of the class of metals, which is part of the class of elements: hence iron is part of the class of elements.

If I now introduce another definition of Logic and say that it is "the science of the necessary forms of thought," the reader will I hope clearly apprehend the meaning of the expression "necessary forms of thought." A form is something which may remain uniform and unaltered, while the matter thrown into that form may be varied. Medals struck from the same dies have exactly the same form, but they may be of various matter, as

bronze, copper, gold or silver. A building of exactly the same form might be constructed either of stone or bricks; furniture of exactly similar shape may be made of oak, mahogany, walnut wood, etc. Just as we thus familiarly recognize the difference of form and substance in common tangible things, so we may observe in Logic, that the form of an argument is one thing, quite distinct from the various subjects or matter which may be treated in that form. We may almost exhibit to the eye the form of reasoning to which belong our two latter arguments, as follows:—



If within the three pairs of brackets, marked respectively X, Y and Z we place three names, such that the one in place of X may be said to come under that in Y, and that in Y under that in Z, then it necessarily follows that the first (X) comes under the last (Z).

Logic, then, is the science occupied in ascertaining and describing all the general forms of thought which we must employ so long as we reason validly. These forms are very numerous, although the principles on which they are constructed are few and simple. It will hence appear that logic is the most general of all the sciences. Its aid must be more often required than the aid of any other science, because all the particular sciences treat portions only of existing things, and create very different and often unconnected branches of knowledge. But logic treats of those principles and forms of thought which must be employed in every branch of knowledge. It treats of the very origin and foundations of knowledge itself; and though it is true that the logical method employed in one science may differ somewhat from that em-

ployed in another science, yet whatever the particular form may be, it must be logical, and must conform to the laws of thought. There is in short something in which all sciences must be similar; to which they must conform so long as they maintain what is true and selfconsistent; and the work of logic is to explain this

common basis of all science.

One name which has been given to Logic, namely the Science of Sciences, very aptly describes the all extensive power of logical principles. The cultivators of special branches of knowledge appear to have been fully aware of the allegiance they owe to the highest of the sciences, for they have usually given names implying this allegiance. The very name of logic occurs as part of nearly all the names recently adopted for the sciences, which are often vulgarly called the "ologies," but are really the "logics," the "o" being only a connecting vowel or part of the previous word. Thus geology is logic applied to explain the formation of the earth's crust; biology is logic applied to the phenomena of life; psychology is logic applied to the nature of the mind; and the same is the case with physiology, entomology, zoology, teratology, morphology, anthropology, theology, ecclesiology, thalattology, and the rest*. Each science is thus distinctly confessed to be a special logic. The name of logic itself is derived from the common Greek word λόγος, which usually means word, or the sign and outward manifestation of any inward thought. But the same word was also used to denote the inward thought or reasoning of which words are the expression, and it is thus probably that later Greek writers on reasoning were led to call their science

^{*} Except Philology, which is differently formed, and means the love or study of words; the name of this science, if formed upon the same plan, would be logology,

鬼

h

έπιστήμη λογική, or logical science; also τέχνη λογική, or logical art. The adjective λογική, being used alone, soon came to be the name of the science, just as Mathematic, Rhetoric, and other names ending in "ie" were originally adjectives but have been converted into substantives.

Much discussion of a somewhat trifling character has arisen upon the question whether Logic should be considered a science only, an art only, or both at the same time. Sir W. Hamilton has even taken the trouble to classify almost all the writers on logic according as they held one opinion or the other. But it seems substantially correct and sufficient to say, that logic is a science in so far as it merely investigates the necessary principles and forms of thought, and thus teaches us to understand in what correct thinking consists; but that it becomes an art when it is occupied in framing rules to assist persons in detecting false reasoning. A solonce teaches us to know and an art to do, and all the more perfect sciences lead to the creation of corresponding useful arts. Astronomy is the foundation of the art of navigation on the ocean, as well as of the arrangement of the calendar and chronology. Physiology is the basis of the art of medicine, and chemistry is the basis of many useful arts. Logic has similarly been considered as the basis of an art of correct reasoning or investigation which should teach the true method to be observed in all sciences. The celebrated British logician Duns Scotus, who lived in the 13th century, and called logic the Science of Sciences, called it also the Art of Arts, expressing fully its preeminence. Others have thus defined it-" Logic is the art of directing the reason aright in acquiring the knowledge of things, for the instruction both of ourselves and others." Dr Isaac Watts, adopting this view of logic, called his well-known work "the Art of Thinking."

It may be fairly said however that Logic has more the form of a science than an art for this reason-all persons necessarily acquire the faculty and habit of reasoning long before they even know the name of logic, This they do by the natural exertion of the powers of mind, or by constant but unconscious imitation of others. They thus observe correctly but unconsciously the principles of the science in all very simple cases; but the contradictory opinions and absurd fallacies which are put forth by uneducated persons shew that this unaided exercise of mind is not to be trusted when the subject of discussion presents any difficulty or complexity. study of logic then cannot be useless. It not only explains the principles on which every one has often reasoned correctly before, but points out the dangers which exist of erroneous argument. The reasoner thus becomes consciously a correct reasoner and learns consciously to avoid the snares of fallacy. To say that men can reason well without logical science is about as true as to say that they can live healthily without medicine. So they can—as long as they are healthy; and so can reasoners do without the science of reasoning—as long as they do reason correctly; but how many are there that can do so? As well might a man claim to be immortal in his body as infallible in his mind,

And if it be requisite to say a few words in defence of Logic as an art, because circumstances in the past history of the science have given rise to misapprehension, can it be necessary to say anything in its praise as a science? Whatever there is that is great in science or in art or in literature, it is the work of intellect. In bodily form man is kindred with the brutes, and in his perishable part he is but matter. It is the possession of conscious intellect, the power of reasoning by general notions that raises him above all else upon the earth; and who

can say that the nature and procedure of this intellect is not almost the highest and most interesting subject of study in which we can engage? In vain would any one deny the truth of the favourite aphorism of Sir W. Hamilton---

IN THE WORLD THERE IS NOTHING GREAT BUT MAN. IN MAN THERE IS NOTHING GREAT BUT MIND.

LESSON II.

THE THREE PARTS OF LOGICAL DOCTRINE.

IT has been explained in the previous lesson that Logic is the Science of Reasoning, or the Science of those Necessary Laws of Thought which must be observed if we are to argue consistently with ourselves and avoid self-contradiction. Argument or reasoning therefore is the strictly proper subject before us. But the most convenient and usual mode of studying logic is to consider first the component parts of which any argument must be made up. Just as an architect must be acquainted with the materials of a building, or a mechanic with the materials of a machine, before he can pretend to be acquainted with its construction, so the materials and instruments with which we must operate in reasoning are suitably described before we proceed to the actual forms of argument.

If we examine a simple argument such as that given in the last lesson, thus—

Iron is a metal,

Every metal is an element,

Therefore Iron is an element,—

we see that it is made up of three statements or assertions, and that each of these contains, besides minor words, two nouns substantive or names of things, and the verb "is." In short, two names, or terms, when connected by a verb, make up an assertion or proposition; and three such propositions make up an argument, called in this case a syllogism. Hence it is natural and convenient first to describe terms, as the simplest parts; next to proceed to the nature and varieties of propositions constructed out of them, and then we shall be in a position to treat of the syllogism as a whole. Such accord-

ingly are the three parts of logical doctrine.

But though we may say that the three parts of logic are concerned with terms, propositions, and syllogisms. it may be said with equal or greater truth that the acts of mind indicated by those forms of language are the real subject of our consideration. The opinions, or rather perhaps the expressions, of logicians have varied on this point. Archbishop Whately says distinctly that logic is entirely conversant about language; Sir W. Hamilton, Mr Mansel, and most other logicians treat it as concerned with the acts or states of mind indicated by the words; while Mr J. S. Mill goes back to the things themselves concerning which we argue. Is the subject of logic, then, language, thought, or objects? The simplest and truest answer is to say that it treats in a certain sense of all three. Inasmuch as no reasoning process can be explained or communicated to another person without words, we are practically limited to such reasoning as is reduced to the form of language. Hence we shall always be concerned with words, but only so far as they are the instruments for recording and referring to our thoughts. The grammarian also treats of language, but he treats it as language merely, and his science terminates with the description and explanation of the forms, varieties, and

THE PERSON NAMED IN COLUMN TWO IS NOT THE PERSON NAMED IN COLUMN TWO IS NAMED IN COLUMN TW

relations of words. Logic also treats of language, but only as the necessary index to the action of mind.

Again, so long as we think correctly we must think of things as they are; the state of mind within us must correspond with the state of things without us whenever an opportunity arises for comparing them. possible and inconceivable that iron should prove not to be an elementary substance, if it be a metal, and every metal be an element. We cannot suppose, and there is no reason to suppose, that by the constitution of the mind we are obliged to think of things differently from the manner in which they are. If then we may assume that things really agree or differ according as by correct logical thought we are induced to believe they will, it does not seem that the views of the logicians named are irreconcileable. We treat of things so far as they are the objects of thought, and we treat of language so far as it is the embodiment of thought. If the reader will bear this explanation in mind, he will be saved from some perplexity when he proceeds to read different works on logic, and finds them to vary exceedingly in the mode of treatment, or at least of expression.

If, when reduced to language, there be three parts of logic, terms, propositions, and syllogisms, there must be as many different kinds of thought or operations of mind. These are usually called—

- 1. Simple apprehension.
- 2. Judgment.
- Reasoning or discourse.

The first of these, Simple Apprehension, is the act of mind by which we merely become aware of something, or have a notion, idea, or impression of it brought into the mind. The adjective simple means apart from other things, and apprehension the taking hold by the mind. Thus the name or term Iron instantaneously makes the

mind think of a strong and very useful metal, but does not tell us anything about it, or compare it with any thing else. The words sun, Jupiter, Sirius, St Paul's Cathedral, are also terms which call up into the mind certain well-known objects, which dwell in our recollection even when they are not present to our senses. In fact, the use of a term, such as those given as examples, is merely as a substitute for the exhibition of the actual things named.

Judgment is a different action of mind, and consists in comparing together two notions or ideas of objects derived from simple apprehension, so as to ascertain whether they agree or differ. It is evident, therefore, that we cannot judge or compare unless we are conscious of two things or have the notions of two things in the mind at the same time. Thus if I compare Jupiter and Sirius I first simply apprehend each of them; but bringing them into comparison I observe that they agree in being small. bright, shining bodies, which rise and set and move round the heavens with apparently equal speed, minute examination, however, I notice that Sirius gives a twinkling or intermittent light, whereas Jupiter shines steadily. More prolonged observation shews that Iupiter and Sirius do not really move with equal and regular speed, but that the former changes its position upon the heavens from night to night in no very simple manner. If the comparison be extended to others of the heavenly bodies which are apprehended or seen at the same time, I shall find that there are a multitude of stars which agree with Sirius in giving a twinkling light and in remaining perfectly fixed in relative position to each other, whereas two or three other bodies may be seen which resemble Jupiter in giving a steady light, and also in changing their place from night to night among the fixed stars. I have now by the action of judgment formed in my mind the general notion of fixed stars, by bringing together mentally a number of objects which agree; while from several other objects I have formed the general notion of *planets*. Comparing the two general notions together, I find that they do not possess the same qualities or appearances, which I state in the proposition, "Planets are not fixed stars."

I have introduced the expression "General Notion" as if the reader were fully acquainted with it. But though philosophers have for more than two thousand years constantly used the expressions, general notion, idea, conception, concept, &c., they have never succeeded in agreeing exactly as to the meaning of the terms. One class of philosophers called Nominalists say that it is all a matter of names, and that when we join together Jupiter, Mars, Saturn, Venus, &c., and call them planets, the common name is the bond between them in our minds. Others, called Realists, have asserted that besides these particular planets there really is something which combines the properties common to them all without any of the differences of size, colour, or motion which distinguish them. Every one allows in the present day however that nothing can physically exist corresponding to a general notion; because it must exist here or there, of this size or of that size, and therefore it would be one particular planet, and not any planet whatever. The Nominalists, too, seem equally wrong, because language, to be of any use, must denote something, and must correspond, as we have seen, to acts of mind. If then proper names raise up in our minds the images of particular things, like the sun, Jupiter, &c., general names should raise up general notions.

The true opinion seems to be that of the philosophers called Conceptualists, who say that the general notion is the knowledge in the mind of the common properties or resemblances of the things embraced under the notion. Thus the notion planet really means the consciousness in anybody's mind that there are certain heavenly bodies which agree in giving a steady light and in moving about the heavens differently from the fixed stars. It should be added, however, that there are many, including Sir W. Hamilton, who would be counted as Nominalists and who yet hold that with the general name is associated a consciousness of the resemblance existing between the things denoted by it. Between this form of the doctrine and conceptualism it is not easy to draw a precise distinction, and the subject is of too debatable a character to be pursued in this work.

It will appear in the course of these lessons that the whole of logic and the whole of any science consists in so arranging the individual things we meet in general notions or classes, and in giving them appropriate general names or terms, that our knowledge of them may be made as simple and general as possible. Every general notion that is properly formed admits of the statement of general laws or truths; thus of the planets we may affirm that they move in elliptic orbits round the sun from west to east; that they shine with the reflected light of the sun; and so on. Of the fixed stars we may affirm that they shine with their own proper light; that they are incomparably more distant than the planets; and so on. The whole of reasoning will be found to arise from this faculty of judgment, which enables us to discover and affirm that a large number of objects have similar properties, so that whatever is known of some may be inferred and asserted of others.

It is in the application of such knowledge that we employ the third act of mind called discourse or reasoning, by which from certain judgments we are enabled, without any new reference to the real objects, to form a new judgment. If we know that iron comes under the

general notion of metal, and that this notion comes under the still wider notion of element, then without further examination of iron we know that it is a simple undecomposable substance called by chemists an element. Or if from one source of information we learn that Neptune is a planet, and from another that planets move in elliptic orbits, we can join these two portions of knowledge together in the mind, so as to elicit the truth that Neptune moves in an elliptic orbit.

Reasoning or Discourse, then, may be defined as the progress of the mind from one or more given propositions to a proposition different from those given. Those propositions from which we argue are called Premises, and that which is drawn from them is called the Conclusion. The latter is said to follow, to be concluded, inferred or collected from them; and the premises are so called because they are put forward or at the beginning (Latin bra. before, and mitto, I send or put). The essence of the process consists in gathering the truth that is contained in the premises when joined together, and carrying it with us into the conclusion, where it is embodied in a new proposition or assertion. We extract out of the premises all the information which is useful for the purpose in view-and this is the whole which reasoning accomplishes.

I have now pointed out the three parts of logical doctrine, Terms, Propositions, and Reasoning or Syllogism, into which the subject is conveniently divided. To the consideration of these parts we shall proceed. But it may be mentioned that a fourth part has often been added, called Method, which is concerned with the arrangement of the parts of any composition.

It is sometimes said that what proposition is to term, and what syllogism is to proposition, such is method to syllogism, and that a fourth division is necessary to complete the doctrine of Logic. It is at any ra however that this fourth part is much inferior ance and distinctness to the preceding three; at will be said of it is to be found in Lesson XXIV.

LESSON III.

TERMS, AND THEIR VARIOUS KI

IT has been explained in the preceding lesson t assertion or statement expresses the agreeme ference of two things, or of two general not putting the assertion or statement into words, accordingly have words suitable for drawing the of the mind to the things which are compared, words indicating the result of the comparison, say, the fact whether they agree or differ. which we point out the things or classes of question are called Terms, and the words dencomparison are said to form the Copula. Henc plete assertion or statement consists of two ten copula, and when thus expressed it forms a Pr Thus in the proposition "Dictionaries are useft the two terms are dictionaries and useful books pula is the verb are, and expresses a certain agre the class dictionaries with the class of useful be sisting in the fact that the class of dictionaries fr of the class of useful books. In this case each t sists of only one or two words, but any number may be required to describe the notions or clas

pared together. In the proposition "the angles at the base of an isosceles triangle are equal to each other," the first term requires nine words for its expression, and the second term, four words (equal to each other); and there is no limit to the number of words which may be employed in the formation of a term.

A term is so called because it forms one end (Latin, terminus) of a proposition, and strictly speaking it is a term only so long as it stands in the proposition. But we commonly speak of a term or a name meaning any noun, substantive or adjective, or any combination of words denoting an object of thought, whether that be, as we shall shortly see, an individual thing, a group of things, a quality of things, or a group of qualities. It would be impossible to define a name or term better than has been done by Hobbes: "A name is a word taken at pleasure to serve for a mark, which may raise in our mind a thought like to some thought which we had before, and which, being pronounced to others, may be to them a sign of what thought the speaker had before in his mind."

Though every term or name consists of words it is not every word which can form a name by itself. We cannot properly say "Not is agreeable" or "Probably is not true;" nothing can be asserted of a preposition, an adverb, and certain other parts of speech, except indeed that they are prepositions, adverbs, &c. No part of speech except a noun substantive, or a group of words used as a noun substantive, can form the subject or first term of a proposition, and nothing but a noun substantive, an adjective, the equivalent of an adjective, or a verb, can form the second term or predicate of a proposition. It may indeed be questioned whether an adjective can ever form a term alone; thus in "Dictionaries are useful," it may be said that the substantive things, or books is understood in the predicate the complete sen-

tence being "Dictionaries are useful books," but as this is a disputed point we will assume that words are divided into two kinds in the following manner:—

Words which stand, or appear to stand alone as complete terms, namely the substantive and adjective, and certain parts of a verb, are called categore the words, from the Greek word κατηγορέω, to assert or predicate.

Those parts of speech, on the other hand, such as prepositions, adverbs, conjunctions, &c., which can only form parts of names or terms are called syncategorematic words, because they must be used with other words in order to compose terms (Greek $\sigma \dot{\nu} \nu$, with, and $\kappa \alpha \tau \eta \gamma o \rho \dot{\epsilon} \omega$). Of syncategorematic words we need not take further notice except so far as they form part of categorematic terms.

We have now to consider the various kinds and peculiarities of terms, so as to gain a clear idea of what they mean. Terms are first of all distinguished into singular or individual, and general or common terms, this being a very obvious division, but one of much importance. A Singul te is one which can denote only a single object, so long at least as it is used in exactly the same meanin; thus the Emperor of the French, the Atlantic Ocean, St Paul's, William Shakspeare, the most precious of the metals, are singular terms. All proper names belong to this class; for though John Jones is the name of any men, yet it is used not as me ing any of these

en, but some single man—it has, in short, a different meaning in each case, just as London, the name of our capital, has no connexion in meaning with London in Canada.

neral te s, on the contrary, are applicable in the same sense equally to any one of indefinite nu ber of objects which rese ble each other in certain qualities. Thus etal is a general name because it may be applied

indifferently to gold, silver, copper, tin, aluminium, or any of about fifty known substances. It is not the name of any one of these more than any other, and it is in fact applied to any substance which possesses metallic lustre, which cannot be decomposed, and which has certain other qualities easily recognised by chemists. Nor is the number of substances in the class restricted; for as new kinds of metal are from time to time discovered they are added to the class. Again, while Mars, Jupiter, Saturn, &c., are singular terms, since each can denote only a single planet, the term planet is a general one, being applicable to as many bodies as may be discovered to revolve round the sun as the earth does.

We must carefully avoid any confusion between general and collective terms. By a collective term we mean the name of a number of things when all joined together as one whole; like the soldiers of a regiment. the men of a jury, the crew of a vessel: thus a collective term is the name of all, but not of each. A general term. on the other hand, is the name of a number of things. but of each of them separately, or, to use the technical expression, distributively. Soldier, juryman, sailor, are the general names which may belong to John Jones, Thomas Brown, &c., but we cannot say that John Jones is a regiment, Thomas Brown a jury, and so on. The distinction is exceedingly obvious when thus pointed out, but it may present itself in more obscure forms, and is then likely to produce erroneous reasoning, as will be pointed out in Lesson xx. It is easy to see that we must not divide terms into those which are general and those which are collective, because it will often happen that the same term is both general and collective, according as it is regarded. Thus, library is collective as regards the books in it, but is general as regards the great number of different libraries, private or public, which exist.

first: but so far does the abuse of language now go. especially in newspaper writing, that we hear of a nationality meaning a nation, although of course if nation is the concrete, nationality ought to be the abstract, meaning the quality of being a nation. Similarly, action, intention, extension, conception, and a multitude of other properly abstract names, are used confusedly for the corresponding concrete, namely, act, intent, extent, concept, &c. Production is properly the condition or state of a person who is producing or drawing something forth; but it has now become confused with that which is produced, so that we constantly talk of the productions of a country. meaning the products. The logical terms, Proposition, Deduction, Induction, Syllogism, are all properly abstract words, but are used concretely for a Proposition, a Deduction, an Induction, a Syllogism; and it must be allowed that logicians are nearly as bad as other people in confusing abstract and concrete terms. Much injury is done to language by this abuse.

Another very obvious division of terms is between those which are positive, and those which are negative. The difference is usually described by saying that positive terms signify the existence or possession of a quality,

grateful, metallic, organic, etc., while the corresponding negatives signify the absence of the same qualities as in ungrateful, non-metallic, inorganic. The negative terms may be adjectives—above, or substantives, concrete or abstract; thus ingratitude, inequality, inconvenience are abstract negative terms; and individuals, unequals, &c. are concrete negatives. We usually consider

negative terms any which have a negative prefix such as not, non, un, in, &c.; but there are a great many terms which serve as negatives without possessing any mark of their negative character. Darkness is the negative of light or lightness, since it eans the absence of light:

compound is the negative of element, since we should give the name of compound to whatever can be decomposed; theoretically speaking every term has its corresponding negative, but it by no means follows that language furnishes the term ready-made. Thus table has the corresponding adjective tabular, but there is no similar negative untabular; one man may be called a bookworm, but there is no negative for those who are not bookworms, because no need of the expression has been felt. A constant process of invention of new negative terms goes on more rapidly perhaps than is desirable, for when an idea is not often referred to it is better to express it by a phrase than add to the length of the dictionary by a new-created word.

It would seem that in many cases a negative term implies the presence of some distinct quality or fact. Thus inconvenience doubtless implies the absence of convenience, but also the presence of positive trouble or pain occasioned thereby. Unhappiness is a negative term, but precisely the same notion is expressed by the positive term misery. The negative of healthy is unhealthy, but the positive term sickly serves equally well. It thus appears to be more a matter of accident than anything else whether a positive or negative term is used to express any particular notion. All that we can really say is that every positive term necessarily implies the possibility of a corresponding negative ter, which is the name of all those things to which the positive name cannot be applied. Whether this term has been invented or not is an accident of language: its existence may be assumed in logic.

The reader may be cautioned against supposing that every term appearing to be of a negative character on account of possessing a negative prefix is really so. The participle *unloosed* certainly appears to be the negative of

loosed; but the two words mean exactly the same thing, the prefix un not being really the negative; invaluable, again, means not what is devoid of value, but what is so valuable that the value cannot be measured; and a shameless action can equally be called by the positive term, a shameful action. Other instances might no doubt be found.

Great care should be taken to avoid confusing terms which express the presence or absence of a quality with those which describe its degree. Less is not the negative of greater because there is a third alternative, equal. The true negative of greater is not-greater, and this is equivalent to either equal or less. So it may be said that disagreeable is not the simple negative of agreeable, because there may be things which are neither one nor the other. but are indifferent to us. It would not be easy to say offhand whether every action which is not honest is dishonest, or whether there may not be actions of an intermediate character. The rule is that wherever the question is one of degree or quantity a medium is possible, and the subject belongs rather to the science of quantity than to simple logic; where the question is one of the presence or absence of a quality, there cannot be more than two alternatives, according to one of the Primary Laws of Thought, which we will consider in Lesson XIV. In the case of quantity we may call the extreme terms opposites; thus less is the opposite of greater, disagreeable of agreeable; in the case of mere negation we may call the terms negatives or contradictories, and it is really indifferent in a logical point of view which of a pair of contradictory terms we regard as the positive and which as the negative. Each is the negative of the other.

Logicians have distinguished from simple negative terms a class of terms called privative, such as blind, dead, &c. Such terms express that a thing has been

deprived of a quality which it before possessed, or was capable of possessing, or usually does possess. A man may be born blind, so that he never did see, but he possesses the organs which would have enabled him to see except for some accident. A stone or a tree could not have had the faculty of seeing under any circumstances. No mineral substance can properly be said to die or to be dead, because it was incapable of life; but it may be called uncrystallized because it might have been in the form of a crystal. Hence we apply a privative term to anything which has not a quality which it was capable of having; we apply a negative term to anything which has not and could not have the quality. It is doubtful however whether this distinction can be properly carried out, and it is not of very much importance.

It is further usual to divide terms according as they are relative or absolute, that is, non-relative. The adjective absolute means whatever is "loosed from connection with anything else" (Latin ab, from, and solutus, loosed); whereas relative means that which is carried in thought, at least, into connection with something else. Hence a relative term denotes an object which cannot be thought of without reference to some other object, or as part of a larger whole. A father cannot be thought of but in relation to a child, a monarch in relation to a subject, a shepherd in relation to a flock; thus father, monarch, and shepherd are relative terms, while child, subject, and flock are the correlatives (Latin con, with, and relativus), or those objects which are necessarily joined in thought with the original objects. The very meaning, in fact, of father is that he has a child, of monarch that he has subjects, and of shepherd that he has a flock. As examples of terms which have no apparent relation to anything else, I may mention water, gas, tree. There does not seem to me to be anything so habitually associated

with water that we must think of it as part of the same idea, and gas, tree, and a multitude of other terms, also denote objects which have no remarkable or permanent relations such as would entitle the terms to be called relatives. They may therefore be considered absolute or non-relative terms.

The fact, however, is that everything must really have relations to something else, the water to the elements of which it is composed, the gas to the coal from which it is manufactured, the tree to the soil in which it is rooted. By the very laws of thought, again, no thing or class of things can be thought of but by separating them from other existing things from which they differ. I cannot use the term mortal without at once separating all existing or conceivable things into the two groups mortal and immortal; metal, element, organic substance, and every other term that could be mentioned, would necessarily imply the existence of a correlative negative term, nonmetallic, compound, inorganic substance, and in this respect therefore every term is undoubtedly relative. Logicians, however, have been content to consider as relative terms those only which imply some peculiar and striking kind of relation arising from position in time or space, from connexion of cause and effect, &c.; and it is in this special sense therefore the student must use the distinction.

The most important varieties of terms having been explained, it is desirable that the reader should acquire a complete familiarity with them by employing the exercises at the end of the book. The reader is to determine concerning each of the terms there given:—

- Whether it is a categorematic or syncategorematic term.
- 2. Whether it is a general or a singular term.
- 3. Whether it is collective or distributive.

- 4. Whether it is concrete or abstract.
- 5. Whether it is positive, or negative, or privative.
- 6. Whether it is relative or absolute.

It will be fully pointed out in the next lesson that most terms have more than one meaning; and as the one meaning may be general and the other singular, the one concrete and the other abstract, and so on, it is absolutely necessary that the reader should first of all choose one precise meaning of the term which he is examining. And in answering the questions proposed it is desirable he should specify the way in which he regards it. Taking the word sovereign, we may first select the meaning in which it is equivalent to monarch; this is a general term in so far as it is the name of any one of many monarchs living or dead, but it is singular as regards the inhabitants of any one country. It is clearly categorematic, concrete, and positive, and obviously relative to the subjects of the monarch.

Read Mr Mill's chapter on Names, System of Logic Book I. chap 2.

LESSON IV.

OF THE AMBIGUITY OF TERMS.

THERE is no part of Logic which is more really useful than that which treats of the ambiguity of terms, that is of the uncertainty and variety of meanings belonging to words. Nothing indeed can be of more importance to the attainment of correct habits of thinking and reasoning than a thorough acquaintance with the great imperfections of language. Comparatively few terms have one

single clear meaning and one meaning only, and whenever two or more meanings are unconsciously confused together, we inevitably commit a logical fallacy. If, for instance, a person should argue that "punishment is an evil," and according to the principles of morality "no evil is to be allowed even with the purpose of doing good," we might not at the first moment see how to avoid the conclusion that "no punishments should be allowed," because they cause evil. A little reflection will show that the word evil is here used in two totally different senses; in the first case it means physical evil or pain; in the second moral evil, and because moral evil is never to be committed, it does not follow that physical evils are never to be inflicted, for they are often the very means of preventing moral evil.

Another very plausible fallacy which has often been put forth in various forms is as follows: "A thoroughly benevolent man cannot possibly refuse to relieve the poor, and since a person who cannot possibly act otherwise than he does can claim no merit for his actions, it follows that a thoroughly benevolent man can claim no merit for his actions." According to this kind of argument a man would have less merit in proportion as he was more virtuous, so as to feel greater and greater difficulty in acting wrongly. That the conclusion is fallacious every one must feel certain, but the cause of the fallacy can only be detected by observing that the words cannot possibly have a double meaning, in the first case referring to the influence of moral motives or good character, and in the second to circumstances entirely beyond a person's control; as, for instance, the compulsion of the laws, the want of money, the absence of personal liberty. The more a person studies the subtle variations in the meaning of common words, the more he will be convinced of the dangerous nature of the tools he has to use in all

communications and arguments. Hence I must ask much attention to the contents of this Lesson.

Terms are said to be univocal when they can suggest to the mind no more than one single definite meaning. They are called equivocal or biguous when they have two or more different meanings. It will be observed. however, that a term is not equivocal because it can be applied to many objects when it is applied in the same sense or meaning to those different objects. Thus cathedral is the name of St Paul's, the York Minster, and the principal churches of Salisbury, Wells, Lincoln and a number of other cities, but it is not ambiguous, because all these are only various instances of the same meaning; they are all objects of the same description or kind. The word cathedral is probably univocal or of one logical meaning only. The word church, on the other hand, is equivocal, because it sometimes means the building in which religious worship is performed, sometimes the body of persons who belong to one sect or persuasion, and Sometimes also the church assemble in churches. means the body of the clergy as distinguished from the laity: hence there is a clear difference in the sense or meaning with which the word is used at different times.

Instances of univocal terms are to be found chiefly in technical and scientific language. Steam-engine, gasometer, railway train, permanent way, and multitudes of such technical names denoting distinct common objects, are sufficiently univocal. In common life the names penny, mantelpiece, teacup, bread and butter, have a sufficiently definite and single meaning. So also in chemistry oxygen, hydrogen, sulphate of copper, alumina, lithia, and thousands of other terms, are very precise, the words themselves having often been invented in very recent years, and the meanings exactly fixed and maintained invariable. Every science has or ought to have a series

of terms equally precise and certain in meaning. (See Lesson XXXIII.) The names of individual objects, buildings, events, or persons, again, are usually quite certain and clear, as in Julius Cæsar, William the Conqueror, the first Napoleon, Saint Peter's, Westminster Abbey, the Great Exhibition of 1851, and so on.

But however numerous may be the univocal terms which can be adduced, still the equivocal terms are astonishingly common. They include most of the nouns and adjectives which are in habitual use in the ordinary intercourse of life. They are called ambiguous from the Latin verb ambigo, to wander, hesitate, or be in doubt; or again homonymous, from the Greek opos, se, and ovopa, name. Whenever a person uses equivocal words in such a way as to confuse the different meanings and fall into error, he may be said to commit the fallacy of Equivation in the logical meaning of the name (see Lesson XX.); but in common life a person is not said to equivocate unless he uses words consciously and deceitfully in a manner calculated to produce a confusion of the true and apparent meanings.

I will now describe the various kinds and causes of ambiguity of words, following to some extent the interesting chapters on the subject in Dr Watts' Logic. In the first place we may distinguish three classes of equivocal words, according as they are—

1. Equivocal in sound only.

2. Equivocal in spelling only.

3. Equivocal both in sound and spelling.

The first two classes are comparatively speaking of very slight importance, and do not often give rise to serious error. They produce what we should call trivial mistakes. Thus we may confuse, when spoken only, the words right, wright and rite (ceremony); also the words rein, rain and reign, might and mite, &c. Owing partly

to defects of pronunciation mistakes are not unknown between the four words air, hair, hare and heir.

Words equivocal in spelling but not in sound are such as tear (a drop), and tear pronounced tare, meaning a rent in cloth; or lead, the metal, and lead, as in following the lead of another person. As little more than momentary misapprehension, however, can arise from such resemblance of words, we shall pass at once to the class of words equivocal both in sound and spelling. These I shall separate into three groups according as the equivocation arises—

- I. From the accidental confusion of different words.
- From the transfer of meaning by the association of ideas.
- From the logical transfer of meaning to analogous objects.
- 1. Under the first class we place a certain number of curious but hardly important cases in which ambiguity has arisen from the confusion of entirely different words, derived from different languages or from different roots of the same language, but which have in the course of time assumed the same sound and spelling. Thus the word mean denotes either that which is medium or mediocre, from the French moyen and the Latin medius, connected with the Anglo-Saxon

id, or middle; or it denotes what is low-minded and base, being then derived from the Anglo-Saxon Gemæne, which means "that belonging to the mæne or many," whatever in short is vulgar. The verb to mean can hardly be confused with the adjective mean, but it comes from a third distinct root, probably connected with the Sanscrit verb. to think.

As other instances of this casual ambiguity, I may ention *rent*, a money payment, from the French *rente* (*rendre*, to return), or a tear, the result of the action of

rending, this word being of Anglo-Saxon origin and one of the numerous class beginning in r or wr, which i itate more or less perfectly the sound of the action which they denote. Pound, from the Latin pondus, a weight, is confused with pound, in the sense of a village pinfold for cattle, derived from the Saxon pyndan, to pen up. Fell, a mountain, is a perfectly distinct word from fell, a skin or hide; and pulse, a throb or beating, and pulse, peas, beans, or potage, though both derived from the Greek or Latin, are probably quite unconnected words. It is curious that gin, in the meaning of trap or machine, is a contracted for of engine, and when denoting the spirituous liquor is a corruption of Geneva, the place where the spirit was first made.

Certain important cases of confusion have been detected in grammar, as between the numeral one, derived from Aryan root, through the Latin unus, and the indeterminate pronoun, one (as in "one ought to do one's duty"), which is really a corrupt form of the French word homme or man. The Germans to the present day use man in this sense, as in man sagt, i.e. one says.

2. By far the largest part of equivocal words have become so by a tr fer of the meant from the thing originally denoted by the word to some other thing habitually connected with it so as to become closely associated in thought. Thus, in Parliamentary language, the House means either the chamber in which the members meet, or it means the body of members who happen to be assembled in it at any time. Similarly, the word church originally denoted the building (κυριακόν, the Lord's House) in which any religious worshippers assemble, but it has thence derived a variety of meanings; it may mean a particular body of worshippers accustomed to assemble in any one place, in which sense it is used in Acts xiv. 23; or it means any body of persons holding

the same opinions and connected in one organization, as in the Anglican, or Greek, or Roman Catholic Church; it is also sometimes used so as to include the laity as well as the clergy; but more generally perhaps the clergy and religious authorities of any sect or country are so strongly associated with the act of worship as to be often called the church par excellence. It is quite evident moreover that the word entirely differs in meaning according as it is used by a member of the Anglican, Greek, Roman Catholic, Scotch Presbyterian, or any other existing church.

The word foot has suffered several curious but very evident transfers of meaning. Originally it denoted the foot of a man or an animal, and is probably connected in a remote manner with the Latin pes, pedis, and the Greek πούς, ποδός; but since the length of the foot is naturally employed as a rude measure of length, it came to be applied to a fixed measure of length; and at the bottom of the body the name was extended by analogy to the foot of a mountain, or the feet of a table; by a further extension, any position, plan, reason, or argument on which we place ourselves and rely, is called the foot or footing. The same word also denotes soldiers who fight upon their feet, or infantry, and the measured part of a verse having a definite length. That these very different meanings are naturally connected with the original meaning is evident from the fact that the Latin and Greek words for foot are subject to exactly similar series of ambiguities.

It would be a long task to trace out completely the various and often contradictory meanings of the word fellow. Originally a fellow was what follows another, that is a companion; thus it came to mean the other of a pair, as one shoe is the fellow of the other, or simply an equal, as when we say that Shakspeare "hath not a fellow,"

From the simple meaning of companion again it comes to denote vaguely a person, as in the question "What fellow is that?" but then there is a curious confusion of depreciatory and endearing power in the word; when a man is called a mere fellow, or simply a fellow in a particular tone of voice, the name is one of severe conte pt; alter the tone of voice or the connected words in the least degree, and it beco es one of the most sweet and endearing appellations, as when we speak of a dear or good fellow. We may still add the technical meanings of the name as applied in the case of a Fellow of a College, or of a learned society.

Another good instance of the growth of a number of different meanings from a single root is found in the word post. Originally a post was something posited, or placed firmly in the ground, such as an upright piece of wood or stone; such meaning still remains in the cases of a lamp-post, a gate-post, signal-post, &c. As a post would often be used to mark a fixed spot of ground, as in a mile-post, it came to mean the fixed or appointed place where the post was placed, as in a military post, the post of danger or honour, &c. The fixed places where horses were kept in readiness to facilitate rapid travelling during the times of the Roman empire were thus called posts.

d thence the whole system of arrangement for the conveyance of persons or news came to be called the posts. The name has retained an exactly similar meaning to the present day in most parts of Europe, and we still use it in post-chaise, post-boy, post-horse and postillion. A system of post conveyance for letters having been organised for about two centuries in England and other countries, this is perhaps the eaning most closely associated with the word post at present, and a number of expressions have thus arisen, such as post-office, postage, postalguide, postman, postmaster, postal-telegraph, &c. Curi-

ously enough we now have iron letter-posts, in which the word post is restored exactly to its original meaning.

Although the words described above were selected on account of the curious variety of their meanings. I do not hesitate to assert that the majority of common nouns possess various meanings in greater or less number. Dr Watts, in his Logic, suggests that the words book, bible, fish, house, and elephant, are univocal terms, but the reader would easily detect ambiguities in each of them. Thus fish bears a very different meaning in natural history from what it does in the mouths of unscientific persons, who include under it not only true fishes, but shellfish or mollusca, and the cetacea, such as whales and seals, in short all swimming animals, whether they have the character of true fish or not. Elephant, in a stationer's or bookseller's shop, means a large kind of paper instead of a large animal. Bible sometimes means any particular copy of the Bible, sometimes the collection of works constituting the Holy Scriptures. The word man is singularly ambiguous; sometimes it denotes man as distinguished from woman; at other times it is certainly used to include both sexes; and in certain recent election cases lawyers were unable to decide whether the word man as used in the Reform Act of 1867 ought or ought not to be interpreted so as to include women. On other occasions man is used to denote an adult male as distinguished from a boy, and it also often denotes one who is emphatically a man as possessing a masculine character. Occasionally it is used in the same way as groom, for a servant, as in the proverb, "Like master, like man." At other times it stands specially for a hushand.

3. Among ambiguous words we must thirdly distinguish those which derive their various meanings in a somewhat different manner, namely by analo or real resemblance

When we speak of a sweet taste, a sweet flower, a sweet tune, a sweet landscape, a sweet face, a sweet poe . it is evident that we apply one and the same word to very different things; such a concrete thing as lump-sugar can hardly be compared directly with such an intellectual existence as Tennyson's May Queen. Nevertheless if the word sweet is to be considered ambiguous, it is in a different way from those we have before considered, because all the things are called sweet on account of a peculiar pleasure which they yield, which cannot be described otherwise than by comparison with sugar. In a similar way, we describe a pain as sharp, a disappointment as bitter, a person's temper as sour, the future as bright or gloomy, an achievement as brilliant; all these adjectives implying comparison with bodily sensations of the simplest kind. The adjective brilliant is derived from the French briller, to glitter or sparkle; and this meaning it fully retains when we speak of a brilliant diamond, a brilliant star, &c. By what a subtle analogy is it that we speak of a brilliant position, a brilliant achievement, brilli t talents, brilliant style! We cannot speak of a clear explanation, indefatigable perseverance, perspicuous style, or sore calamity, without employing in each of these expressions a double analogy to physical impressions, actions, or events. It will be shewn in the sixth Lesson that to this process we owe the creation of all names connected with mental feelings or existences.

Read Watts' Logic, Chapter IV.
Locke's Essay on the Human Understanding, Book III
Chapters IX. and X.

LESSON V.

OF THE TWOFOLD MEANING OF TERMS-IN EXTENSION AND INTENSION.

There is no part of the doctrines of Logic to which I would more urgently request the attention of the reader than to that which I will endeavour to explain clearly in the present Lesson. I speak of the double meaning which is possessed by most logical terms—the meaning in extension, and the meaning in intension. I believe that the reader who once acquires a thorough apprehension of the difference of these meanings, and learns to bear it always in mind, will experience but little further difficulty in the study of logic.

The meaning of a term in extension consists of the objects to which the ter may be applied; its meaning in intension consists of the qualities which possessed by objects be g that n e. A simple example will make this distinction most apparent. What is the meaning of the name "metal"? The first and most obvious answer is that metal means either gold, or silver, or iron, or copper, or aluminium, or some other of the 48 substances known to chemists, and considered to have a metallic nature. These substances then form the plain and common meaning of the name, which is the meaning in extension. But if it be asked why the name is applied to all these substances and these only, the answer must be-Because they possess certain qualities which belong to the nature of metal. We cannot, therefore, know to what substances we may apply the name, or to what we

may not, unless we know the qualities which are indispensable to the character of a metal. Now chemists lay these down to be somewhat as follows:—(I) A metal must be an element or simple substance incapable of decomposition or separation into simpler substances by any known means. (2) It must be a good conductor of heat and electricity. (3) It must possess a great and peculiar reflective power known as metallic lustre*.

These properties are common to all metals, or nearly all metals, and are what mark out and distinguish a metal from other substances. Hence they form in a certain way the meaning of the name metal, the meaning in intension, as it is called, to distinguish it from the

former kind of meaning.

In a similar manner almost any other common name has a double meaning. "Steamship" denotes in extension the Great Eastern, the Persia, the Himalaya, or any one of the thousands of steamships existing or which have existed; in intension it means "a vessel propelled by steam-power." Monarch is the name of Queen Victoria, Victor Emmanuel, Louis Napoleon, or any one of a considerable number of persons who rule singly over countries; the persons themselves form the meaning in extension; the quality of ruling alone forms the intensive meaning of the name. Animal is the name in extension of any one of billions of existing creatures and of indefinitely greater numbers of other creatures that have existed or will exist; in intension it implies in all those creatures the existence of a certain animal life and sense. or at least the power of digesting food and exerting force. which are the marks of animal nature.

^{*} It is doubtfully true that all metals possess metallic lustre, and chemists would find it very difficult to give any consistent explanation of their use of the name; but the statements in the t t are sufficiently true to furnish an example.

It is desirable to state here that this distinction of extension and intension has been explained by logicians under various forms of expression. It is the peculiar misfortune of the science of logic to have a superfluity of names or synonyms for the same idea. Thus the intension of a term is synonymous with its co prehension, or connotation, or depth; while the extension is synonymous with the denotation or breadth. This may be most clearly stated in the form of a scheme:—

The extension, extent, breadth, denotation, domain, sphere or application of a name consists of the individual things to which the name applies.

The intension, intent, depth, connotation, or implication of a name consists of the qualities the possession of which by those things is *implied*.

Of these words, denotation and connotation are employed chiefly by Mr J. S. Mill among modern logical writers, and are very apt for the purpose. To denote is to ark down, and the name marks the things to which it may be applied or affixed; thus metal denotes gold, silver, copper, &c. To connote is to mark along with (Latin con, together; notare, to mark), and the connotation accordingly consists of the qualities before described, the possession of which is implied by the use of the name metal.

When we compare different but related terms we may observe that they differ in the quantity of their extension and intension. Thus the term element has a greater extension of meaning than metal, because it includes in its meaning all metals and other substances as well. But it has at the same time less intension of meaning; for among the qualities of a metallic substance must be found the qualities of an element, besides the other qualities peculiar to a metal. If again we compare the terms metal and malleable metal, it is apparent that the

40

latter term does not include the metals antimony, arsenic, and bismuth, which are brittle substances. Hence malleable metal is a term of narrower meaning in extension than metal; but it has also deeper meaning in intension, because it connotes or implies the quality of malleability in addition to the general qualities of a metal. malleable metal is again a narrower term in extension because it does not include gold and copper; and I can go on narrowing the meaning by the use of qualifying adjectives until only a single metal should be denoted by the term

The reader will now see clearly that a general law of great importance connects the quantity of extension and the quantity of intension, viz.—As the intension of a ter

incre ed the extension is decreased. It must not be supposed, indeed, that there is any exact proportion between the degree in which one meaning is increased and the other decreased. Thus if we join the adjective red to metal we narrow the meaning much more than if we join the adjective white, for there are at least twelve times as many white metals as red. Again, the term white

an includes a considerable fraction of the meaning of the term man as regards extension, but the term blind man only a small fraction of the meaning. Thus it is obvious that in increasing the intension of a term we may decrease the extension in any degree.

In understanding this law we must carefully discri inate the cases where there is only an apparent increase of the intension of a term, from those where the increase is real. If I add the term elementary to metal, I shall not really alter the extension of meaning, for all the metals are elements; and the elementary metals are neither more nor less numerous than the metals. But then the intension of the term is really unaltered at the same time; for the quality of an element is really found among the

qualities of metal, and it is superfluous to specify it over again. A quality which belongs invariably to the whole of a class of things is commonly called a property of the class (see Lesson XII.), and we cannot qualify or restrict a term by its own property.

This is a convenient place to notice a distinction between terms into those which are connotative and those which are non-co otative, the latter consisting of the terms which simply denote things without implying any knowledge of their qualities. As Mr Mill considers this distinction to be one of great importance, it will be well

to quote his own words *:-

The Mon-connotative term is one which signifies a subject only, or an attribute only. A connotative term is one which denotes a subject, and implies an attribute. By a subject is here meant anything which possesses attributes. Thus John, or London, or Engl d, are names which signify a subject only. Whiteness, length, virtue, signify an attribute only. None of these names, therefore, are connotative. But white, long, virtuous, are connotative. The word white denotes all white things, as snow, paper, the foam of the sea, &c., and implies, or, as it was termed by the schoolmen, connotes the attribute whiteness. The word white is not predicated of the attribute, but of the subjects, snow, &c.; but when we predicate it of them, we imply, or connote, that the attribute whiteness belongs to them......

"All concrete general names are connotative. The word *man*, for example, denotes Peter, James, John, and an indefinite number of other individuals, of whom, taken as a class, it is the name. But it is applied to them, because they possess, and to signify that they possess, cer-

^{*} System of Logic, Vol. 1. p. 31, 6th ed. Book I. Chap. II.

tain attributes.... What we call men, are the subjects, the individual Styles and Nokes; not the qualities by which their humanity is constituted. The name therefore is said to signify the subjects directly, the attributes indirectly; it denotes the subjects, and implies, or involves, or indicates, or, as we shall say henceforth, co otes, the attributes. It is a connotative name....

"Proper names are not connotative: they denote the individuals who are called by them; but they do not indicate or imply any attributes as belonging to those individuals. When we name a child by the name Paul, or a dog by the name Cæsar, these names are simply marks used to enable those individuals to be made subjects of discourse. It may be said, indeed, that we must have had some reason for giving them those names rather than any others; and this is true; but the name, once given, is independent of the reason. A man may have been named John, because that was the name of his father; a town may have been named Dartmouth, because it is situated at the mouth of the Dart. But it is no part of the signification of the word John, that the father of the person so called bore the same name; nor even of the word Dartmouth to be situated at the mouth of the Dart. If sand should choke up the mouth of the river, or an earthquake change its course, and remove it to a distance from the town, the na e of the town would not necessarily be changed."

I quote this in Mr Mill's own words, because though it expresses most clearly the view accepted by Mr Mill and many others, it is nevertheless probably erroneous. The connotation of a name is confused with the etymological meaning, or the circumstances which caused it to be affixed to a thing. Surely no one who uses the name England, and knows what it denotes, can be ignorant of the peculiar qualities and circumstances of the country,

and these form the connotation of the term. To any one who knows the town Dartmouth the name must imply the Possession of the circumstances by which that town is characterised at the present time. If the river Dart should be destroyed or removed, the town would so far be altered, and the signification of the name changed. The name would no longer denote a town situated on the Dart, but one which was formerly situated on the Dart, and it would be by a mere historical accident that the for of the name did not appear suitable to the town. So again any proper name such as John Smith, is almost without meaning until we know the John Smith in question. It is true that the name alone connotes the fact that he is a Teuton, and is a male; but, so soon as we know the exact individual it denotes, the name surely implies, also, the peculiar features, form, and character, of that individual. In fact, as it is only by the peculiar qualities, features, or circumstances of a thing, that we can ever recognise it, no name could have any fixed meaning unless we attached to it, mentally at least, such a definition of the kind of thing denoted by it, that we should know whether any given thing was denoted by it or not. If the name John Smith does not suggest to my mind the qualities of John Smith, how shall I know him when I meet him? for he certainly does not bear his name written upon his brow *.

This, however, is quite an undecided question; and as Mr Mill is generally considered the best authority upon the subject, it may be well for the reader provisionally to accept his opinion, that singular or proper names are non-c nnotative, and all concrete general names are connot tive. Abstract names, on the other hand, can hardly

^{*} Further objections to Mr Mill's views on this point will be fo d in Mr Shedden's Elements of Logic. London, 1864. pp. 14. &c.

possess connotation at all, for as they already denote the attributes or qualities of something, there is nothing left which can form the connotation of the name. Mr Mill. indeed, thinks that abstract names may often be considered connotative, as when the name fault connotes the attribute of hurtfulness as belonging to fault. But if fault is a true abstract word at all I should regard hurtfulness as a part of its denotation; I am inclined to think that faultiness is the abstract name, and that fault is generally used concretely as the name of a particular action or thing that is faulty, or possesses faultiness. But the subject cannot be properly discussed here, and the reader should note Mr Mill's opinion that abstract names are usually non-connotative, but may be connotative in some cases.

The subject of Extension and Intension may be pursued in Hamilton's Lectures on Logic, Lect. VIII. : or in Thomson's Laws of Thought, Sections 48 to It is much noticed in Spalding's Logic (Encyclopædia Britannica, 8th ed.).

LESSON VI.

THE GROWTH OF LANGUAGE.

WORDS, we have seen, become equivocal in at least three different ways-by the accidental confusion of different words, by the change of meaning of a word by its habitual association with other things than its original meaning, d by analogical transfer to objects of a similar nature. We must however consider somewhat more closely certain changes in language which arise out of the

VI.

last cause, and which are in constant progress. We can almost trace in fact the way in which langu ge is created and extended, and the subject is to the logici n one of a highly instructive and important character. There are two great and contrary processes which modify language as follows:—

- 1. Generalization, by which a name comes to be applied to a wider class of objects than before, so that the extension of its meaning is increased, and the intension diminished.
- 2. Specialization, by which a name comes to be restricted to a narrower class, the extension being decreased and the intension increased.

The first change arises in the most obvious manner, from our detecting a resemblance between a new object, which is without a name, and some well-known object. To express the resemblance we are instinctively led to apply the old name to the new object. Thus we are well acquainted with glass, and, if we meet any substance having the same glassy nature and appearance, we shall be apt at once to call it a kind of glass; should we often meet with this new kind of glass it would probably come to share the name equally with the old and original kind of glass. The word coal has undergone a change of this kind; originally it was the name of charked or charred wood, which was the principal kind of fuel used five hundred years ago. As mineral coal came into use it took the name from the former fuel, which it resembled more nearly than anything else, but was at first distinguished as sea-coal or pit-coal. Being now far the more common of the two, it has taken the simple name, and we distinguish charred wood as charcoal. Paper has undergone a like change; originally denoting the papyrus used in the Roman Empire, it was transferred to the new writing material made of cotton or linen rags, which was introduced ta quite

uncertain period. The word character is interesting on account of its logical employment; the Greek χαρακτήρ denoted strictly a tool for engraving, but it became transferred by association to the marks or letters engraved with it, and this meaning is still retained by the word when we speak of Greek characters, Arabic characters, i. e. figures or letters. But inasmuch as objects often have natural arks, signs, or tokens, which may indicate them as well as artificial characters, the name was generalized, and now means any peculiar or distinctive mark or quality by which an object is easily recognised.

Changes of this kind are usually effected by no particular person and with no distinct purpose, but by a sort of unconscious instinct in a number of persons using the name. In the language of science, however, changes are often made purposely, and with a clear apprehension of the generalization implied. Thus soap in ordinary life is applied only to a compound of soda or potash with fat: but chemists have purposely extended the name so as to include any compound of a metallic salt with a fatty substance. Accordingly there are such things as lime-soap and lead-soap, which latter is employed in making common diachylon plaster. Alcohol at first denoted the product of ordinary fermentation commonly called spirits of wine, but chemists having discovered that many other substances had a theoretical composition closely resembling spirits of wine, the name was adopted for the whole class, and a long enumeration of different kinds of alcohols will be found in Dr Roscoe's lessons on chemistry. The nu ber of known alcohols is likewise subject to indefinite increase by the progress of discovery. Every one of the chemical terms acid, alkali, metal, alloy, earth, ether, oil, gas, salt, may be shown to have undergone great generalizations.

In other sciences there is hardly a less supply of

VI.]

instances. A lens originally meant a lenticular shaped or double convex piece of glass, that being the kind of glass most frequently used by opticians. But as glasses of other shapes came to be used along with lenses, the name was extended to concave or even to perfectly flat pieces of glass. The words lever, plane, cone, cylinder, arc, conic section, curve, prism, magnet, pendulum, ray, light, and many others, have been similarly generalized.

In common language we may observe that even proper or singular names are often generalized, as when in the time of Cicero a good actor was called a Roscius after an actor of preeminent talent. The name Cæsar was adopted by the successor of Julius Cæsar as an official name of the Emperor, with which it gradually became synonymous, so that in the present day the Kaisers of Austria and the Czars of Russia both take their title from Cæsar. Even the abstract name Cæsarism has been formed to express a kind of imperial system as established by Cæsar. The celebrated tower built by a king of Egypt on the island of Pharos, at the entrance of the harbour of Alexandria, has caused lighthouses to be called phares in French, and pharos in obsolete English. From the celebrated Roman General Quintus Fabius Maximus any one who avoids bringing a contest to a crisis is said to pursue a Fabian policy.

In science also singular names are often extended, as when the fixed stars are called distant suns, or the companions of Jupiter are called his moons. It is indeed one theory, and a probable one, that all general names were created by the process of generalization going on in the early ages of human progress. As the comprehension of general notions requires higher intellect than the apprehension of singular and concrete things, it seems natural that names should at first denote individual objects, and should afterwards be extended to classes. We have a

glimpse of this process in the case of the Australian natives who had been accustomed to call a large dog *Cadli*, but when horses were first introduced into the country they adopted this name as the nearest description of a horse. A very similar incident is related by Captain Cook of the natives of Otaheite. It may be objected, however, that a certain process of judgment must have been exerted before the suitability of a name to a particular thing could have been perceived, and it may be considered probable that specialization as well as generalization must have acted in the earliest origin of language uch as it does at present.

S cializati is an exactly opposite process to generalization and is almost equally important. It consists in narrowing the extension of meaning of a general name, so that it comes to be the name only of an individual or a minor part of the original class. It is thus we are furnished with the requisite names for a multitude of new implements, occupations and ideas with which we deal in advancing civilization. The name physician is derived from the Greek φυσικός, natural, and φύσις, nature, so that it properly means one who has studied nature, especially the nature of the human body. It has become restricted, however, to those who use this knowledge for medical purposes, and the investigators of natural science have been obliged to adopt the new na e physicist. The name naturalist has been similarly restricted to those who study living things. The name surgeon originally meant handicraftsman, being a corruption of chirurgeon, derived fro the Greek χειρουργός, hand-worker. It h long been specialized however to those who perform the mech ical parts of the s atory art.

Language abounds with equally good exa ples. Minister originally nt a servant, or one who acted as a minor of another. Now it often means specially the most

VI.)

important man in the kingdom. A chancellor was a clerk or even a door-keeper who sat in a place separated by bars or cancelli in the offices of the Roman Emperor's palace; now it is always the name of a high or even the highest dignitary. Peer was an equal (Latin, Par), and we still speak of being tried by our peers; but now, by the strange accidents of language, it means the few who are superior to the rest of the Queen's subjects in rank. Deacon, Bishop, Clerk, Queen, Captain, General, are all words which have undergone a like process of specialization. In such words as telegraph, rail, signal, station, and many words relating to new inventions, we may trace the progress of change in a lifetime.

One effect of this process of specialization is very soon to create a difference between any two words which happen from some reason to be synonymous. Two or more words are said to be synonymous (from the Greek σύν, with, and ονομα, name) when they have the same meaning, as in the case, perhaps, of teacher and instructor, similarity and resemblance, beginning and commencement, sameness and identity, hypothesis and supposition, intension and comprehension. But the fact is that words commonly called synonymous are seldom perfectly so, and there are almost always shades of difference in meaning or use. which are explained in such works as Crabb's English Synonyms. A process called by Coleridge desynonymization, and by Herbert Spencer differentiation, is always going on, which tends to specialize one of a pair of synonymous words to one meaning and the other to another. Thus wave and billow originally eant exactly the same physical effect, but poets have now appropriated the word 'billow,' whereas wave is used chiefly in practical and scientific matters. Undulation is a third synonym, which will probably become the sole scientific term for a wave in course of time. Cab was originally a mere

extension is the spreading out; intention, the bendin to; explication, the unfolding; application, the folding to; conception, the taking up together; relation, the carrying back; experience is the thoroughly going through a thing; difference is the carrying apart; deliberation, the weighing out; interruption, the breaking between; proposition, the placing before; intuition, the seeing into; and the list might be almost indefinitely extended. Our English name for reason, the understanding, obviously contains some physical metaphor which has not been fully explained; with the Latin *intellect* there is also a metaphor.

Every sense gives rise to words of refined eaning; sapience, taste, insipidity, goût, are derived from the sense of taste; sagacity, from the dog's extraordinary power of smell; but as the sense of sight is by far the most acute and intellectual, it gives rise to the larger part of language; clearness, lucidity, obscurity, haziness, perspicuity, and innumerable other expressions, are derived fro this sense.

It is truly astonishing to notice the power which language possesses by the processes of generalization, specialization, and metaphor, to create many words from one single root. Prof. Max Müller has given a remarkable instance of this in the case of the root spec, which means sight, and appears in the Aryan languages, as in the Sanscrit spas, the Greek σκέπτουαι, with transposition of consonants, in the Latin specio, and even in the English spy. The following is an incomplete list of the words developed from this one root; species, special, especial, specimen, spice, spicy, specious, speciality, specific, specialization. specie (gold, or silver), spectre, specification, spectacle, spectator, spectral, spectrum, speculum, specular, speculation. The same root also enters into composition with various prefixes; and we thus obtain a series of words, suspect, aspect circu spect, expect, inspect,

prospect, respect, retrospect, introspection, conspicuous, perspicuity, perspective; with each of which, again, a number of derivatives is connected. Thus, from suspect, we derive suspicion, suspicable. suspicious, suspiciously, suspiciousness. I have estimated that there are in all at least 246 words, employed at some period or other in the English language which undoubtedly come from the one root spec.

J. S. Mill's Logic, Book IV. Chap. V. 'On the Natural History of the Variations in the Meanings of Terms.' Archbishop Trench, On the Study of Words.

Max Müller, Lectures on the Science of Language.

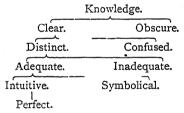
LESSON VII.

LEIBNITZ ON KNOWLEDGE.

In treating of terms it is necessary that we should clearly understand what a perfect notion of the eaning of a term requires. When a name such as monarch, or civilization, or autonomy is used, it refers the mind to some thing or some idea, and we ought if possible to obtain a perfect knowledge of the thing or idea before we use the word. In what does this perfect knowledge consist? What are its necessary characters? This is a question which the celebrated mathematician and philosopher Leibnitz attempted to answer in a small treatise or tract first published in the year 1684. This tract has been the basis of what is given on the subject in several recent works on Logic, and a complete translation of the tract

has been appended by Mr Baynes to his translation of the *Port Royal Logic*. As the remarks of Leibnitz himself are not always easy to understand, I will not confine myself to his exact words, but will endeavour to give the simplest possible statement of his views, according as they have been interpreted by Dr Thomson or Sir W. Hamilton.

Knowledge is either obscure or clear; either confused or distinct; either adequate or inadequate; and lastly either symbolical or intuitive. Perfect knowledge must be clear, distinct, adequate and intuitive; if it fails in any one of these respects it is more or less imperfect. We may, therefore, classify knowledge as in the following scheme:—



A notion, that is to say our knowledge of a thing, is obscure when it does not enable us to recognize the thing again and discriminate it from all other things. We have a clear notion of a rose and of most common flowers because we can recognise them with certainty, and do not confuse them with each other. Also we have a clear notion of any of our intimate friends or persons whom we habitually meet, because we recognise them whenever we see them with the utmost certainty and without hesitation. It is said that a shepherd acquires by practice a clear notion of each sheep of his flock, so as to enable him to single out any one separately, and a keeper of

hounds learns the name and character of each hound, while other persons have only an obscure idea of the hounds generally, and could not discriminate one from the other. But the geologist cannot give a clear idea of what sandstone, conglomerate, or schist, or slate, or trap rock consists, because different rocks vary infinitely in degree and character, and it is often barely possible to say whether a rock is sandstone or conglomerate, schist or slate, and so on. In the lower forms of life the naturalist hardly has a clear notion of animal life, as distinguished from vegetable life; it is often difficult to decide whether a protophyte should be classed with animals or plants.

Clear knowledge, again, is confused, when we cannot distinguish the parts and qualities of the thing known, and can only recognise it as a whole. Though any one instantly knows a friend, and could discriminate him from all other persons, yet he would generally find it impossible to say how he knows him, or by what marks. He could not describe his figure or features, but in the very roughest manner. A person unpractised in drawing, who attempts to delineate even such a familiar object as a horse or cow, soon finds that he has but a confused notion of its form, while an artist has a distinct idea of the form of every limb. The chemist has a distinct as well as a clear notion of gold and silver, for he can not only tell with certainty whether any metal is really gold or silver. but he can specify and describe exactly the qualities by which he knows it; and could, if necessary, mention a great many other qualities as well. We have a very distinct notion of a chess-board, because we know it consists of 64 square spaces; and all our ideas of geometrical figures, such as triangles, circles, parallelograms, squares, pentagons, hexagons, &c. are or ought to be perfectly distinct. But when we talk of a constitutional government.

or a civilized nation, we have only the vaguest idea of what we mean. We cannot say exactly what is requisite to ake a Government constitutional, without including also Governments which we do not intend to include; and so of civilized nations; these terms have neither distinct nor clear meanings.

It is to be remarked that no simple idea, such as that of red colour, can be distinct in the meaning here intended, because nobody can analyse red colour, or describe to another person what it is. A person who has been blind from birth cannot be made to conceive it; and it is only by bringing an actual red object before the eye that we can define its character. The same is generally true of all simple sensations, whether tastes, smells, colours, or sounds; these then may be clearly known but not distinctly, in the meaning which Leibnitz gives to this word.

To explain the difference which Leibnitz intended to denote by the names adequate and inadequate, is not easy. He says, "When everything which enters into a distinct notion is distinctly known, or when the last analysis is reached, the knowledge is adequate, of which I sc cely know whether a perfect example can be offered—the knowledge of numbers, however, approaches near to it."

To have adequate knowledge of things, then, we must not only distinguish the parts which make up our notion of a thing, but the parts which make up those parts. For instance, we might be said to have an adequate notion of a chess-board, because we know it to be made up of 64 squares, and we know each of those squares distinctly, because each is made up of 4 equal right lines, joined at right angles. Nevertheless, we cannot be said to have a distinct notion of a straight line, because we cannot well define it, or resolve it into anything simpler. To be com

pletely adequate, our knowledge ought to admit of analysis after analysis ad infinitum, so that adequate knowledge would be impossible. But, as Dr Thomson remarks, we may consider any knowledge adequate which carries the analysis sufficiently far for the purpose in view. A mechanist, for instance, has adequate knowledge of a machine, if he not only know its several wheels and parts, but the purposes, materials, forms, and actions of those parts; provided again that he know all the mechanical properties of the materials, and the geometrical properties of the forms which may influence the working of the machine. But he is not expected to go on still further and explain why iron or wood of a particular quality is strong or brittle, why oil acts as a lubricator, or on what axioms the principles of mechanical forces are founded.

Lastly, we must notice the very important distinction of symbolical and intuitive knowledge. From the original meaning of the word, intuitive would denote that which we gain by seeing (Latin, intueor, to look at), and any knowledge which we have directly through the senses, or by immediate communication to the mind, is called intuitive. Thus we may learn intuitively what a square or a hexagon is, but hardly what a chiliagon, or figure of

1000 sides, is.

We could not tell the difference by sight of a figure of 1000 sides and a figure of 1001 sides. Nor can we imagine any such figure completely before the mind. It is known to us only by name or symbolically. All large numbers, such as those which state the velocity of light (186,000 miles per second), the distance of the sun (91,000,000 miles), and the like, are known to us only by symbols, and they are beyond our powers of imagination.

Infinity is known in a similar way, so that we can in an intellectual manner become acquainted with that of which our senses could never inform us. We speak also of nothing, of zero, of that which is self-contradictory, of the non-existent, or even of the unthinkable or inconceivable, although the words denote what can never be realized in the mind and still less be perceived through the senses intuitively, but can only be treated in a merely symbolical way.

In arithmetic and algebra we are chiefly occupied with symbolical knowledge only, since it is not necessary in working a long arithmetical question or an algebraical problem that we should realise to ourselves at each step the meaning of the numbers and symbols. We learn from algebra that if we multiply together the sum and difference of two quantities we get the difference of the squares; as, in symbols

$$(a + b)(a - b) = a^2 - b^2;$$

which is readily seen to be true, as follows:

$$a + b$$

$$a - b$$

$$a^{2} + ab$$

$$-ab - b^{2}$$

$$a^{2} + 0 - b^{2}$$

In the above we act darkly or symbolically, using the letters α and δ according to certain fixed rules, without knowing or caring what they mean; and whatever meaning we afterwards give to α and δ we may be sure the process holds good, and that the conclusion is true without going over the steps again.

But in geometry, we argue by intuitive perception of the truth of each step, because we actually employ a representation in the mind of the figures in question, and satisfy ourselves that the requisite properties are really possessed by the figures. Thus the algebraical truth shown above in symbols may be easily proved to hold true VII.

of lines and rectangles contained under those lines, as a corollary of the 5th Prop. of Euclid's Second Book.

Much might be said concerning the comparative advantages of the intuitive and symbolical methods. The latter is usually much the less laborious, and gives the most widely applicable answers; but the symbolical seldom or never gives the same command and comprehension of the subject as the intuitive method. Hence the study of geometry is always indispensable in education, although the same truths are often more readily proved by algebra. It is the peculiar glory of Newton that he was able to explain the motions of the heavenly bodies by the geometric or intuitive method; whereas the greatest of his successors, such as Lagrange or Laplace, have treated these motions by the aid of symbols.

What is true of mathematical subjects may be applied to all kinds of reasoning; for words are symbols as uch as A, B, C, or x, y, z, and it is possible to argue with words without any consciousness of their meaning. Thus if I say that "selenium is a dyad element, and a dyad element is one capable of replacing two equivalents of hydrogen," no one ignorant of chemistry will be able to attach any meaning to these terms, and yet any one will be able to conclude that "selenium is capable of replacing two equivalents of hydrogen." Such a person argues in a purely symbolical manner. Similarly, whenever in common life we use words, without having in mind at the moment the full and precise meaning of the words, we possess symbolical knowledge only.

There is no worse habit for a student or reader to acquire than that of accepting words instead of a knowledge of things. It is perhaps worse the useless to read a work on natural history about Infusoria, Fora inifera, Rotifera and the like, if these names do not convey clear images to the mind. Nor can a student who has not

witnessed experiments, and examined the substances with his own eyes, derive any considerable advantage from works on chemistry and natural philosophy, where he will meet with hundreds of new terms which would be to him mere empty and confusing signs. On this account we should lose no opportunity of acquaintin ourselves, by means of our senses, with the for s, properties and changes of things, in order that the language we e ploy may, as far as possible, be employed intuitively, and we may be saved from the absurdities and fallacies into which we might otherwise fall. We should observe, in short, the advice of Bacon—ipsis consuescere rebus—to accustom ourselves to things themselves.

Hamilton's Lectures on Logic. Lect. IX.
Baynes' Port Royal Logic. Part I. Chap. 9, and Appendix.

LESSON VIII.

KINDS OF PROPOSITIONS.

A TER standing alone is not capable of expressing truth; it merely refers the mind to some object or class of objects, about which something may be affirmed or denied, but about which the term itself does not affirm or deny anything. "Sun," "air," "table," suggest to every mind objects of thought, but we cannot say that "sun is true," or "air is mistaken," or "table is false." We must join words or terms into sentences or propositions before they can express those reasoning actions of the mind to which

truth or falsity may be attributed. "The sun is bright," "the air is fresh," "the table is unsteady," are statements which may be true or may be false, but we can certainly entertain the question of their truth in any circumstances. Now as the logical term was defined to be any combination of words expressing an act of simple apprehension, so a logical proposition is any combination of words expressing an act of judgment. The proposition is in short the result of an act of judgment reduced to the form of language.

What the logician calls a proposition the grammarian calls a sentence. But though every proposition is a sentence, it is not to be supposed that every sentence is a proposition. There are in fact several kinds of sentences more or less distinct from a proposition, such as a Sentence Interrogative or Question, a Sentence Imperative or a Command, a Sentence Optative, which expresses a wish, and an Exclamatory Sentence, which expresses an emotion of wonder or surprise. These kinds of sentence may possibly be reduced, by a more or less indirect mode of expression, to the form of a Sentence Indicative, which is the grammatical name for a proposition; but until this be done they have no proper place in Logic, or at least no place which logicians have hitherto sufficiently explained.

The name proposition is derived from the Latin words pro, before, and pono, I place, and means the laying or placing before any person the result of an act of judgment. Now every act of judgment or comparison must involve the two things brought into comparison, and every proposition will naturally consist of three parts—the two terms or names denoting the things compared, and the copula or verb indicating the connection between them, as it was ascertained in the act of judg ent. Thus the proposition, "Gold is a vellow substance," expresses

an agreement between gold and certain other substances previously called yellow in regard to their colour. Gold and yellow substance are evidently the two terms. and is

the copula.

It is always usual to call the first term of a proposition the subject, since it denotes the underlying matter, as it were (Latin, sub, under, and jactum, laid) about which something is asserted. The second term is called the predicate, which simply means that which is affirmed or asserted. This name is derived from the Latin prædicare, to assert, whence comes the French name prédicateur, corrupted into our preacher. This Latin verb is not to be confused with the somewhat similar one predicere, which has the entirely different meaning to predict or foretell. I much suspect that newspaper writers and others, who pedantically use the verb "to predicate," sometimes fall into this confusion, and really mean to predict, but it is in any case desirable that a purely technical term like predicate should not be needlessly introduced into common language, when there are so many other good words which might be used. This and all other technical scientific terms should be kept to their proper scientific use, and the neglect of this rule injures at once the language of common life and the language of science.

Propositions are distinguished into two kinds, according as they make a statement conditionally or unconditionally. Thus the proposition, "If metals are heated they are softened," is conditional, since it does not make an assertion concerning metals generally, but only in the circumstances when they become heated. Any circumstance which must be granted or supposed before the assertion becomes applicable is a condition. Conditional propositions are of two kinds. Hypothetical and Disjunctive, but their consideration will be best deferred to a subsequent Lesson (XIX). Unconditional propositions are those with which we shall for some time be solely concerned, and these are usually called Categorical Propositions, from the Greek verb κατηγορέω (kategoreo, to assert or affirm).

The following diagram will conveniently represent the classification of sentences and propositions as far as we

have yet proceeded:-

Sentence Indicative Categorical Hypothetical.

Interrogative Conditional Disjunctive. Optative Exclamatory

It is now necessary to consider carefully the several kinds of categorical propositions. They are classified according to quality and according to qu tity. As regards quality they are either affirmative or negative; as regards quantity they are either universal or particular.

An affirmative proposition is one which asserts a certain agreement between the subject and predicate, so that the qualities or attributes of the predicate belong to the subject. The proposition, "gold is a yellow substance," states such an agreement of gold with other yellow substances, that we know it to have the colour yellow, as well as whatever qualities are implied in the name substance. A negative proposition, on the other hand, asserts a difference or discrepancy, so that some at least of the qualities of the predicate do not belong to the subject. "Gold is not easily fusible" denies that the quality of being easily fused belongs to gold.

Propositions are again divided according to quantity into universal and particul propositions. If the proposition affirms the predicate to belong to the whole of the subject, it is universal proposition, as in the example

"all metals are elements," which affirms that the quality of being undecomposable or of being simple in nature is true of all metals. But if we say "some metals are brittle," the quality of brittleness is affirmed only of some indefinite portion of the metals, and there is nothing in the proposition to make us sure that any certain metal is brittle. The name particular being derived from the diminutive of the Latin pars would naturally signify a small part, but in logic it must be carefully interpreted as signifying any part, from the smallest fraction up to nearly the whole. Particular propositions do not include cases where a predicate is affirmed of the whole or of none of the subject, but they include any between these limits. We may accordingly count among particular propositions all such as the following:—

A very few metals are less dense than water.

Most elements are metals.

Many of the planets are comparatively small bodies. Not a few distinguished men have had distinguished sons.

The reader must carefully notice the somewhat subtle point explained further on, that the particular proposition though asserting the predicate only of a part of the subject, does not deny it to be true of the whole.

Aristotle, indeed, considered that there were altogether four kinds of proposition as regards quantity,

namely-

Proposition Universal. Particular. ingular. Indefinite.

The singul proposition is one which has a singular term for its subject, as in—

Socrates was very wise. London is a vast city. But we may fairly consider that a singular proposition is an universal one; for it clearly refers to the whole of the subject, which in this case is a single individual thing.

Indefinite or indesignate propositions are those which are devoid of any mark of quantity whatever, so that the form of words gives us no mode of judging whether the predicate is applicable to the whole or only part of the subject. Metals are useful, Comets are subject to the law of gravitation, are indefinite propositions. In reality, however, such propositions have no distinct place in logic at all, and the logician cannot properly treat the until the true and precise meaning is made apparent. The predicate must be true either of the whole or of part of the subject, so that the proposition, as it stands, is clearly incomplete; but if we attempt to remedy this and supply the marks of quantity, we overstep the proper boundaries of logic and assume ourselves to be acquainted with the subject matter or science of which the proposition treats. We may safely take the preceding examples to mean "some metals are useful" and "all comets are subject to the law of gravitation," but not on logical grounds. Hence we may strike out of logic altogether the class of indefinite propositions, on the understanding that they must be rendered definite before we treat them. I may observe, however, that in the following lessons I shall frequently use propositions in the indefinite form as examples, on the understanding that where no sign of quantity appears, the universal quantity is to be assumed. It is probable that wherever a term is used alone, it ought to be interpreted as meaning the whole of its class. But however this ay be, we need not recognize the indefinite proposition as a distinct kind; and sin ular propositions having been resolved into universals, there remain only the two kinds, Universal and Particular.

Remembering now that there are two kinds of propo-

sition as regards quality, and two as regards quantity, we shall be able to form altogether four varieties, thus:—

$$Proposition \left\{ \begin{aligned} & Universal \left\{ \begin{aligned} & Affirmative & \textbf{A} \\ & Negative \end{aligned} \right. \\ & Particular \left\{ \begin{aligned} & Affirmative & \textbf{I} \\ & Negative \end{aligned} \right. \end{aligned} \right.$$

The vowel letters placed at the right hand are symbols or abbreviated names, which are always used to denote the four kinds of proposition; and there will be no difficulty in remembering their meaning if we observe that A and I occur in the Latin verb affirmo, I affirm, and E and O in nego, I deny.

There will not generally be any difficulty in referring to its proper class any proposition that we meet with in writings. The mark of universality usually consists of so e adjective of quantity, such as all, every, each, any, none; but whenever the predicate is clearly intended to apply to the whole of the subject we may treat the proposition as universal. The signs of a particular proposition are the adjectives of quantity, some, certain, a few, many, ost, or such others as clearly indicate part at least.

The negative proposition is known by the adverbial particle not being joined to the copula; but in the proposition, that is the universal negative, we frequently use the particle no or none prefixed to the subject. Thus, "no metals are compound," "none of the ancients were acquainted with the laws of motion," are familiar forms of the universal negative.

The student must always be prepared too to meet with isleading or ambiguous forms of expression. Thus the proposition, "all the metals are not denser than water," might be taken as or 0, according as we interpret it to

mean "no metals are denser than water," or "not all the etals," &c., the last of course being the true sense. The little adjective few is very subject to a subtle ambiguity of this kind; for if I say "few books are at once learned and amusing," I may fairly be taken to assert that a few books certainly are so, but what I really mean to draw attention to is my belief that "the greater number of books are not at once learned and amusing." A proposition of this kind is generally to be classed rather as 0 than I. The word some is subject to an exactly similar ambiguity between some but not all, and some at least, it may be all; the latter appears to be the correct interpretation, as shewn in the following lesson (p 79).

As propositions are met with in ordinary language they are subject to various inversions and changes of the

simple logical form.

(1) It is not uncommon, especially in poetry, to find the predicate placed first, for the sake of emphasis or variety; as in "Blessed are the merciful;" "Comes something down with eventide;" "Great is Diana of the Ephesians." There is usually no difficulty in detecting such an inversion of the terms, and the sentence must then be reduced to the regular order before being treated in logic.

(2) The subject may so etimes be mistaken for the predicate when it is described by a relative clause, standing at the end of the sentence, as in "no one is free who is enslaved by his appetites." Here free is evidently the predicate, although it stands in the middle of the sentence, and "one who is enslaved by his appetites" is the real subject. This proposition is evidently of the

for E

Propositions are also expressed in various odes differing from the simple logical order, and some of the different kinds which arise must be noticed. Exclusive propositions contain some words, such as only, alone, none but, which limit the predicate to the subject. Thus, in "elements alone are metals," we are informed that the predicate "metal" cannot be applied to anything except "elements," but we are not to understand that "all elements are metals." The same meaning is expressed by "none but elements are metals;" or, again, by "all that are not ele ents are not metals;" and this we shall see in the next lesson is really equivalent to "all metals are elements." Arguments which appear fallacious at first sight will often be found correct when they contain exclusive propositions and these are properly interpreted.

ceptive propositions affirm a predicate of all the subject with the exception of certain defined cases, to which, as is implied, the predicate does not belong. Thus, "all the planets, except Venus and Mercury, are beyond the earth's orbit," is a proposition evidently equivalent to two, viz. that Venus and Mercury are not beyond the e th's orbit, but that the rest are. If the exceptions e not actually specified by name an exceptive proposition ust often be treated as a particular one. For if I say "all the planets in our system except one agree with Bode's law," and do not give the name of that one exception, the reader cannot, on the ground of the proposition, assert of y planet positively that it does agree with ode's law.

Some propositions are distinguished as explicative or essenti, because they erely affirm of their subject a predicate which is known to belong to it by all who can define the subject. Such propositions erely unfold what is already contained in the subject. "A parallelogra has four sides d four angles," is an explicative or essential proposition. "London, which is the capital of England, is the largest city of Europe," contains two pro-

positions; of which one merely directs our attention to a fact which all may be supposed to know, viz. that

London is the capital of England.

Ampliative propositions, on the other hand, join a new predicate to the subject. Thus to those who do not know the comparative sizes of cities in Europe, the last example contains an ampliative proposition. The greater number of propositions are of this kind.

Tautologous or Truistic propositions are those which erely affirm the subject of itself, and give no information whatever; as in, "whatever is, is;" "what I have

written, I have written."

It is no part of formal Logic to teach us how to interpret the eanings of sentences as we meet them in writings; this is rather the work of the grammarian and philologist. Logic treats of the relations of the different propositions, and the inferences which can be drawn from the; but it is nevertheless desirable that the reader should acquire some familiarity with the real logical eaning of conventional or peculiar forms of expression, and a number of examples will be found at the end of the book, which the reader is requested to classify and treat as directed.

In addition to the distinctions already noticed it has long been usual to distinguish propositions as they are pure or odal. The pure proposition simply asserts that the predicate does or does not belong to the subject, while the modal proposition states this cum modo, or with an intimation of the mode or manner in which the predicate belongs to the subject. The presence of any adverb of ti e, place, manner, degree, &c., or any expression equivalent to an adverb, confers modality on a proposition. "Error is always in haste;" "justice is ever equal;" "a perfect man ought always to be conquering himself," are examples of modal propositions in this acceptation of

the na e. Other logicians, however, have adopted a different view, d treat od ity as consisting in the de ee of certainty or probability with which a judgment is ade and asserted. Thus, we may say, "an equilateral triangle is necessarily equiangular;" "men are generally trustworthy;" "a falling barometer probably indicates a co ing storm;" "Aristotle's lost treatises a possibly be recovered;" and all these assertions are made with a different degree of certainty or modality. Dr Thomson is no doubt right in holding that the modality does not affect the copula of the proposition, and the subject could only be properly treated in a work on Probable Reasoning.

Many logicians have also divided propositions according as they are true or false, and it might well seem to be a distinction of importance. Nevertheless, it is wholly beyond the province of the logician to consider whether a proposition is true or not in itself: all that he to determine is the comparative truth of propositions -that is, whether one proposition is true when another Strictly speaking, logic has nothing to do with a proposition by itself; it is only in converting or transmuting certain propositions into certain others that the work of re oning consists, and the truth of the conclusion is only so far in question as it follows from the truth of what we shall call the premises. It is the duty of the special sciences each in its own sphere to determine what are true propositions and what are false, and logic would be but another name for the whole of knowledge could it take this duty on itself.

See Mr Mill's System of Logic, Book I. Chap. IV. which generally agrees with what is given above. Chapters V. and VI. contain Mr Mill's views on the Nature and Import of Propositions, which subject may be further

studied in Mr Mill's Examination of Sir W. Hamilton's Philosophy, Chap. XVIII.; Hamilton's Lectures on Logic, No. XIII.; and Mansel's Prolegomena Logica, Chap. II.; but the subject is too metaphysical in character to be treated in this work.

LESSON IX.

THE OPPOSITION OF PROPOSITIONS.

WE have ascertained that four distinct kinds of propositions are recognized by logicians,—the Universal affirmative, the Particular affirmative, the Universal negative, and the Particular negative, commonly indicated by the symbols A, I, , 0. It is now desirable to compare together somewhat minutely the meaning and use of propositions of these various kinds, so that we may clearly learn how the truth of one will affect the truth of others, or how the same truth may be thrown into various forms of expression.

The proposition A expresses the fact that the thing or class of things denoted by the subject is included in, and forms part of the class of things denoted by the predicate. Thus "all metals are elements" means that metals form a part of the class of *elements*, but not the whole. As there are altogether 63 known elements, of which 48 are metals, we cannot say that all elements are metals. The proposition itself does not tell us anything about *elements in general*; it is not in fact concerned with ele ents, metals being the subject about which it gives us informa-

tion. This is best indicated by a kind of diagram, first used by the celebrated mathematician Euler, in his letters to a German princess. In Fig. 1, the metals are supposed to be enclosed in the small circle somewhat as sheep might be in a pinfold, this circle containing all the metals and nothing else. The greater circle is supposed to contain in a similar manner all the elements and nothing else. Now as the small circle is wholly within the larger one, it follows that all the metals must be counted as

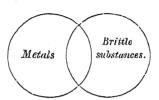
Fig. 1.



elements, but of the part of the elements outside the circle of metals we know nothing from the proposition.

The particul affir ative proposition I exactly resembles A in meaning, except that only part of the subject is brought into question. When I say that "some metals are brittle," I mean that of a collection of all the different etals a few at least might be picked out which would be found to be brittle; but the word some is exceedingly indefinite, shewing neither the exact number of brittle metals, nor how we are to know them from the others, unless indeed by trying whether they are brittle. This proposition will be properly represented in Euler's mode by two intersecting circles, one supposed to enclose all metals, and the other all brittle substances. The mere fact of the two circles intersecting proves that some

Fig. 2.



part of one class must coincide with some part of the other class, which is what the proposition is intended to express. Concerning the portions of the circles which do not overlap the proposition tells us nothing.

The iversal negative proposition E denies the existence of any agreement or coincidence between the subject and predicate. Thus from "no metals are compound substances," we learn that no metal is to be found among compound substances, and it follows necessarily that no compound substance can be found among the metals. For were there a compound substance among the metals, there would evidently be one metal at least among the compound substances. This entire separation in thought of the two classes is well shewn in Euler's method by two disconnected circles.

Fig. 3.

Metals

Compounds.

distinguished from A and I, by the fact that it gives us some information concerning the whole of the predicate, because we learn that none of the objects included in the predicate can be found among those included in the subject. The affirmative propositions, on the other hand, warranted us in holding that the objects denoted by the subject, or some particular part of them, were included in the predicate, but they give us no warrant for saying that any specified part of the predicate is in the subject. Because we merely know that a substance is an element, we do not learn from the proposition "all metals are elements" whether it is a metal or not. And from the proposition "some metals are brittle," we certainly cannot ascertain whether any particular brittle substance is a etal. We must seek the information from other sources.

etal. We must seek the information from other sources. But from "no metals are compounds" we learn of any co pound substance that it is not a metal, as well as of

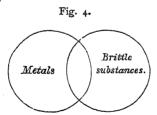
a metal that it is not a compound substance.

The import t difference above explained is expressed in technical language by saying that the proposition distributes its predicate, whereas the affirmative propositions A and I do not distribute their predicates. By distribution of a term is simply meant taking it universally, or referring to all parts of it; and as the validity of any argument or syllogism will usually depend upon the sufficient distribution of the terms occurring in it, too much attention cannot be paid to this point.

Judging from the examples we have had, it will be seen that the universal affirmative distributes its subject, but not its predicate; for it gives us some information concerning all metals, but not all elements. The particular affirmative distributes neither subject nor predicate; for we do not learn anything from our example concerning all metals nor concerning all brittle substances. But the universal negative distributes both subject and predi-

cate, for we learn so ething of all metals and also of all compound substances.

The particular negative proposition 0 will be found to distribute its predicate, but not its subject. When I say so e etals are not brittle, I intentionally refer only to a part of the metals, and exclude them from the cl s of brittle substances; but I cannot help at the same time referring to the whole of the brittle substances. If the metals in question coincided with any part of the brittle substances they could not be said to be excluded from the class. To exclude a thing from any space, as from a particular chamber of a house, it must not merely be re oved from some part, but from any part, or fro the whole of that space or chamber. Euler's diagram for this proposition may be constructed in the same manner as for the proposition I as follows:—



It is apparent that though part of the metals fall into the circle of brittle substances, yet the remaining portion are excluded from any part of the predicate.

We may state the result at which we have now arrived in the following form:—

Proposition	Universal	Affirmative A.		Subject. Distributed.	Predicate. Undistributed.
		Negative	•	Distributed.	Distributed.
	Particular	Affirmative Negative	I. 0.	Subject. Distributed, Distributed, Undistributed. Undistributed.	Undistributed. Distributed.

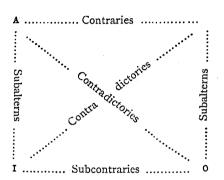
We shall now discover with great ease the relations of the four propositions, each to each, that is to say, the way in which they are opposed to each other. It is obvious that the truth of a proposition ay interfere ore or less completely with the truth of another proposition having the same subject and predicate. If "all metals are elements," it is impossible that "some metals are not elements," and still more palpably impossible, so to say, that "no metals should be elements." The proposition A, then, is inconsistent with both E and O; and, vice versa, 0 are inconsistent with A. Similarly, E is inconsistent with A and I. But this important difference must be noted, that if A be false, O is necessarily true, but E may or may not be true. If it is not true that "all men are sincere," it follows that "some men are not sincere," but it does not in the least follow that "no men are sincere." This difference is expressed by saying that A and O are co tra ctory propositions, whereas A and E are called contrary propositions. It is plain that A and , as in "all men are sincere" and "no men are sincere," represent the utmost possible contrariety of circu stances. order to prove the falsity of A, it is sufficient to establish the truth of 0, and it is superfluous, even if possible, to prove E; similarly E is disproved by proving I, and it is superfluous to prove A. Any person who asserts a universal proposition, either A or E, lays himself under the necessity of explaining away or disproving every single exception brought against it. An opponent may always restrict himself to the much easier task of finding instances which apparently or truly contradict the universality of the statement, but if he takes upon himself to affirm the direct contrary, he is himself open to easy attack. Were it to be asserted, for instance, that "All Christians are more moral than Pagans," it would be easy to adduce examples showing that "Some Christians

are not more moral than Pagans," but it would be absurd to suppose that it would be necessary to go to the contrary extreme, and shew that "No Christians are more moral than Pagans." In short A is sufficiently and best disproved by O, and by I. It will be easily apparent that, vice versâ, O is disproved by A, and I by E; nor is there, indeed, any other mode at all of disproving these particular propositions.

When we compare together the propositions I and 0 we find that they are in a certain sense contrary in nature, one being affirmative and the other negative, but that they are still consistent with each other. It is true both that "Some metals are brittle," for instance Antimony, Bismuth and Arsenic; but it is also true that "Some metals are not brittle." And the reader will observe that when I affirm "Some metals are ele ents," there is nothing in this to prevent the truth of "Some metals are not elements," although on other grounds we know that this is not true. The propositions I and 0 are called subcontraries each of the other, the name connoting a less degree of contrariety than exists between A and.

As regards the relation of A to I and to 0, it is plain that the truth of the universal includes and necessitates the truth of the particular What may be affirmed or denied of all parts of a class may certainly be affir ed or denied similarly of some part of the class. From the truth of the particular we have no right to infer either the truth or falsity of the universal of the same quality. These pairs of propositions are called sub te s, i. e. one under the other (Latin sub under, and alter the other of two), or we may say more exactly that I and 0 are respectively the subalternates of A and , each of which is a subalternans.

The relations of the propositions just described ar all clearly shown in the following scheme:—



It is so highly important to apprehend completely and readily the istency or opposition of propositions, the I will put the matter in another form. Taking any two propositions having the same subject and predicate, they must come under one of the following statements:—

- 1. Of contradictory propositions, one ust be true and one false.
- Of contrary propositions, both cannot be true, and both ay be false.
- 3. Of subcontrary propositions, one only can be fals , and both may be true.
- 4. Of subalterns, the particular is true if the univers 1 be true; but the universal ay or ay not be true whe the particular is true.

I put the same atter in yet other fo in the following table, which shows how the truth of each of A, , I, d 0, affects the truth of each of the others.

			A	E	I	0
			is	is	is	is
If A	be	true	true	false	true	false.
"	,,	22	false	true	false	true.
" I	,,	72	doubtful	false	true	doubtful.
" 0	,,	"	false	doubtful	doubtful	true.

It will be evident that from the affirmation of universals more information is derived than from the affirmation of particulars. It follows that more information can be derived from the denial of particulars than from the denial of universals, that is to say, there are less cases left doubtful, as in the above table.

The reader may well be cautioned, however, against an ambiguity which has misled some even of the most eminent logicians. In particular propositions the adjective some is to be carefully interpreted as some, and there may or may not be more or all. Were we to interpret it as some, not more nor all, then it would really give to the proposition the force of I and O combined. If I say "some men are sincere." I must not be taken as implying that "some men are not sincere;" I must be understood to predicate sincerity of some men, leaving the character of the remainder wholly unaffected. It follows from this that, when I deny the truth of a particular, I must not be understood as implying the truth of the universal of the same quality. To deny the truth of "some men are ortal" might seem very natural, on the ground that not some but all men are mortal; but then the proposition denied would really be some men are not mortal, i. e. O not I. Hence when I deny that "some men are immortal" I mean that "no en are immortal;" and when I deny that "some men are not mortal," I mean that "all mortal."

It has long been usual to compare propositions as

regards the quality of the subject matter to which they refer, and what is technically called the atter was distinguished into three kinds, necessary, contingent, and impossible. Necessary matter consists of any subject in which the proposition A may be affirmed; impossible in which E may be affirmed. Any subject or branch of knowledge in which universal statements cannot usually be made is called contingent matter, and it implies the truth of I and 0. Thus "comets are subject to gravitation." though an indefinite or indesignate proposition (p. 65), may be interpreted as A, because it refers to a part of natural science where such general laws obtain. "men are sincere" would be properly interpreted as par ticular or I, because the matter is clearly contingent. Th truth of the following statements is evident.

In necessary matter A and I are true; and O false. In contingent atter I and O are true; A and false. In impossible matter E and O are true; A and I false.

In reality, however, this part of logical doctrine i thoroughly illogical, because in treating a proposition we have no right, as already explained (p. 70), to assum ourselves acquainted with the science to which it refer our duty is to elicit the exact consequences of any statements given to us. We must learn in logic to transforminformation in every possible way, but not to add extraneous facts.

LESSON X.

CONVERSION OF PROPOSITIONS, AND IMMEDIATE INFERENCE.

WE are said to infer whenever we draw one truth from another truth, or pass from one proposition to another. As Sir W. Hamilton says, Inference is "the carrying out into the last proposition what was virtually contained in the antecedent judgments." sphere of the science of logic indeed is to teach the principles on which this act of inference must be performed, and all the previous consideration of terms and propositions is only useful or pertinent so far as it assists us to understand the processes of inference. We have to consider in succession all the modes in which the same information may be moulded into different forms of expression often implying results of an apparently different character. Logicians are not agreed exactly as to what we may include under the name Inference, and what we should not. All would allow that there is an act of inference when we see drops of water on the ground and believe that it has rained. This is a so ewhat complicated act of inference, which we shall consider in later lessons under the subject of Induction. Few or none would say that there is an act of inference in passing from "The Duke of Cambridge is the Commander-in-chief," to "The Commander-inchief is the Duke of Cambridge." But without paying much regard to the name of the process I shall in this

lesson point out all the ways in which we can from a single proposition of the forms A, , I or 0, pass to another

proposition.

We are said to convert a proposition when we tr spose its subject and predicate; but in order that the converse or converted proposition shall be inferred from the convertend, or that which was to be converted, we ust observe two rules (I) the quality of the proposition (affirmative or ne ative) ust be preserved, and ust be distributed in the Converse unless it (2) no ter. as distributed in the Convertend.

If in "all metals e elements" we were simply to transpose the terms, thus-" all ele ents are metals," we imply a certain knowledge about all elements, whereas it has been clearly shewn that the predicate of A is undistributed, and that the convertend does not really give us any info ation concerning all elements. All that infer is that "some elements are metals;" this converse proposition agrees with the rule, and the process by which we thus pass from A to I is called Conversion by mitation, or Per accidens.

When the converse is a proposition of exactly the s e form as the convertend the process is called simple conve ion. Thus from "some metals are brittle substances" I can infer "some brittle substances are etals," as all the ter s are here undistributed. Thus

I is simply converted into I.

Again, from "no metals are compounds," I can pass directly to "no co pounds are metals," because these propositions are both in , and all the terms are therefore distributed. Euler's diagram (p. 73, Fig. 3) clearly shows, that if all the metals are separated fro all the compounds, all the compounds are necessarily separated from all the metals. The proposition E is then simply converted into .

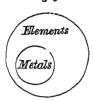
But in attempting to convert the proposition O we encounter a peculiar difficulty, because its subject is undistributed; and yet the subject should become by conversion the predicate of a negative proposition, which distributes its predicate. Take for example the proposition, "some existing things are not material substances." By direct conversion this would become "all material substances are not existing things;" which is evidently absurd. The fallacy arises from existing things being distributed in the converse, whereas it is particular in the convertend; and the rules of the Aristotelian logic prevent us from inserting the sign of particular quantity before the predicate. The converse would be equally untrue and fallacious were we to make the subject particular, as in "some material substances are not existing things." We must conclude, then, that the proposition 0 cannot be treated either by simple conversion or conversion by limitation. It is requisite to apply a new process, which may be called Conversion by Negation, and which consists in first changing the convertend into an affirmative proposition, and then converting it simply. If we attach the negation to the predicate instead of to the copula, the proposition becomes "some existing things are immaterial substances," and, converting simply, we have-"some immaterial substances are existing things," which may truly be inferred from the convertend. The proposition o, then, is only to be converted by this exceptional method of negation.

Another process of conversion can be applied to the proposition A, and is known as conversion by contraposition. From "all metals are elements," it neces sarily follows that "all not-elements are not metals." If this be not at the first moment apparent, a little reflection will render it so, and from fig. 5 we see that if all the metals be among the elements, whatever is not ele-

84 CONVERSION OF PROPOSITIONS, [LESS.

ent, or outside the circle of ele ents, ust also be outside the circle of etals. We may also prove the truth

Fig. 5.



of the contrapositive proposition in this way, if we may anticipate the contents of Lesson XXIII.:—If what is not-element should be metal, then it must be an element by the original proposition, or it must be at once an element and not an element; which is impossible according to the Primary Laws of Thought (Lesson XIV.), since nothing can both have and not have the same property. It follows that what is not-element must be not-metal.

Mistakes may readily be committed in contrapositive conversion, from a cause which will be more apparent in Lesson XXII. We are very liable to infer from a proposition of the form "all metals are elements," that all not-metals are not-elements, which is not only a false statement in itself, but is not in the least warranted by the original proposition. In fig. 5, it is apparent that because a thing lies outside the circle of metals, it does not necessarily lie outside the circle of elements, which is wider than that of metals. Nevertheless the mistake is often made in common life, and the reader will do well to re ember that the process of conversion by contraposition consists only in taking the negative of the predicate of the proposition A, as a new subject, and affirmin of it universally the negative of the old subject.

Contrapositive conversion cannot be applied to the particular propositions I and O at all, nor to the proposition, in that form; but we may change into A by attaching the negation to the predicate, and then the process can be applied. Thus "no men are perfect," may be changed into "all men are not-perfect," i.e. "are imperfect," and then we infer by contraposition "all not-imperfect beings are not-men." But not-imperfect is really the same as perfect, so that our new proposition is really equivalent to "all perfect beings are not en," or "no perfect beings are men," (E) the simple converse of the original proposition.

There remain to be described certain deductions which may be drawn from a proposition without converting its terms. They may be called immediate inferences, and have been very clearly described by Archbishop Thomson in his "Outline of the Necessary Laws of

Thought" (pp. 156, &c.).

Immediate Inference by Privative Conception consists in p sing from any affirmative proposition to a negative proposition i plied in it, or equivalent to it, or vice versa, in passing from a negative proposition to its corresponding affirmative. It is also called Obversion.

The following table contains a proposition of each kind changed by privative conception into an equivalent

proposition:

A all metals are elements.

E no metals are compounds.

(E no men are perfect.

(A all men are imperfect.

I some men are trustworthy.

some men are not untrustworthy.some men are not trustworthy.

I some men are untrustworthy.

The truth of any of the above can be clearly illustrated

by diagrams; thus it will be apparent that if the whole circle of metals lies inside the circle of elements, no part can lie outside of that circle or among the compounds, Any of the above propositions may be converted, but the results will generally be such as we have already obtained. Thus the simple converse of "no metals are compounds" is "no compounds are metals," or "no notelements are metals," the contrapositive of "all metals are elements." From the last example we get also by simple conversion "some untrustworthy beings are men." which is obviously the converse by negation, as before explained. Applying this kind of conversion to "some men are not untrustworthy," we have "some not-untrustworthy beings are men." Lastly, from "all men are imperfect" we may obtain through conversion by limitation, "some imperfect beings are men."

I ediate inference by added dete inants consists in joining some adjective or similar qualification both to the subject and predicate of a proposition, so as to render the meaning of each term narrower or better determined. Provided that no other alteration is made the truth of the new proposition necessarily follows from the

truth of the original in almost all cases.

From "all metals are elements," we may thus infer that "all very heavy metals are very heavy elements." From "a comet is a material body" we infer "a visible comet is a visible material body." But if we apply this kind of inference too boldly we may meet with fallacious and absurd results. Thus, from "all kings are men," we might infer "all incompetent kings are incompetent men;" but it does not at all follow that those who are incompetent as kings would be incompetent in other positions. In this case and many others the qualifying adjective is liable to bear different meanings in the subject and predicate; but the inference will only be true of

necessity when the meaning is exactly the same in each case. With comparative terms this kind of inference will seldom be applicable; thus from "a cottage is a building," we cannot infer "a huge cottage is a huge building," since a cottage may be large when co pared with other cottages, but not with buildings generally.

I e ate Inference by Complex Conception is closely similar to the last, and consists in employing the subject and predicate of a proposition as parts of a more complex conception. From "all metals are elements," I can pass to "a mixture of etals is a mixture of elements." From "a horse is a quadruped" I infer "the skeleton of a horse is the skeleton of a quadruped." But here again the reader must beware of applying the process where the new complex conception has a different meaning in the subject and predicate. Thus, from "all Protestants are Christians," it does not follow that "a majority of Protestants are a majority of Christians," nor that "the most excellent of the Protestants is the most excellent of the Christians."

The student is recommended to render himself familiar with all the transformations of propositions, or immediate inferences described in this lesson; and copious examples are furnished for the purpose. It is a ood exercise to throw the same proposition through a series of changes, so that it comes out in its original form at last, and thus proves the truth of all the intermediate changes; but should conversion by limitation have been used, the original universal proposition cannot be regained, but only the particular proposition corresponding to it.

On Immediate Inference, Archbishop Thomson, Outline of the Laws of Thought, §§ 85—92.

LESSON XI.

LOGICAL ANALYSIS OF SENTENCES.

PROPOSITIONS as they are usually to be found in written or spoken compositions seldom exhibit the simple form, the conjunction of a subject, copula, and predicate, which we have seen to be the proper logical construction. Not only is the copula often confused with the predicate, but several propositions may be combined into one gramatical sentence. For a full account of the analysis of sentences I shall refer to several excellent little works devoted to the subject; but I will here attempt to give a sketch of the various ways in which a sentence may be constructed.

So often is the copula united to the predicate in ordinary language, that the grammarian treats the proposition as composed of only two parts, the subject and predicate, or verb. Thus the proposition, "The sun rises," apparently contains nothing but a subject "the sun," and a predicate "rises;" but the proposition is really equivalent to "the sun is rising," in which the copula is distinctly shown. We shall, therefore, consider the v b or grammatic predicate as containing both copula d logical predicate. In Latin one single word ay combine all the three parts of the proposition, as in su, "I am;" and the celebrated exclamation of Cæsar, Veni, vidi, vici, "I came, I saw, I conquered," contains three distinct and complete propositions in three words. These peculiar cases only arise, however, from the parts of the proposition having been blended together and disguised in one word; and in the Latin sum, the letter m is a relic of the pronoun me, which is the real subject of the proposition. If we had a perfect acquaintance with the Grammar of any language it would probably not contradict the logical view of a sentence, but would perhaps explain how the several parts of the complete proposition had become blended and apparently lost, just as the words will and not are blended in the colloquial "I wont."

A atical sentence may contain any number of distinct propositions, which admit of being separated but which are combined together for the sake of brevity. In the sentence.

"Art is long and Time is fleeting," there are two distinct subjects, Art and Time, and two predicates, "long" and "fleeting," so that we have simply two propositions connected by the conjunction and. We may have however several distinct subjects with one and the sa e predicate; as in

"Thirty days hath September, April, June, and November."

In this well-known couplet the predicate "having thirty days" is placed first for the sake of emphasis, and there are four subjects, September, April, &c., of each of which it is affirmed. Hence these lines really contain four distinct propositions.

Again, there may be one subject with a plurality of predicates, so that several different propositions are asserted without the repetition of the subject and copula. Thus the sentence

"Nitrogen is a colourless, tasteless, inodorous gas, slightly lighter than air," contains one subject only, Nitrogen, but four or five predicates; it is plainly equivalent to "Nitrogen is colourless," "Nitrogen is tasteless," "Nitrogen is a gas," and so on.

Lastly, we may have several subjects and several

£

٤

Z

F

.

p

w

tc

а.

h

d.

a

h

S

Cé

predicates all combined in the same sentence, and with only one copula, so that each predicate is asserted of each subject; and a great number of distinct propositions are condensed into one brief sentence. Thus in the sentence, "Iron, Copper, Lead and Zinc are abundant, cheap and useful metals," we have evidently four subjects, and we ay be said to have four predicates, "abundant," "cheap," "useful," and "metal." As there is nothing to prevent our applying each predicate to each subject the sentence really contains 16 distinct propositions in only II words; thus "Iron is abundant," "Iron is cheap," "Copper is abundant," "Copper is cheap," and so on. In the curious sentence,—

"Hearts, tongues, figures, scribes, bards, poets, cannot think, speak, cast, write, sing, number, his love to Antony*," Shakspeare has united six subjects and six predicates, or verbs, so that there are, strictly speaking, six times six or thirty-six propositions.

In all the cases above noticed the sentence is said to be co pound, and the distinct propositions combined together are said to be coordinate with each other, that is of the same order or rank, because they do not depend upon each other, or in any way affect each other's truth. The abundance, cheapness, or utility of iron need not be stated in the same sentence with the qualities of copper, lead or zinc; but as the predicates happen to be the same, considerable trouble in speaking or writing is saved by putting as m y subjects as possible to the same set of predicates. It is truly said that brevity is the soul of wit, and one of the great arts of composition consists in condensing as many statements possible into the fewest words, so long as the meaning is not confused thereby.

^{*} Antony and Cleopatra, Act III. Sc. 2

Propositions are however combined in a totally different manner when one proposition forms a part of the subject or predicate of the other. Thus in the sentence, "The man who is upright need not fear accusation," there are two verbs, and two propositions, but one of these only describes the subject of the other; "who is upright" evidently restricts the application of the predicate "need not fear accusation" to a part of the class "man." The meaning of the whole sentence might be expressed in the form

"The upright man need not fear accusation."

And it is clearly seen that the clause or apparent proposition is substituted for an adjective. Such a clause or proposition is called subordinate, because it merely assists in the formation of the principal sentence, and has no me ing apart from it; and any sentence containing a subordinate clause is said to be so plex. Almost any part of a sentence may thus be replaced by a subordinate clause. Thus in "Oxygen and Nitrogen are the gases which for the largest part of the atmosphere," there is a subordinate clause making part of the predicate, and the meaning ight be expressed nearly as well in this way, "Oxygen and Nitrogen are the gases forming the largest part of the atmosphere."

In the case of a modal proposition (see p. 69), or one which states the manner in which the predicate belongs to the subject, the mode may be expressed either by an adverb, or by a subordinate clause. "As a man lives so he dies" is such a proposition; for it means, "a an dies as he lives," and "as he lives" is equivalent to an adverb; if he lives well, he dies well; if he lives badly, he dies badly. Adverbs or adverbial clauses may also specify the time, place, or any other circumstance con-

cerned in the truth of the main proposition.

Assuming the reader to be acquainted with the gram-

LESS-

matical terms used, we may thus state the parts of which the most complex sentence ust consist.

The subject may consist of-

- I. A noun; as in "The Queen reigns."
- 2. A pronoun; as in "She reigns."
- 3. An adjective converted into a noun; as in "Whites are civilized."
 - 4. A gerund; as "Seeing is believing."
 - 5. An infinitive; as "To see is to believe."
- 6. A subordinate clause; as "Who falls from virtue is lost."

The subject may be qualified or restricted by combining with it an attribute which may be expressed in any of the following ways:

- I. An adjective; as, "Fresh air is wholesome."
 - 2. A participle; as "Falling stars are often seen."
- 3. A noun used as an adjective; as "Iron ships are now uch employed."
- 4. A noun and preposition; as "ships of iron are now much employed."
- 5. A possessive case; as "Chatham's son was the great minister Pitt."
- 6. A noun in apposition; as "The Metropolis London is the most populous of cities."
 - 7. A gerund or dative infinitive; as, "The desire to go abroad is common in Englishmen."

The p cate consists almost always of a verb, which often has some object or qualifying words; thus it may be—

- I. A si ple tense of a complete verb; as "The sun rises."
 - 2. A compound tense; as "The sun has risen."
- 3. An incomplete verb and complement; as "The sea see s rough."

- 4. The verb "to be" and an adjective: as "Ti e is fleeting."
 - 5. A verb with an object; as "War th melts ice."
- 6. A verb with an adverbial; as "The snow falls thickly."

The **obje** of a verb is usually a noun or pronoun, but any other of the six kinds of expressions which may serve as a subject may also serve as an object.

The adverbial qualifying a verb and expressing the anner, time, place, or other circumstance affecting the proposition may be—

- 1. An adverb; as "The days pass slowly."
- 2. A noun and preposition; as "The resolution was passed by a large majority."
- 3. An absolute phrase; as "The snow melts, the sun having risen."
 - 4. A dative infinitive; as "She stoops to conquer."
- 5. Any phrase equivalent to an adverb; as "The dividends are paid twice a year."

Various modes of exhibiting the construction of sentences by symbols and names for the several parts have been invented; but I believe that by far the simplest and most efficient mode is to exhibit the construction in the form of a diagram. Any two or more parts of a sentence which are co-ordinate with each other, or bear the same relation to any other part, are written beside each other, and coupled together by a bracket; thus the diagram,—

Iron
Copper
Lead
Zinc

are

abundant,
cheap,
useful
metals,

clearly shows that there are four co-ordinate subjects,

and four co-ordinate predicates in the example previously taken.

Whenever one part of a sentence is subordinate to another part it may be connected with it by a line drawn in any convenient direction. Thus the analysis of the following sentence is readily shown by the diagram below it:—

"No one who is a lover of money, a lover of pleasure, and a lover of glory, is likewise a lover of m kind; but only he who is a lover of virtue."

who is { a lover of oney, a lover of pleasure, a lover of glory.
one is not } a lover of ankind, he only is } a lover of virtue.

We see that the sentence is both compound and complex, that is to say it contains two principal coordinate propositions with a common predicate, "a lover of ankind." The first proposition is negative and its subject is described by three subordinate clauses, while the second proposition is affirmative and has one subordinate clause.

I conclude this somewhat lengthy lesson with the analysis of a few sentences, of which the first consists of some remarkably complex lines from a poe of Burbidge:

"He who metes, as we should mete, Could we His insight use, shall most approve, Not that which fills most space in earthly eyes, ut what—though Time scarce note it as he flies— Fills, like this little daisy at my feet, Its function best of diligence in love."

```
which fills most space in earthly eyes

He shall most approve { not that but what fills best who metes its function of like this little daisy at my love feet, could we His insight use.
```

as he flies.

though Time scarce note it

"Most sweet it is with unuplifted eyes

To pace the ground, if path there be or none,
While a fair region round the traveller lies
Which he forbears again to look upon;
Ple ed rather with some soft ideal scene,
The work of fancy, or some happy tone
Of meditation slipping in between,
The beauty coming, and the beauty gone."

WORDSWORTH.

It is most sweet

To pace the ground

if path		while a fair region	
there	be or none	round the traveller lies	
		if path there { be or none	

which (region) he (the traveller) forbears to look upon

pleased rather with some soft ideal scene the work of fancy or some happy tone of meditation

slipping in between the beauty coming d the beauty gone.

In the above sentence there is evidently one subject

"to pace the ground," which by means of the pronoun it, is connected with the predicate most sweet. The main part of the sentence however consists of three adverbials, expressing the manner and surrounding circumstances, and the third adverbial is developed in a very complicated manner. The sentence is not compound, but is complex on account of four subordinate propositions.

In the following sentence there is strictly but one principal proposition, "We find," but this is only a mode of introducing the true purport of the sentence, "the two classes of intellectual operations have much that is different, much that is common."

"When the notions with which men are conversant in the common course of life, which give meaning to their familiar language and which give employment to their hourly thoughts, are compared with the ideas on which exact science is founded, we find, that the two classes of intellectual operations have much that is different, much that is common."

we find—that the two classes (* †)

of intellectual { much that is different operations have { much that is common }}

When the notions * are compared with which which give which give with the ideas + meaning men are employon which conversant to their ment to in the familiar exact science is their hourly founded. common language thoughts course of life

Here the two classes form a collective term, and have two coordinate predicates rendering the sentence so far a co pound one. The greater part of the sentence, however consists of a complicated subordinate sentence of the nature of an adverbial, expressing the time or occasion when this is found to be the case.

As a 1 texample we take the sentence given below:—
"The law of gravitation, the most universal truth at which human reason has yet arrived, expresses not merely the general fact of the mutual attraction of all matter; not erely the vague state ent that its influence decreases the distance increases, but the exact numerical rate at which that decrease takes place; so that when its amount is known at any one distance it may be exactly calculated for any other."

at which human reason has yet arrived

the most universal truth

The law of gravitation expresses

not merely the not merely the but the exact eneral fact vague statement numerical rate of the utual that its influence at which that attraction of all decreases decrease takes atter place as the distance increases

so that its amount may be calculated for any other distance when it is known at any one distance.

W. S. Dalgleish's Gram atical Analysis, or J. D. Morell's Analysis of Sentences.

Alex. Bain's English Composition and Rhetoric, pp. 91—117, treats of construction of sentences.

LESSON XII.

THE PREDICABLES, DIVISION, AND DEFINITION.

IT is desirable that the reader, before proceeding further, should acquire an exact co prehension of the meaning of certain logical terms which are known as the Predicables, meaning the kinds of terms or attributes which can always be predicated of any subject. These terms are five in number; genus, species, difference, property, and accident; and when properly employed are of exceeding use and importance in logical science. It would neither be possible nor desirable in this work to attempt to give any idea of the various and subtle eanings which have been attributed to the predicables by ancient writers, and the ost s' ple and useful view of the subject is what alone

c be given here.

Any class of things may be called a genus (Greek yévos, ce or kind), if it be regarded as made up of two

or more species. "Element" is a genus when we consider it divided into the two species "metallic and non-metallic." Triangle is a genus as regards the species

acute-angled, right-angled, and obtuse-angled.

On the other hand, a spe es is y class which is reg ded forming part of the next larger class, so that the tes genus and species are relative to each other, the enus being the larger cls which is divided, and the species the two or ore saller classes into which the genus is divided.

It is indispensable, however, to regard these expressions in the double e ing of extension and intension.

Fro the explanation of these different e 'ngs in Lesson V. it will be apparent that the extent of a enus or species is simply the number of individuals included in it, and there will always be fewer individuals in the species th in the genus. In extent the genus book includes all books of whatever size, language, or contents; if divided in respect to size the species of book are folio, quarto, octavo, duodecimo, &c.; and, of course, each of these species contains much fewer individual books th the whole genus.

In intension the genus means, not the individual things contained in it, but the sum of the qualities common to all those things, and sufficient to mark them out clearly from other classes. The species simil ly eans the su of the qualities common to all the individuals forming part of the species, and sufficient to mark the out from the rest of the genus, as well as from all other things. It is evident, therefore, that there must be more qualities implied in the meaning of the species than of the genus, for the species must contain all the qualities of the genus,

well as a certain additional quality or qualities by which the several species e distinguished fro each other. Now these additional qualities form the ference, which ay be defined the quality or sum of qualities which mark out one part of a genus from the other part or parts. The difference (Latin differentia, Greek διαφορά) cannot have any meaning except in intension, and when we use all the tes wholly in intension we may say that the difference added to the genus makes the species. Thus if "building" be the genus, dwe add the difference "used for a dwelling," we get the species "house." If we take "triangle" as the genus, it means the sum of the qualities of "three-sided rectilineal figure;" if we add the quality of "having two sides equal," we obta the species "isosceles trian le."

ay be both a enus and a species at the same ti e, ac-

cording as we regard it as divided into s aller classes or fo ing part of a larger class. Thus triangle, which is a genus as re ards isosceles triangle, is a species as regards right-lined geometrical figures. House is a species of building, but a genus with respect to ansion, cottage, villa, or other kinds of houses. We ay, in fact, have almost interminable chain of genera d species, each class being a species of the class next above it, and a genus as regards that next below. Thus the genus British subject h the species Born in the United K' gdo, Colonial-born, and Naturalised. Each of these beco es a genus as regards the species male and female; each species again may be divided into adult d inor, educated, uneducated, employed in some occupation or unemployed, self-maintaining, a tained by friends, or pauper; and so on. The subdivision ay thus proceed til we reach a class of so restricted extent, that it cannot be divided except into individuals; in this case the species is called the lowest species or infima species. All the intermediate genera and species of the chain are called subaltern (Latin sub, under, and alter, the other of two), because they stand one under the other. If there be a genus which is not regarded as a species, that is as part of any higher genus, it is called the su the highest genus, or genus generalissimu, the general genus. It is questionable whether we can thus set any limit to the chain of classes. The class British subject is certainly not an absolute su mum genus, since it is but a speci of an, which is a species of

i al, livin bein, portion of the earth, subst ce, d so on. If there were y real m u enus it would probably be "Being," or "Thing," or "Object conceivable;" but we ay usefully e ploy the te to signify the highest class of things comprehended in any science or classification. Thus "material substance" is the sumum genus ex ined in the science of che istry; "inhabitant of the United Kingdo" is the summu enus enumerated and classified in the ritish census. Logical terms are only a species of words or phrases, but they are the summum enus as regards logic, which has nothing to do with the various parts of speech d the relations of words, syllables, and letters, ex ed by grammarians.

Several very useful expressions have been derived from the words genus and species. When a th'g is so peculiar and unlike other things that it cannot easily be brought into one class with them, it is said to be sui generis, or of its own genus; thus the rings of Saturn are so different fro anything else a ong the heavenly bodies that they may fairly be called sui generis. In zoology, the Ornithorhynchus, or Australian Duck-bill, the Amphioxus, and some other i als, are so peculiar that they may be called sui generis. When a subst ce is the same in all its parts, or when a number of things are all alike, we say that they are homogeneous (Greek ôµôs, like, yévos, kind), that is of the sa e nature; otherwise they may be called heterogeneous (Greek ĕrepos, other).

It is necessary to distinguish carefully the purely logical use of the terms genus and species from their peculiar use in natural history. A species is there a class of plants d animals supposed to have descended fro common parents, and to be the narrowest class possessing a fixed form; the genus is the next higher class. ut if we accept Darwin's theory of the origin of species, this definition of species becomes entirely illusory, since different genera and species must have according to this theory descended from common parents. The species then denotes a merely bitrary amount of rese blance

which naturalists choose to fix upon, and which it is not possible to define more exactly. This use of the te no connection whatever with the logical use. accordin to which any class of things whatever is a species, provided it is regarded as part of a wider class or enus.

The fourth of the Predicables is Property (Latin propriu, Greek 1810, own), which it is hardly possible to define in a anner free from objection and difficulty, but ay perhaps be best described as which v quality which is common to the whole of a class, but is not necesark out that class from other classes. a property of the genus "triangle" to have the three internal angles equal to two right angles; this is a very re arkable circumstance, which is always true of triangles, but it is not ade a part of the genus, or is not e ployed in defining a trian le, because the possession of three straight sides is a sufficient mark. The properties of geo etrical figures are very numerous; the Second Book of Euclid is occupied in proving a few properties of rect-

gles: the Third Book similarly of circles. As we comonly use the term property it may or may not belong to other objects as well as those in question; some of the properties of the circle may belong also to the ellipse; so e of the properties of man, as for instance the power of emory, or of anger, may belong to other animals.

Logicians have invented various subtle divisions of properties, but it will be sufficient to say that a peculiar property is one which belongs to the whole of a class, and to that class only, as laughter is supposed to belong only to

ankind; the property of containing the greatest space in a line of given length is peculiar to circles. When a property is not peculiar, it may belong to other classes of objects as well as that of which it is called the property. We may further distinguish the neric Property, or that

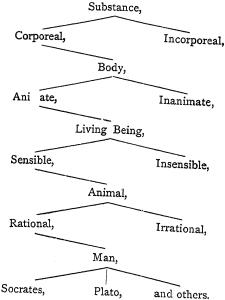
which belongs to the whole of the genus, from the Specific Property, which belongs to the whole of a lowest species.

Lastly, an accident (Latin accidens, Greek συμβεβηκός) is any quality which may indifferently belong or not belong to a class, as the case ay be, without affecting the other qualities of the cl s. The word means that which falls or happens by chance, and has no necessary connection with the nature of a thing. the absolute size of a triangle is a pure accident as regards its geometrical properties; for whether the side of a triangle be to of an inch or a million miles, whatever Euclid proves to be true of one is true of the other. The birthplace of a man is an accident concerning him, as are also the clothes in which he is dressed, the position in which he rests, and so on. Some writers distinguish separable and inseparable accidents. Thus the clothes in which a man is dressed is a sep able accident, because they can be changed, as can also his position, and many other circumstances; but his birthplace, his height, his Christian name, &c., are inseparable accidents, because they can never be changed, although they have no necessary or important relation to his general character.

illustration of so e part of the scheme of clas-As sification described under the name of Predicables, I may here give, as is usual in manuals of Logic, the Tree of Porphyry, a sort of example of classification invented by one of the earliest Greek logicians, named Porphyrius. I have simplified the common form in which it is given by translating the Latin names and omitting superfluous

words.

In this Tree we observe a succession of genera and species-Substance, Body, Living Being, Animal and Man. Of these Substance is the summum genus, because it is not regarded as a species of any higher class; Man is the *infi* a species, because it is a class not divided into any lower cl s, but only into individuals, of whom it is



usual to specify Socrates and Plato. Body, Living Being, and Ani al are called subaltern genera and species, because each is a species as regards the next higher genus, and a genus as regards the next lower species. The qualities implied in the adjectives Corporeal, Animate, Sensible (i.e. capable of feeling) and Rational are the successive differences which occasion a division of each genus into species. It will be evident that the negative parts of the enera, namely Incorporeal Substance, In-

i ate Body, &c., are capable of subdivision, which has not been carried out in order to avoid confusing the figure.

Logic vision is the name of the process by which we distinguish the species of which a genus is composed. Thus we are said to divide the genus "book" when we consider it as ade up of the groups folio, quarto, octavo, duodeci o books, &c., and the size of the books is in this case the ground, basis, or principle of division, commonly called the Funda ent ivisionis. In order that a quality or circumstance may be taken as the basis of division, it ust be present with some and absent with others, or ust vary with the different species comprehended in the genus. A generic property of course, being present in the whole of the genus, cannot serve for the purpose of division. Three rules may be laid down to which a sound and useful division must conform:

- I. The constituent species must exclude each other.
- 2. The constituent species must be equal when added together to the genus.
- 3. The division must be founded upon one principle or basis.

It would be obviously absurd to divide books into folio, quarto, French, German and dictionaries, because these species overlap each other, and there may be French or German dictionaries which happen to be quarto or folio and belong to three different species at once. A division of this kind is said to be a Cross Division, because there is more than one principle of division, and the several species in consequence cross each other and produce confusion. If I were to divide rectilineal figures into triangles, parallelograms, rectangles and polygons of more than four sides, I should com it all the possible faults in one division. The species parallelogram and rectangle do not exclude each other, since all rectangles must be

p allelograms; the constituent species are not altogether equal to the genus rectilineal figure, since irregular foursided figures which are not parallelograms have been omitted; and there are three principles of division, namely the nu ber of sides, the directions of those sides, and the angles contained. But when subdivision is employed. and each of the species is considered as a genus which av be subjected to a further separation, a new principle

of division may and in fact must be employed each time. Thus I can divide rectilineal figures according to the three

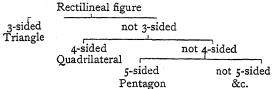
principles mentioned above:

	Rectilineal Figu	ıre	
3 sides	4 sides	more than 4 sides	
Triangle	Quadrilateral	Polygo	
with parallel sides		without parallel	
Parallelogram		sides	
		Trapezium.	

Here the principles of division are the number of their sides, and in the case of four-sided figures their parallelism. Triangles do not admit of division in this second respect. We may make a new division of parallelograms. adopting the equality of sides and the size of the angles as the principles: thus:

-	_			
	Paral	lelog	ram	
adjoining sides equal		adjoining sides not equal		
right- angled Square	not right- angled Rhombus	•	ri ht- angled Oblong	not right- angled Rhomboid.

The most perfect divisions in a logical point of view are produced by continually dividing each enus into two species by a difference, of which an example h been given in the Tree of Porphyry. This process is called Dichoto y (Greek $\delta i \chi a$, in two; $\tau \epsilon \mu \nu \omega$, to cut); it is also called tive vision because it always of necessity obeys the second rule, and provides a place for every possible existing thing. By a Law of Thought to be considered in the next Lesson, every thing must either have a quality or not have it, so that it must fall into one or other division of the genus. This process of exhaustive division will be shewn to have considerable import ce in Lesson XXIII., but in practice it is not by any means always necessary or convenient. It would, for instance, produce a needlessly long classification if we divided rectilineal figures thus:



As we know beyond all doubt that every figure ust have 3, 4, 5, 6, or more sides, and no figure c belong to more than one group, it is uch better at once to enumerate the parts as Triangle, Quadrilateral, Pentagon, Hexagon, &c. Again, it would be very awkward if we divided the counties of England into Middlesex and not-Middlesex; the latter into Surrey and not-Surrey; the latter, again, into Kent and not-Kent. Dichoto y is useless, and even seems absurd in these cases, because we c observe the rules of division certainly in a much briefer division. ut in less certain branches of knowledge our divisions can never be free from possible oversight unless they proceed by dichoto y. Thus, if we divide the population of the world into three br ches, Aryan, Semitic, and

Turanian, so e race might ultimately be discovered which is distinct fro y of these, and for which no place has been provided: but had we proceeded thus—

	Man	
Aryan	not-	Aryan
	Semitic	not-Semitic
	Turania	n not-Turanian,

it is evident that the new race would fall into the last group, which is neither Aryan, Semitic, nor Turanian. All the divisions of naturalists are liable to this inconvenience. If we divide Vertebrate Ani als into Mammalia, Birds, Reptiles, and Fish, it ay any ti e happen that a new form is discovered which belongs to none of these, and therefore upsets the division.

A further precaution required in Division is not to proceed from a high or wide genus at once to a low or narrow species, or, as the phrase is, divisio non faciat saltum (the division should not make a leap). The species should always be those of the proximate or next higher genus; thus it would obviously be inconvenient to begin by dividing geometrical figures into those which have parallel sides and those which have not; but this principle of division is very proper when applied to the proximate genus.

Logical division must not be confused with physical division or Partition, by which an individual object, as a tree, is regarded as co posed of its separate parts, root, trunk, branches, leaves, &c. There is even a third and distinct process, called etaphysical ivision, which consists in regarding a thing as an aggregate of qualities, and separatin these in thought; as when we discri inate the form, colour, taste, ds ell of an orange.

Closely connected with the subject of this Lesson is

the process of Lo cal e tion, by which we determine the co mon qualities or arks of the objects belongin to any given class of objects. We ust give in a definition the briefest possible statement of such qualities as

e sufficient to distinguish the class from other classes, and determine its position in the general classification of conceptions. Now this will be fulfilled by regarding the class as a species, and giving the proximate genus and the difference. The word genus is here used in its intensive meanin, and denotes the qualities belonging to all of the genus, and sufficient to mark them out; and as the difference marks out the part of the genus in question, we get a perfect definition of the species desired. But we should be careful to give in a definition no superfluous

arks; if these are accidents and do not belong to the whole, the definition will be i properly narrowed, as if we were to define Quadrilateral Figures as figures with four equal sides; if the superfluous marks belong to all the things defined they are Properties, and have no effect upon the definition whatever. Thus if I define parallelograms as "four-sided rectilineal figures, with the opposite sides equal and parallel, d the opposite angles equal," I have added two properties, the equality of the opposite sides and angles which necessarily follow from the parallelis of the sides, and only add to the complexity of the definition without rendering it more precise.

There are certain rules usually given in logical works which express the precautions necessary in definition.

1. A definition should state the essential attributes of the species defined. So far as any exact meaning can be given to the expression "essential attributes," it means, as explained above, the proximate genus and difference.

2. A definition must not contain the name defined. For the purpose of the definition is to ake the species known, and as long as it is not known it cannot serve to

make itself known. When this rule is not observed, there is said to be 'circulus in definiendo,' or 'a circle in de ning,' because the definition brings us round again to the very word from which we started. This fault will usually be com itted by usin a word in the definition which is really a synonym of the name defined, if I were to define "Pl t" as "organized bein possessin vegetable life," or elements as simple substances, ve etable being really equivalent to plant, and simple to elementary. If I were to define metals as "substances possessing metallic lustre," I should either commit this fault, or use the term metallic lustre in a sense which would admit other substances, and thus break the following rule.

3. The definition must be exactly equivalent to the species defined, that is to say, it must be an expression the denotation of which is neither narrower nor wider than the species, so as to include exactly the same objects. The definition, in short, must denote the species, the whole species, and nothing but the species, and this ay really be considered a description of what a definition is,

4. A definition must not be expressed in obscure, figurative or ambiguous language. In other words, the terms employed in the definition must be all exactly known, otherwise the purpose of the definition, to make us acquainted with the sufficient marks of the species, is obviously defeated. There is no worse logical fault than to define ignotum per ignotius, the unknown by the still ore unkno. Aristotle's definition of the soul as 'The Entelechy, or first form of an organized body which has potential life,' certainly seems subject to this objection.

5. And lastly, A definition must not be negative where it can be affir ative. This rule however is often not applicable, and is by no means always binding.

Read Mr Mill on the nature of Cl sification and the

five Predicables, System of Logic, Book I. Chap. VII. For ancient Scholastic Views concerning Definition, see Mansel's Artis Logicæ Rudimenta (Aldrich), App. Note C.

LESSON XIII.

PASCAL AND DESCARTES ON METHOD.

IT may be doubted whether any man ever possessed a ore acute and perfect intellect than that of Blaise Pascal. He was born in 1623, at Clermont in Auvergne, and from his earliest years displayed signs of a remarkable character. His father attempted at first to prevent his studying geometry, but such was Pascal's genius and love of this science, that, by the age of twelve, he had found out many of the propositions of Euclid's first book without the aid of any person or treatise. It is difficult to say whether he is most to be admired for his mathematical discoveries, his invention of the first calculating machine, his wonderful Provincial Letters written against the Jesuits, or for his profound Pensées or Thoughts, a collection of his reflections on scientific and religious topics.

Among these Thoughts is to be found a remarkable fragment upon Logical method, the substance of which is also given in the Port Royal Logic. It forms the second article of the Pensées, and is entitled Réflexions sur la Géo étrie en général. As I know no composition in which perfection of truth and clearness of expression are ore nearly attained, I propose to give in this lesson a free translation of the more i portant parts of this

fragment, appending to it rules of method from the Port Royal Logic, and from Descartes' celebrated Essay on Method. The words of Pascal are nearly as follows.

"The true ethod, which would furnish de onstrations of the highest excellence, if it were possible to e ploy the method fully, consists in observing two principal rules. The first rule is not to employ any term of which we have not clearly explained the meaning; the second rule is never to put forward any proposition which we cannot demonstrate by truths already known; that is to say, in a word, to define all the terms, and to prove all the propositions. But, in order that I may observe the rules of the method which I am explaining, it is necessary that I declare what is to be understood by efinition.

"We recognise in Geometry only those definitions which logicians call omin efinitions, that is to say, only those definitions which impose a name upon things clearly designated in terms perfectly known; and I speak

only of those definitions."

Their value and use is to clear and abbreviate discourse by "expressing in the single name which we i pose what could not be otherwise expressed but in several words; provided nevertheless that the name imposed remain divested of any other eaning which it ight possess, so as to bear that alone for which we

intend it to stand.

"For example, if we need to distinguish among n bers those which are divisible into two equal parts, from those which are not so divisible, in order to avoid the frequent repetition of this distinction, we give a name to it in this anner:—we call every number divisible into two equal parts an Even Nu ber.

"This is a eo etrical definition, because after havin cle ly designated a thing, na ely y nu ber divisible to two equal parts, e ive it a n e divested of every other eaning, which it might have, in order to bestow

upon it the meaning designated.

"Hence it appears that definitions are very free, and that they can never be subject to contradiction, for there is nothing more allowable, than to give any na e we wish to a thing which we have clearly pointed out. It is only necessary to take care that we do not abuse this liberty of imposing names, by giving the same name to two different things. Even that would be allowable, provided that we did not confuse the results, and extend them fro one to the other. But if we fall into this vice, we have a very sure and infallible remedy; -it is, to substitute mentally the definition in place of the thing defined, and to hold the definition always so present in the ind, that every time we speak, for instance, of an even number, we may understand precisely that it is a number divisible into two equal parts, and so that these two things should be so combined and inseparable in thought, that as often as one is expressed in discourse, the mind may direct itself immediately to the other.

"For geometers and all who proceed methodically only impose names upon things in order to abbreviate discourse, and not to lessen or change the ideas of the things concerning which they discourse. They pretend that the mind always supplies the entire definition of the brief terms which they employ simply to avoid the confusion produced by a multitude of words.

"Nothing prevents more promptly and effectively the insidious fallacies of the sophists than this method, which we should always employ, and which alone suffices to banish all sorts of difficulties and equivocations.

"These things being well understood, I return to y explanation of the true method, which consists, as I said, in defining everything and provin everything.

"Certainly this ethod would be an excellent one,

It is evident that the were it not absolutely impossible. s we wished to define would require previous ter s to serve for their explanation, and similarly the first propositions we wished to prove, would presuppose other propositions preceding the in our knowledge; and thus it is cle that we should never arrive at the first

ter s or first propositions.

"Accordingly in pushing our researches further and further, we arrive necessarily at primitive words which we cannot define, and at principles so clear, that we cannot find any principles more clear to prove them by. it appears that men are naturally and inevitably incapable of treating any science whatever in a perfect method; but it does not thence follow that we ought to abandon every kind of method.....The most perfect method available to men consists not in defining everything and demonstrating everything, nor in defining nothing and de-

onstrating nothing, but in pursuing the middle course of not defining things which are clear and understood by all persons, but of defining all others; and of not proving truths known to all persons, but of proving all others. ethod they equally err who undertake to ded prove everything, and they who neglect to do it

in things which are not self-evident."

It is made plain in this admirable passage that we can never by using words avoid an ultimate appeal to things, because each definition of a word must require one or ore other words, which also will require definid so on ad infinitum. Nor must we ever return back upon the words already defined; for if we define Aby B, and B by C, and C by D, and then D by A, we ay be called a circulus in definiendo; a ost serious fallacy, which might lead us to suppose that we know the nature of A, B, C, d D, when we really know nothing about the

Pascal's views of the geometrical method were clearly summed up in the following rules, inserted by him in the *Port Royal Logic**.

 To admit no terms in the least obscure or equivocal without defining them.

2. To employ in the definitions only terms perfectly known or already explained.

3. To demand as axioms only truths perfectly evident.

4. To prove all propositions which are at all obscure, by e ploying in their proof only the definitions which have preceded, or the axioms which have been accorded, or the propositions which have been already demonstrated, or the construction of the thing itself which is in dispute, when there may be any operation to perform.

5. Never to abuse the equivocation of terms by failing to substitute for them, mentally, the definitions which

restrict and explain them.

The reader will easily see that these rules are much more easy to lay down than to observe, since even geometers are not agreed as to the simplest axioms to assume, or the best definitions to make. There are many different opinions as to the true definition of parallel lines, and the simplest assumptions concerning their nature; and how much greater must be the difficulty of observing Pascal's rules with confidence in less certain branches of science. Next after Geometry, Mechanics is perhaps the ost perfect science, yet the best authorities have been far fro agreeing as to the exact definitions of such notions as force, mass, oment, power, inertia, and the ost different opinions are still held as to the simplest os by which the law of the composition of forces may

be proved. Nevertheless if we steadily bear in mind, in

* Mr Spencer Baynes' Translation, p. 317.

studying each science, the necessity of defining every term as far as possible, and proving each proposition which can be proved by a simpler one, we shall do much to clear away error and confusion.

I also wish to give here the rules proposed by the celebrated Descartes for guiding the reason in the attainent of truth. They are as follows:—

- 1. Never to accept anything as true, which we do not clearly know to be so; that is to say, carefully to avoid haste or prejudice, and to co prise nothing more in our judgments than what presents itself so clearly and distinctly to the mind that we cannot have any room to doubt it.
- 2. To divide each difficulty we examine into as many parts as possible, or as may be required for resolving it.
- To conduct our thoughts in an orderly manner, co mencing with the most simple and easily known objects, in order to ascend by degrees to the knowledge of the most complex.
- 4. To make in every case enumerations so complete, and reviews so wide, that we may be sure of o itting nothing.

These rules were first stated by Descartes in his admirable Discourse on Method, in which he gives his reflections on the right mode of conducting the reason, and searching for truth in any of the sciences. This little treatise is easily to be obtained in the original French, and has also been translated into English by Mr Veitch*. The reader can be strongly advised to study it. Always to observe the rules of Descartes and Pascal, or to know whether we in every case observe the properly, is i

^{*} Published at Edinburgh in 1850.

possible, but it ust nevertheless be valuable to know at what we ou ht to aim.

Read Locke's brief Essay on the Conduct of the Understanding, which contains admirable re arks on the acquirement of exact and logical habits of thought.

LESSON XIV.

THE LAWS OF THOUGHT.

BEFORE the reader proceeds to the lessons which treat of the most common forms of reasoning, known as the syllogism, it is desirable that he should give a careful attention to the very simple laws of thought on which all reasoning must ultimately depend. These laws describe the very simplest truths, in which all people must agree, and which at the same time apply to all notions which we can conceive. It is impossible to think correctly and avoid evident self-contradiction unless we observe what are called the Three Primary Laws of Thought, which may be stated as follows:

- I. The Law of Identity. Whatever is, is.
- The Law of Contradiction. Nothing c both be and not be.
- The Law of Excluded Middle. Everything ust either be or not be.

Though these laws when thus stated may seem absurdly obvious, and were ridiculed by Locke and others on that account, I have found that students are seldo able to see at first their full meaning and i portance. It will be pointed out in Lesson XXIII. that logici s have

overlooked until recent years the very simple way in which all arguments may be explained when these self-evident laws are granted; and it is not too uch to say that the whole of logic will be plain to those who will constantly use these laws as the key.

The first of the laws may be regarded as the best definition we can give of identity or sameness. Could y one be ignorant of the meaning of the word Identity, it would be sufficient to inform him that everything is identical with itself.

The second law however is one which requires more consideration. Its meaning is that nothing can have at the same time and at the sa e place contradictory and inconsistent qualities. A piece of paper may be blackened in one part, while it is white in other parts: or it may be white at one ti e, and afterwards become black; but we cannot conceive that it should be both white and black at the same place and time. A door after being open may be shut, but it cannot at once be shut and open. Water ay feel wa to one hand and cold to another hand, but it cannot be both warm and cold to the same hand. No quality can both be present and absent at the same time; and this seems to be the most simple and general truth which we can assert of all things. It is the very nature of existence that a thing cannot be otherwise than it is; and it may be safely said that all fallacy and error arise fro unwittingly reasoning in a way inconsistent with this law. All statements or inferences which i ply a co bination of contradictory qualities ust be taken as i possible and false, and the breaking of this law is the ark of their being false. It easily be shewn that if Iron be a etal, and every ele ent. Iron must be ele ent or it can be nothin at all, since it would co bine qualities which are inconsistent (see Lesson XXIII).

The Law of Excluded Middle is much less self-evident than either of the two preceding ones, and the reader will not perhaps see at the first mo ent that it is equally important and necessary with them. Its meaning may be best explained by saying that it is impossible to mention any thing and any quality or circumstance, without allowing that the quality or circumstance either belongs to the thing or does not belong. The name of the law expresses the fact that there is no third or middle course; the answer must be Yes or No. Let the thing be rock and the quality hard; then rock must be either hard or not-hard. Gold must be either white or not white; a line must be either straight or not straight; an action must be either virtuous or not virtuous. Indeed when we know nothing of the terms used we may neverake assertions concerning them in accordance with this law. The reader may not know and in fact che ists may not really know with certainty, whether is a metal or not a metal, but any one knows that it must be one or the other. Some readers know what a cycloid is or what an isochronous curve is; but they must know that a cycloid is either an isochronous curve or it is not an isochronous curve.

This law of excluded middle is not so evident but that plausible objections may be suggested to it. Rock, it may be urged, is not always either hard or soft, for it ay be half way between, a little hard and a little soft at the same time. This objection points to a distinction which is of great logical importance, and when neglected often leads to fallacy. The law of excluded middle affirmed nothing about hard and soft, but only referred to hard

d not-hard; if the reader chooses to substitute soft for not-hard he falls into a serious confusion between opposite terms and cont ctory ter s. It is quite possible that a thing may be neither hard nor soft, being half way

between; but in that case it cannot be fairly called hard, so that the law holds true. Similarly water must be either warm or not-warm, but it does not follow that it must be warm or cold. The alternative not-war dently includes all cases in which it is cold besides cases where it is of a medium temperature, so that we should call it neither warm nor cold. We must thus carefully distinguish questions of de ee or quantity from those of simple logical fact. In c es where a thing or quality may exist to a greater or less extent there are any alternatives. Warm water, for, instance may have any temperature from 70° perhaps up to 120°. Exactly the same question occurs in cases of geometrical reasoning; for Euclid in his Elements frequently argues from the selfevident truth that any line ust be either greater than, equal to, or less than any other line. While there are only two alternatives to choose from in logic there are three in Mathematics; thus one line, compared with another, may be-

Another and even more plausible objection ay be raised to the third law of thought in this way. Virtue bein the thing proposed, and triangular the quality, the Law of Excluded Middle enables us at once to sert that virtue is either triangular or not-triangular. At first sight it might see false and absurd to say that i material notion such virtue should be either triangular or not, because it h nothing co on with those material substances occupying space to which the notion of figure belon s. ut the absurdity would arise, not from any falseness the law, but fro isinterpretation of the expr sion not-tr ngular. If in saying that a thing is

xiv.

"not triangular" we are taken to imply that it has so e figure though not a triangular figure, then of course the expression cannot be applied to virtue or anything i -

aterial. In strict logic however no such i plied eaning is to be allowed, and not-triangular will include both things which have figure other than trian ular, as well as things which have not the properties of figure at all; and it is in the latter meaning that it is applicable to an immaterial thing.

These three laws then being universally and necessarily true to whatever things they are applied, beco e the foundation of reasoning. All acts of reasoning proceed from certain judgments, and the act of judgment consists in comparing two things or ideas together and discovering whether they agree or differ, that is to say whether they are identical in any qualities. The laws of thought inform us of the very nature of this identity with which all thought is concerned. But in the operation of discourse or reasoning we need certain additional laws, or axioms, or self-evident truths, which may be thus stated:

1. Two terms agreeing with one and the same third term agree with each other.

2. Two terms of which one agrees and the other does not agree with one and the same third term, do not agree with each other.

These self-evident truths are commonly called the c ons or Funda ental Principles of Syllogism, and they are true whatever may be the kind of agreement in question. The example we for erly used (p. 3) of the agreement of the terms "Most useful etal" and "cheapest

etal" with the third common ter "Iron," was but an instance of the first Canon, and the agreement consisted in co plete identity. In the case of the "Earth," the "Planets," and "Bodies revolving in elliptic orbits," the agree ent was less complete, because the Earth is only one of many Planets, and the Planets only a small portion of all the heavenly bodies, such as Satellites, d Double-Stars which revolve in Comets. Meteors, such orbits.

The second of the Canons applies to cases where there is disagreement or difference, as in the following example:

Venus is a planet.

Planets are not self-luminous.

Therefore Venus is not self-lu inous.

The first of these propositions states a certain agreement to exist between Venus and planet, just as in the previous c e of the Earth, but the second proposition states a disagreement between Planet and self-luminous bodies: hence we infer a disagreement between Venus and self-luminous body. But the reader will carefully observe that from two disagreements e can never infer anything. If the following were put forth as an argument it would be evidently absurd:-

> Sirius is not a planet. Planets are not self-luminous. Therefore Sirius is not self-lu inous.

Both the premises or propositions given are true, and yet the conclusion is false, for all the fixed stars are self-luminous, or shine by their own light. We may, in fact, state as a third c on that-

3. Two terms both disagreeing with one and the ay or may not agree with each other.

Self-evident rules, of an exactly si ilar nature to these three C ons, are the basis of all mathematical reasoning. e usually called axioms. Euclid's first axio that "Things which are equal to the same thing are equal to one another;" d whether we apply it to the length of lines, the agnitude of an les, areas, solids, numbers, degrees, or anything else which admits of being equal or unequal, it holds true. Thus if the lines A and B are each equal to C it is evident that each is equal to the other.

A B C D

Euclid does not give axioms corresponding to the second and third Canons, but they are really used in Geometry. Thus if A is equal to B, but D is not equal to B, it follows that A is not equal to D, or things of which one is equal, but the other unequal to the same third thing, are unequal to each other. Lastly, A and E are two lines both unequal to D and unequal to each other, whereas A and B are two lines both unequal to D but equal to each other; thus we plainly see that "two things both unequal to the same thing may or may not be equal to each other."

From what precedes it will be apparent that all reasoning requires that there should be one agreement at least; if there be two agreements we may reason to a third agreement; if there be one agreement and one difference we may reason to a second difference; but if there be two differences only we cannot reason to any conclusion whatever. These self-evident principles will in the next Lesson serve to explain some of the rules of the Syllogism.

Logicians however have not confined themselves to the use of these Canons, but have often put the same truth into a different form in an axiom called the *Dictum de omni et nullo* of Aristotle. This celebrated Latin phrase eans "Statement concerning all and none," and the axiom, or rather pair of axioms, is usually given in the following words:

Whatever is predicated of a ter distributed whether affirmatively or negatively, may be predicated in like anner of everything contained under it.

Or ore briefly:

What pertains to the higher class pertains also to the lower.

erely means, in untechnical language, that This ay be said of all the thin s of any sort or kind ay be said of any one or any part of those things; and, secondly, what ay be denied of all the things in a class ay be denied of any one or any part of the . Whatever may be said of "All planets" may be said of Venus, the Earth, Jupiter, or any other planet; and, as they may all be said to revolve in elliptic orbits, it follows that this ay be asserted of Venus, the Earth, Jupiter, or any other planet. Similarly, according to the negative part of the Dicta, we ay deny that the planets are selflu inous, and knowing that Jupiter is a planet may deny that Jupiter is self-luminous. A little reflection would show that the affirmative Dictum is really the first of the C ons in a less co plete and general form, and that the ne ative Dictum is similarly the second Canon. These Dicta in fact only apply to such cases of agreement between te s as consist in one being the name of a smaller class, and another of the larger class containing it. Logici s have for the ost part strangely overlooked the i port t cases in which one te agrees with another to the extent of being identical with it; but this is a subject which we c not fitly discuss here at any length. It is treated in y little work called The Substitution of Si ilars*.

So e logicians have held that in addition to the three laws which are called the Pri ary Laws of Thought,

^{*} Macmill d Co. 1869.

there is a fourth called "The Principle or Law of Sufficient Reason." It was stated by Leibnitz in the following words:

Nothing happens without a reason why it should be so rather than otherwise. For instance, if there be a pair of scales in every respect exactly alike on each side and with exactly equal weights in each scale, it must remain motionless and in equilibrium, because there is no reason why one side should go down more than the other. It is certainly a fundamental assumption in mechanical science that if a body is acted upon by two perfectly equal forces in different directions it will move equally between the , because there is no reason why it should move more to one side than the other. Mr Mansel, Sir W. Hamilton and others consider however that this law has no place in logic, even if it can be held self-evident at all; and the question which appears open to doubt need not be discussed here.

I have so freely used the word axiom in this lesson that it is desirable to clear up its meaning as far as possible. Philosophers do not perfectly agree about its derivation or exact meaning, but it certainly comes from the verb àξιώω, which is rendered, to think worthy. It generally denotes a self-evident truth of so simple a character that it must be assumed to be true, and, as it cannot be proved by any simpler proposition, must itself be taken as the basis of reasoning. In mathematics it is clearly used in this sense.

See Hamilton's Lectures on Logic, Lectures 5 and 6.

LESSON XV.

THE RULES OF THE SYLLOGISM.

SYLLOGISM is the common name for Mediate Inference, or inference by a medium or middle term, and is to be distinguished from the process of Immediate Inference, or inference which is performed without the use of any third or middle term.

We are in the habit of employing a iddle te or medium whenever we are prevented from comparing two things together directly, but can compare each of them with a certain third thing. We cannot compare the sizes of two halls by placing one in the other, but we can

easure each by a foot rule or other suitable measure, which forms a comon measure, and enables us to ascertain with any necessary degree of accuracy their relative dimensions. If we have two quantities of cotton goods and want to compare them, it is not necessary to bring the whole of one portion to the other, but a sample is cut off, which represents exactly the quality of one portion, and, according as this sample does or does not agree with the other portion, so ust the two portions of goods agree or differ.

The use of a iddle term in syllogism is closely parallel to what it is in the above instances, but not exactly the sa e. Suppose, as an example, that we wish to ascertain whether or not "Whales are viviparous," and that we had not an opportunity of observing the fact directly; we could yet show it to be so if we knew that "whales are mammalian animals," and that "all a

alian ani als are viviparous." It would follow that "whales are viviparous;" and so far as the inference is concerned it does not matter what is the eaning we attribute to the words viviparous and ma alian. In this case "mammalian animal" is the middle term.

The name Syllogis means the joining together in thought of two propositions, and is derived fro the Greek words σύν, together, and λόγος, thought. is thus exactly the equivalent of the word Computation, eans thinking together (Latin con, together, puto, to think), or reckoning. In a syllogism we so unite in thought two premises, or propositions put forward, that we are enabled to draw from them or infer, by means of the middle term they contain, a third proposition called the conclusion. Syllogism may thus be defined as the act of thought by which from two given propositions we proceed to a third proposition, the truth of which necessarily follows from the truth of these given propositions. When the argument is fully expressed in language it is usual to call it concretely a syllogism.

The special rules of the syllogism are founded upon the Laws of Thought and the Canons considered in the previous Lesson. They serve to inform us exactly under what circumstances one proposition can be inferred from two other propositions, and are eight in number, as follows:—

1. Every syllogism has three and only three terms.

These terms are called the ajor term, the minor term, and the middle term.

2. Every syllogism contains three, and only three propositions.

These propositions are called the ajor pre ise, the inor pre ise, and the conclusion.

3. The middle ter ust be distributed once at least, and ust not be ambiguous.

- 4. No term must be distributed in the conclusion which was not distributed in one of the premises,
 - 5. From negative premises nothing can be inferred.
- 6. If one premise be negative, the conclusion ust be negative; and vice versa, to prove a negative conclusion one of the premises must be negative.

From the above rules may be deduced two subordinate rules, which it will nevertheless be convenient to state at once.

- 7. From two particular premises no conclusion can be drawn.
- 8. If one premise be particular, the conclusion must be particular.

All these rules are of such extre e importance that it will be desirable for the student not only to acquire a perfect comprehension of their meaning and truth, but to commit them to emory. During the remainder of this lesson we shall consider their meaning and force.

As the syllogis consists in comparing two terms by eans of a middle term, there cannot of course be less than three terms, nor can there be more; for if there were four terms, say A, B, C, D, and we compared A with B and C with D, we should either have no common medium at all between A and D, or we should require a second syllogism, so as first to compare A and C with B, and then A and D with C.

The iddle ter may always be known by the fact that it does not occur in the conclusion. The ajor te is always the predicate of the conclusion, and the inor te the subject. These terms are thus called because in the universal affirmative proposition (A) the predicate is necessarily a wider or greater or ajor ter th the subject; thus in "all en are ortals," the predicate includes all other ani als as well as men, and is obviously a major te or wider te than en.

XV.] THE RULES OF THE SYLLOGISM. 129

Again, the syllogism necessarily consists of a premise called the major premise, in which the major and iddle terms are compared together; of a minor premise which similarly compares the minor and iddle terms; and of a conclusion, which contains the major d inor terms only. In a strictly correct syllogis the ajor premise always stands before the minor pre ise, but in ordin y writing and speaking this rule is seldom observed; and that pre ise which contains the major ter still continues to be the major pre ise, whatever may be its position.

The third rule is a very important one, because many fallacies arise from its neglect. By the middle term bein distributed once at least, we mean (see p. 74) that the whole of it must be referred to universally in one premise, if not both. The two propositions—

All Russians are Europeans,

do not distribute the iddle term at all, because they are both affirmative propositions, which have (p. 75) undistributed predicates. It is apparent that Frenchen are one part of Europeans, and Russians another part, as shown in Euler's method in Fig. 6, so that

Fig. 6.

Europeans

Russians

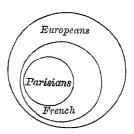
130 THE RULES OF THE SYLLOGISM. [LESS.

there is no real middle term. Those propositions would equally allow of Russians being or not being Frenchmen; for whether the two interior circles overlap or not they are equally within the larger circle of Europeans. Again, the two propositions

All Parisians are Europeans,

do not enable us to infer that all Parisians are Frenchen. For though we know of course that all Parisians

Fig. 7.



are included among Frenchmen, the premises would allow of their being placed anywhere within the circle of Europeans. We see in this instance that the premises and conclusion of an apparent arguent ay all be true d yet the argument may be fallacious.

The part of the third rule which refers to an a bious id e te hardly requires explanation. It h been stated (Lesson IV.) that an ambiguous ter is one which h two different eanings, implying different connotations, and it is really equivalent to two different terms which happen to have the same form of spelling, so that they are readily mistaken for each other. Thus if we were to argue that because "all metals are elements and

brass is metal, therefore it is an element," we should be committing a fallacy by using the middle term metal in two different senses, in one of which it means the pure simple substances known to chemists as metals, and in the other a ixture of metals commonly called metal in the arts, but known to che ists by the name alloy. many examples which may be found in logical books the ambiguity of the middle term is exceedingly obvious, but the reader should always be prepared to meet with cases where exceedingly subtle and difficult cases of ambiguity occur. Thus it might be argued that "what is right should be enforced by law, and that charity is right and should therefore be enforced by the law." Here it is evident that right is applied in one case to what the conscience approves, and in another case to what public opinion holds to be necessary for the good of society.

The fourth rule forbids us to distribute a term in the conclusion unless it was distributed in the premises. As the sole object of the syllogism is to prove the conclusion by the pre ises, it is obvious that we must not make a statement concerning anything unless that thing was mentioned in the pre ises, in a way warranting the statement. Thus if we were to argue that "because any nations are capable of self-govern ent and that nations capable of self-govern ent should not receive laws from a despotic government," we should be clearly exceedin the contents of our premises. The inor te, many nations, was particular in the inor premise, and must not be ade universal in the conclusion. The pre-

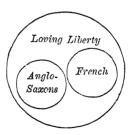
ises do not warrant a statement concerning anything but the *many nations* capable of self-government. The above arguent would therefore be fallacious and would be technically called an cit process of the inor te, eaning that we have i properly treated the inor te.

132 THE RULES OF THE SYLLOGISM. [LESS.

Such a breach of the fourth rule as is described above is exceedingly easy to detect, and is therefore very seldo co itted.

But an cit process or improper treatment of the ajor term is ore common because it is not so transparently false. If we argued indeed that "because all Anglo-Saxons love liberty, and French en are not Anglo-Saxons, therefore they do not love liberty," the fallacy would be pretty apparent; but without a knowledge of logic it would not be easy to give a clear expl ation of the fallacy. It is apparent that the major ter loving liberty, is undistributed in the ajor premise, so that Anglo-S ons must be assu ed to be only a part of those who love liberty. Hence the exclusion of Frenchmen from the class Anglo-Saxons does not necessarily exclude them from the class who love liberty (see Fi . 8). The

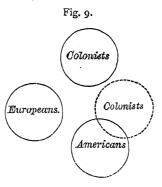
Fig. 8.



conclusion of the false argument being negative distributes its predicate, the major ter, and as this is undistributed in the major pre ise we have a subscript call this fallacy. The followin is an obscurer example of the solution of the subscript of the subscr

are capable of excelling in many branches of knowledge, and such as can so excel are deserving of high comendation;" hence "few students are deserving of high comendation." The little word "few" has here the double meaning before explained (p. 67), and means that "a few are, &c., and the rest are not." The conclusion is thus really a negative proposition, and distributes the major term "deserving of high commendation." But this ajor term is clearly undistributed in the ajor premise, which erely asserts that those who can excel in any branches of knowledge are deserving, but says or implies nothing about other students.

The fifth rule is evidently founded on the principle noticed in the last lesson, that inference can only proceed where there is agreement, and that two differences or disagreements allow of no reasoning. Two ter s, as the third Canon states, may both differ from a com on ter and yet may or may not differ from each other. Thus if



we were to argue that Americans are not Europeans, and Virginians are not Europeans, we see that both terms disagree with the iddle ter Europeans, and yet they agree between themselves. In other cases the two negative premises may be plainly true while it will be quite uncertain whether the major and minor terms agree or not. Thus it is true, for inst ce, that "Colonists e not Europeans, and Americans are not Europeans," but this gives us no right to infer that Colonists e or are not Americans. The two negative premises are represented in fig. 9, by excluding the circles of Colonists and Americans fro that of Europe s; but this exclusion may still be effected whether Colonists and Americ s coincide partially, or wholly, or not at all. A breach of this rule of the syllogism may be conveniently called the fallacy of negative premises. It must not however be supposed that the mere occurrence of a negative particle (not or no) in a proposition renders it negative in the manner contemplated by this rule. Thus the argument

"What is not compound is element. Gold is not compound; Therefore Gold is an ele ent."

contains negatives in both pre ises, but is nevertheless valid, because the negative in both cases affects the middle term, which is really the negative term not-compound.

The truth of the sixth rule depends upon that of the iom, that if two terms agree with a common third term they agree with each other, whence, remembering that a negative proposition asserts disagreement, it is evident that a negative conclusion could not be drawn from really affi ative premises. The corresponding negative axiom prevents our drawing a rmative conclusion if either pre ise should be really negative. Only practice however 'll enable the student to apply this and the preceding rules of the syllogism with certainty, since fallacy ay be hidden and disguised by various for s of expression. Nu erous exa ples are given at the end of

the book by which the student may acquire facility in the analysis of arguments.

The re aining rules of the syllogism, the 7th and 8th, e by no eans of a self-evident character and are in fact corollaries of the first six rules, that is consequences which follow from them. We shall therefore have to shew that they are true consequences in a future Lesson. We ay call a breach of the 7th rule a fallacy of particular pre ises, and that of the 8th rule the fallacy of a universal conclusion from a particular premise, but these fallacies may really be resolved into those of Illicit Process, or Undistributed Middle.

For many details concerning the Aristotelian and Scholastic Views of the Syllogism, and of Formal Logic enerally, see the copious critical notes to Mansel's edition of Aldrich's Artis Logica Rudimenta. 2nd Ed. Oxford. 1852.

LESSON XVI.

THE MOODS AND FIGURES OF THE SYLLOGISM.

WE are now in full possession of those principles of reasoning, and the rules founded upon them, by which a true syllogis may be known from one which only see s to be a true one, and our task in the present Lesson is to ascertain the various shapes or fashions in which a process of mediate inference or syllogism may be et with. We know that every syllogistic argument must contain three propositions and three distinct terms each occurring twice in those propositions. Each proposition

of the syllogis may, so far as we yet know, be either affirmative or negative, universal or particular, so that it is not difficult to calculate the utmost possible varieties of

odes in which a syllogism might conceivably be constructed. Any one of the four propositions A, E, I, or 0 ay in short be taken as a ajor premise, and joined with any one of the sa e four as a minor pre ise, and any one of the four again may be added as conclusion. We should thus obtain a series of the combinations or modes of joining the letters A, E, I, O, a few of which are here written out:

AAA	AEA	AÏA	AOA	EAA	A
AAE		AI	AO		
AAI	I	AII	AOI	AI	I
A.A.	0	AIO	A00	0	c.

It is obvious that there will be altogether $4 \times 4 \times 4$ or 64 such combinations, of which 23 only are given above. The student can easily write out the remainder by carrying on the same systematic changes of the letters. Thus beginning with AAA we change the right-hand letter successively into , I, and O, and then do the same beginning with instead; after the iddle letter has been carried through all its changes we begin to change the left-hand letter. With each change of this we have to repeat all the sixteen changes of the other letters, so that there will obviously be altogether 64 different conceivable modes of arrangin propositions into syllogisms.

We call each of these triplets of propositions a ood or fo of the syllogism (Latin *modus*, shape), and we have to consider how y of such forms can really be used in valid arguents, distinguished fro those which break one or ore of the rules of the syllogism. Thus the ood

would break the 6th rule, that if one premise be ne ative the conclusion must be so too; A breaks the converse part of the same rule, that a negative conclusion can only be proved by a negative pre ise; hile EEA,

&c., break the 5th rule, which prohibits our re onin at all from two negative premises. Examples of y of these moods can easily be invented, and their falsity would be very apparent; thus for AEA we might take

All Austrians are Europeans, No Australians are Europeans;

Therefore, all Australi s are Austrians.

Many of the 64 conceivable moods are excluded by the 7th and 8th rules of the syllogis. Thus AIA and break the rule, that if one premise be particular the conclusion ust be so also, while IIA, 100, 010 d y others, break the rule against two particular pre ises. Some combinations of propositions ay break ore than one le; thus 000 h both negative premises and particular premises, and 00A also violates as well the 6th rule. It is an admirable exercise in the use of the syllogistic rules to write out all the 64 co binations and then strike out such as break any rule; the task if pursued systematically will not be so long or tedious might seem likely. It will be found that there e only twelve moods which escape exclusion, and ay so f: be considered good forms of reasoning, d these are

Of these however 0 will have shortly to be rejected, because it will be found really to break the 4th rule, d involves Illicit process of the ajor term. There are,

then, only eleven oods of the syllogis which e really d we may thus account for the whole of the sixty-four moods.

Nur	
Excluded by of mo	ods.
Negative premises, Rule 5	5
P ticular pre ises " 7	2
One negative premise, 6	2
One premise particular,, 8	
Negative conclusion , 6	4
Illicit ajor, 4	I.
Total excluded 5;	3
Valid oods 1	I
Total	<u>+</u>

We have by no means exhausted as yet all the possible varietics of the syllogism, for we have only determined the character, affirmative or negative, general or particular of the propositions, but have not decided the ways in which the terms may be disposed in them. The major term must be the predicate of the conclusion, but it may either be subject or predicate of the major premise, and simil ly the minor term or subject of the concl ion. ay be either the subject or predicate of the minor pre ise. There thus ise four different ways, or they e called gures, in which the terms can be

disposed. These four figures of the syllogism are shewn in the following scheme, taking

X to	denote	e the major	ter		
Y .		'dd'	le "		
Z		mino	r ,,		
IS	t Fig.	2nd Fig.	3rd Fig.	4th Fig.	
ajor Pre ise	YX	X Y	YX	XY	
Minor "	ZY	ZY	YZ	YZ	
Conclusion			7 X	ZX	

These figures must be carefully committed to memory, which will best be done by noting the position of the middle term. This term stands first as subject of the major premise in the 1st Figure, second as predicate in both pre ises of the 2nd Figure, first again as subject of both premises in the 3rd Figure, and in an intermediate position in the 4th Figure. In the conclusion, of course, the major and inor terms have one fixed position, d when the 'ddle term is once correctly placed in any figure we easily complete the syllogis.

The reader will hardly be pleased to hear that each of the eleven valid oods will have to be exa ined in each of the four figures separately, so that there are 44 c es still possible, fro which the valid syllogisms have to be selected. Thus the mood in the first figure would be

as follows:

All Y's are X's, No Z's are Y's; No Z's are X's.

Therefore No Z's are X's.

This would break the 4th rule and be an Illicit Major, because X is distributed in the conclusion, which is a negative proposition, and not in the ajor pre 'se. In the second figure it would be valid:

All X's are Y's, No Z's are Y's; No Z's are X's.

In the third figure it becomes

Therefore

All Y's are X's, No Y's are Z's, No Z's are X's,

and again breaks the 4th rule, regards the major term. Lastly in the 4th figure it is valid, as the reader may easily satisfy himself.

When all the valid oods are selected out of the 44 possible ones, there are found to be altogether 24, which are as follows:

Valid Moods of the Syllogis .

First	Second	Third	Fourth
Figure.	Figure.	Figure.	Figure.
AAA		AAI	AAI
	E	IAI	
AII	EIO	AII	IAI
IO	A00	AO	EAO
		OAO	EIO
AAI	EAO	EIO	
[o]	[o]		[]

Five of the above moods are set apart and enclosed in brackets, because though valid they are of little or no use. They are said to have a weakened conclusion, because the conclusion is particular when a general one might have been drawn. Thus AAI, in the first figure is represented by the exa ple:

All material substances gravitate, All metals are material substances; Therefore some metals gravitate.

It is apparent that the conclusion only states a part of the truth, and that in reality all etals gravitate. It is not actually erroneous conclusion, because it must be carefully re embered (p. 77) that the affirmin of a subaltern or particular proposition does not deny the corresponding general proposition. It is quite true that so e tals gravitate, and it ust be true bec se all of them do so. But when we can as readily prove that all do gravitate it is desirable to adopt this conclusion.

If we agree with most logicians to overlook the existence of the five syllogisms with weakened conclusions,

there will remain nineteen which are at once valid and useful. In the next lesson certain ancient emonic lines will be furnished by which alone it would be possible for ost persons to carry in the emory these 19 combinations; but the reader will in the mean ti e be able to gather fro the state ent of the moods in p. 140 the truth of the following remarks concerning the peculiar character of each figure of the syllogism.

The first figure is the only one which proves the proposition A, or has A for its conclusion. It is the only figure, too, which can prove any one of the four propositions A, , I, O. As regards the premises, it is especially i portant to note that the ajor premise is always universal (A or), and the minor premise affirmative (A or I): this peculiarity will be further considered in the next lesson.

The second figure only proves negative conclusions (or 0), and the re on is easily apparent. As the middle term in this figure is the predicate of both premises it would necessarily be undistributed in both pre ises if these were affirmatives, and we should commit the fallacy exe plified in p. 137. It follows that one pre ise must be negative and of course one only, so that of the major and inor terms one must be included or excluded wholly fro the iddle, d the other at the s e time excluded or included at least partially. To illustrate this we ay take X, Y and Z to represent, as before, the major, middle and minor terms of a syllogism, and the four oods of this figure are then

.Δ

no X's are Y's, all Z's are Y's; ∴ no Z's are X's. A F

all X's are Y's, no Z's are Y's; ∴ no Z's are X's. 10

no X's are Y's, some Z's are Y's; ∴ some Z's are not X's. A00

all X's are Y's, so e Z's are not Y's; \therefore some Z's are not X's.

The nature of the moods of the second figure is clearly shewn in the following figures:

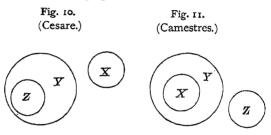
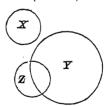


Fig. 12. (Festino.)



It will also be observed that in the second figure the inor premise ay be any of the four A, E, I, O.

The third figure only proves p ticulars (I or 0), and it always h an affirmative inor pre ise (A or I). It also contains the greatest number of oods, since in no case is the conclusion a weakened one.

The fourth figure is usually considered unnatural and comparatively useless, because the same arguments can be more clearly arranged in the form of the first figure, which in some respects it resembles. Thus it proves all the propositions except A, namely, , I, O, d its first mood AAI, is in reality a weakened form of AAA in the first figure. Many logicians, including in recent times Sir W. Hamilton, have rejected the use of this figure altogether.

It is evident that the several figures of the syllogism possess different characters, and logicians have thou ht that each figure w best suited for certain special purposes. A Ge an logician, L bert, stated these purposes concisely as follows:—"The first figure is suited to the discovery or proof of the properties of a th'g; the second to the discovery or proof of the distinctio between things; the third to the discovery or proof of instances dexceptions; the fourth to the discovery, or exclusion, of the different species of genus."

It ay be added that the oods Cesare and C estress are often used disproving a statement, because they give a universal negative conclusion, founded upon the exclusion of one class fro other. Thus if any one were still to assert that light consists of aterial particles it might be met by the follow syllogis:

"Material particles communicate impetus to whatever they strike, Light does not communicate impetus to whatever it strikes;
Therefore light is not material particles."

The oods Baroko and Festino are less used, but allow of a particular conclusion being established.

When we wish however to establish objections or

exceptions to a general statement, which is indeed the natural way of eeting it, we employ the third figure. The state ent that "all metals are solids" would at once be disproved by the exception *mercury*, as follows:

Mercury is not solid, Mercury is a metal; Therefore some metal is not solid.

Were any one to assert that what is incomprehensible c not exist, we meet it at once with the argument that Infinity is incomprehensible, but that infinity certainly exists, because we cannot otherwise explain the nature of a curve line, or of a quantity varying continuously; therefore something that is incomprehensible exists. In this case even one exception is sufficient entirely to negative the proposition, which really means that because a thing is inco prehensible it cannot exist. But if one incomprehensible thing does exist, others may also; and all authority is taken from the statement.

According to the Aristotelian system the third figure ust also be e ployed whenever the middle term is a singular term, because in Aristotle's view of the subject a singular term could not stand as the predicate of a proposition.

LESSON XVII.

REDUCTION OF THE IMPERFECT FIGURES OF THE SYLLOGISM.

In order to facilitate the recollection of the nineteen valid d useful oods of the syllogis, logicians invented, at least s' centuries ago, a ost curious system of artificial words, co bined into e o c ve es, which may be

readily committed to memory. This device, however 'genious, is of a barbarous and wholly unscientific character; but a knowledge of its construction and use is still expected from the student of logic, and the verses are therefore given and explained below.

Barbara, Celarent, Darii, Ferioque, prioris; Cesare, Camestres, Festino, Baroko, secund; Tertia, Darapti, Disamis, Datisi, Felapton, Bokardo, Ferison, habet; Quarta insuper addit Bramantip, Camenes, Dimaris, Fesapo, Fresison.

The words printed in ordinary type are real Latin words, signifying that four moods whose artificial names are Barbara, Celarent, Darii and Ferio, belong to the first figure; that four others belong to the second; six more to the third; while the fourth figure moreover contains five moods. Each artificial name contains three vowels, which indicate the propositions forming a valid mood; thus, Celarent signifies the mood of the first figure, which has E for a major premise, A for the minor, and E for the conclusion. The artificial words altogether contain exactly the series of combinations of vowels shown in p. 140, excepting those in brackets.

These mnemonic lines also contain indications of the mode in which each mood of the second, third and fourth figures can be proved by reduction to a corresponding mood of the first figure. Aristotle looked upon the first figure as a peculiarly evident and cogent form of argument, the *Dictum de omni et nullo* being directly applicable to it, and he therefore called it the Perfect Figure. The fourth figure was never recognised by him, and it is often called the Galeni figure, because the celebrated Galen is supposed to have discovered it. The second

d third figures were known to Aristotle as the Imperfect
Figures, which it was necessary to reduce to the first

figure by cert 'n conversions d transpositions of the premises, for which directions e to be found in the artificial words. These directions are as follows:—

s indicates that the proposition denoted by the pre-

ceding vowel is to be converted si ply.

p indicates that the proposition is to be converted per

accidens, or by limitation.

indicates that the premises of the syllogism are to be tr sposed, the major being ade the inor of a new syllogis, and the old minor the new major. The is derived fro the Latin *mutare*, to change.

B, C, D, F, the initial consonants of the na es, indicate the moods of the first figure, which are produced by reduction; thus Cesare, Camestres and Camenes are reducible to Celarent, Darapti, &c., to Darii, Fresison to Ferio d so on.

k denotes that the mood must be reduced or proved by a distinct process called **Indirect reduction**, or *reductio* ad i possibile, which will shortly be considered.

Let us now take some syllogism, say in *Ca stres*, and follow the directions for reduction. Let the exa ple be

The first s in Camestres shows that we e to convert si ply the minor premise. The m instructs us to change the order of the pre ises, and the final s to convert the conclusion simply. When all these chan es e made we obtain

This, it will be found, is a syllogism in Celarent, as might be known fro the initial C in Camestres.

As another exa ple let us take Fesapo, for instance:

No fixed stars are plets, All plets are round bodies;

Therefore so e round bodies are not fixed stars.

According to the directions in the na e, we e to convert simply the ajor pre ise, and by li itation the inor premise. We have then the followin syllogis in Ferio:

No planets are fixed stars, Some round bodies are planets;

Therefore some round bodies are not fixed stars.

The reader will easily apply the sa e process of conversion or tr sposition to the other moods, according to the directions contained in their na es, defined the only oods it will be necessary to examine especially are Bramantip, Baroko and Bokardo. As an example of Bramantip we may take:

All metals are material substances, All material substances are gravitating bodies; Therefore some gravitating bodies are metals.

The name contains the letter m, which instructs us to transpose the premises, and the letter p, which denotes conversion by limitation; effecting these changes we have:

All material substances are gravitating bodies, All metals are material substances; Therefore some etals are gravitatin bodies.

This is not a syllogism in arbara, as we might have expected, but is the weakened ood AAI of the first figure. It is evident that the precises yield the conclusion "all metals are gravitating bodies," and we must take the letter p to indicate in this ood that the conclusion is weaker than it ight be. In truth the fourth figure is so

imperfect and unnatural in form, containing ill-arranged syllogisms, which would have stated in the first figure, that Aristotle, th logical science, never allowed the existence at all. It is to be regretted that so needless was made to the somewhat complicated syllogism.

The two peculiar moods called Baroko give a good deal of trouble, because they c duced directly to the first figure. To show treating these moods we will take X, Y, Z to major, middle and minor terms of the sy Baroko may then be stated as follows:

All X's are Y's, Some Z's are not Y's; Therefore Some Z's are not X's.

Now if we convert the major premise 1 sition (p. 83) we have "all not-Y's are no making this the major premise of the syllogis

All not-Y's are not X's, Some Z's are not-Y's; Therefore Some Z's are not X's.

Although both the above premises appearitive, this is really a valid syllogism in Feitwo of the negative particles merely affecterm (see p. 134), and we have therefore eff duction of the syllogism.

Bokardo, when similarly stated, is as foll

Some Y's are not X's, All Y's are Z's; So e Z's are not X's.

Therefore

To reduce this, convert the ajor premise by negation, d then transpose the premises. We have:

All Y's are Z's, So e not-X's are Y's:

So e not-X's are Y's; Therefore So e not-X's are Z's.

This conclusion is the converse by negation of the former conclusion, the truth of which is thus proved by reduction to a syllogis in Darii.

Both these oods, Baroko and Bokardo, may however be proved by a peculiar process of indirect reduction, closely analogous to the indirect proofs often employed by Euclid in Geometry. This process consists in supposing the conclusion of the syllogis to be false, and its contradictory therefore true, when a new syllogism can easily be constructed which leads to a conclusion contradictory of one of the original premises. Now it is absurd in logic to call in question the truth of our own premises, for the very purpose of argument or syllogism is to deduce a conclusion which will be true when the premises are true. The syllogis enables us to restate in a new form the information which is contained in the pre ises, just as a machine may deliver to us in a new form the material which is put into it. The achine, or rather the of the machine, is not responsible for the quality of the materials furnished to it, d si ilarly the logician is not responsible in the least for the truth of his premises, but only for their correct treat ent. He must treat them, if he treat them at all, as true; and therefore a conclusion which requires the falsity of one of our premises is altoether absurd.

To apply this method we may take Baroko, as before:

All X's are Y's(1)

So e Z's are not Y's(2)

Therefore So e Z's are not X's (3)

If this conclusion be not true then its contradictory, 'all Z's e X's' ust of necessity be re ded as true (pp. 76—79). Making this the nor pre se of a new syllogism with the original major premise we have:

All X's are Y's(1)
All Z's are X'scontradictory of (3)

Hence All Z's are Y's.

Now this conclusion in A, is the contradictory of our old inor premise in O, and we must either admit one of our o pre ses to be false or allow that our original conclusion is true. The latter is of course the alternative we choose.

We treat Bokardo in a very si ilar anner;

Some Y's are not X's.....(1)
All Y's are Z's.....(2)
perefore
Some Z's are not X's.....(3)

Therefore

If this conclusion be not true then 'all Z's are X's' must be true. Now we can ake the syllogism:

Hence All Y's e X's.

This conclusion is the contradictory of (1), the original ajor pre ise, and as this cannot be allowed, we must either suppose (2) the original minor pre ise to be false, which is equally impossible, or allow that our original conclusion is true.

It will be observed that in both these cases of Indirect Reduction or Proof we use a syllogis in Barb a, which fact is indicated by the initial letters of Baroko and Bokardo. The sa e process of Indirect proof may be applied to y of the other cods, but it is not usual to do so, the si pler process of direct or it is often called ostensive reduction is sufficient.

It will be re embered that when in Lesson XV. (p. 135) we considered the rules of the syllogis , there were two supplementary rules, the 7th and 8th, concernin particular premises, which were by no eans of a self-evident character, and which require to be proved by the six ore fundamental rules. We have now sufficiently advanced to consider this proof with adv tage. The 7th rule forbids us to draw any conclusion fro two particular premises; now such pre ises must be either , IO, OI, or OO. Of these contain no distributed term at all, so that the 3rd le, which requires the middle term to be distributed, must be broken. The premises 00 evidently break the 5th rule, against negative pre ises. The conclusion of the pair 10 must be negative by the 6th rule, because one pre ise is negative; the ajor term therefore will be distributed, but as the major pre ise is a particul affirmative it c not be distributed without committin the fallacy of illicit process of the ajor, against rule 4. Lastly the premises of contain only one distributed te, the predicate of the major pre ise. But as the conclusion ust be ne ative by rule 6th, the ajor term must be distributed: we ought to have then in the pre distributed terms, one for the iddle term, the other for the major term; but the pre ises contain only a single distributed term, we ust commit the fallacy either of undistributed middle or of illicit process of the ter, if we attempt to draw any conclusion at all. We thus see that in no possible case can a pair of particul premises give a valid conclusion.

The 8th rule of the syllogism instructs us that if one premise of a syllogis be particular the conclusion t also be particul. It can only be sho to be t e by oing over all the possible cases and observing that the six principal rules of the syllogis always require the conclusion to be particul. Suppose for inst ce the

premises are A and I; then they contain only one distributed term, the subject of A, and this is required for the middle term by rule 3. Hence the minor term cannot be distributed without breaking rule 4, so that the conclusion must be the proposition I. The premises AO would contain two distributed terms, the subject of A and the predicate of O; but if we were to draw from the the conclusion, the major and minor terms would require to be distributed, so that the middle term would remain undistributed against rule 3. The reader can easily prove the other cases such as by calculating the number of distributed terms in a si ilar anner: it will always be found that there are insufficient terms distributed in the premises to allow of a universal conclusion.

LESSON XVIII.

IRREGULAR AND COMPOUND SYLLOGISMS.

IT ay seem surprising that arguents which are et with in books or conversation are seldo or never thrown to the for of regular syllogisms. Even if a complete syllogism be sometimes met with, it is generally employed in mere affectation of logical precision. In former centuries it was, indeed, the practice for all students at the Universities to take part in public disputations, during which elaborate syllogistic arguments were put forward by one side and confuted by precise syllogisms on the other side. This practice has not been very long discontinued at the University of Oxford, and is said to be still aintained in so e continental Universities; but except in such school disputations it ust be allowed that perfectly formal syllogis s are seldom e ployed.

In truth, however, it is not syllogistic arguments which are wanting; wherever any one of the conjunctions. therefore, because, for, since, hence, inasmuch as, consequently occurs, it is certain that an inference is being drawn, and this will very probably be done by a t e syllogism. It is merely the co plete state ent of the premises and conclusion, which is usually neglected because the reader is enerally aware of one or other of the premises, or he can readily divine what is assumed; it is tedious and even offensive to state at full length what the reader is already aware of. Thus, if I say "atmospheric air ust have wei ht because it is a aterial substance," I certainly e ploy a syllogis; but I think it quite needless to state the premise, of which I clearly assume the t th, that "whatever is a material substance has weight." The conclusion of the syllogis is the first proposition, viz. "atmospheric air has weight." The middle te is " aterial substance." which does not occur in the conclusion; the minor is "atmospheric air," d the major, "having weight." The complete syllogis is evidently:

> All aterial substances have weight, Atmospheric air is a material substance; Therefore atmospheric air h weight.

This is in the very com on and useful mood Barbara.

A syllogism when incompletely stated is usually called an enthyme e, and this n e is often supposed to be derived from two Greek words ($i\nu$, in, and $\theta\nu\mu\dot{\rho}s$, ind), so as to signify that some knowledge is held by the ind and is supplied in the form of a tacit, that is a silent or understood premise. Most commonly this will be the major premise, and then the enthymeme may be said to be of the First Order. Less commonly the minor premise is unexpressed, and the enthy e e is of the Second

Order. Of this nature is the following argument: "Co ets must be subject to the law of gravitation; for this is true of all bodies which move in elliptic orbits." It is so clearly implied that comets move in elliptic orbits, that it would be tedious to state this as the inor premise in a co plete syllogism of the ood Barbara, thus:

All bodies oving in elliptic orbits are subject to the law of gravitation;

Comets ove in elliptic orbits;

Therefore comets are subject to the law of gravitation.

It ay happen occasionally that the conclusion of a syllo is is left unexpressed, and the enthy e e may then be said to belong to the Third Order. This occurs in the case of epigrams or other witty sayings, of which the very wit often consists in aking an unexpressed truth apparent. Sir W. Hamilton gives as an instance of this kind of enthymeme the celebrated epigram written by Porson the English scholar upon a contemporary Ger an scholar:

"The Ger ans in Greek
Are sadly to seek;
Not five in five score,
But ninety-five more;
All, save only Hermann,
And Hermann's a German."

It is evident that while pretending to make an exception of He ann, the writer ingeniously insinuates that since he is a German he has not a correct knowledge of Greek. The wonderful speech of Antony over the body of Cæsar, in Shakspe e's greatest historical play, contains a series of syllogistic arguments of which the conclusions are suggested only.

Even a single proposition may have a syllogistic force if it clearly sug est to the ind a second premise which

thus enables a conclusion to be dra . The expression of Horne Tooke, "Men who have no rights cannot justly complain of any wrongs," see s to be a c e in point; for there are few people who have not felt wronged at some ti e or other, and they would therefore be likely to argue, whether upon true or false premises, as follows:

Men who have no rights cannot justly complain of any wrongs;

We c justly co plain;

Therefore we are not men who have no rights.

In other words, we have rights.

Syllogisms ay be variously joined and combined together, and it is convenient to have special na es for the several parts of a complex argu ent. Thus a syllogis which proves or furnishes a reason for one of the premises of other syllogism is called a Prosyllogis; and a syllogis which contains a premise the conclusion of another syllogism is called an pisyllogism.

Take the example:

All B's are A's, And all C's are B's; Therefore all C's are A's. But all D's are C's;

Therefore

All D's are A's.

This evidently contains two syllogisms in the ood Barbara, the first of which is a Prosyllogism with respect to the second, while the second is an Episyllogism with respect to the first.

The peculiar na e Epicheire is given to a syllogism when either premise proved or supported by a re on implying the existence of an imperfectly expressed pro-

syllogism; thus the form,

All B's e A's, for they are P's, And all C's are B's, for they are Q's; Therefore all C's are A's,

is a double Epicheire a, containing reasons for both premises. The reader will readily decompose it into three complete syllogis s of the mood Barbara.

A ore interesting form of reasoning is found in the chain of syllogisms co monly called the Sorites, from the Greek word $\sigma\omega\rho\delta$ s, meaning heap. It is usually stated in this way:

All A's are B's, All B's are C's, All C's are D's, All D's are E's;

Therefore all A's are E's.

The chain can be carried on to any length provided it is perfectly consecutive, so that each term except the first and last occurs twice, once as subject and once as predicate. It hardly needs to be pointed out that the sorites really contains a series of syllogis s imperfectly expressed; thus

First Syllogism. Second Syllogis . Last Syllogism. B's are C's, C's are D's, D's are E's, A's are C's; A's are C's; A's are C's. A's are C's. A's are E's.

Each syllogis furnishes a premise to the succeeding one, of which it is therefore the prosyllogism, and any syllogis ay equally be considered the episyllogism of that which precedes.

In the above sorites all the premises were universal and afficative, but a sorites may contain one particular premise provided it be the first, and one negative premise provided it be the last. The reader ay easily sure his self by trial, that if any premise except the first were

particular the fallacy of undistributed iddle would be committed, because one of the iddle terms would be the predicate of one affirmative premise and the subject of another particular premise. If any premise but the 1 t were negative there would be a fallacy of illicit process of the ajor term.

It is not to be supposed that the forms of the syllogis hitherto described are all the kinds of reasoning actually employed in science or common life. In addition to the hypothetical and disjunctive syllogisms and some other forms to be described in succeeding lessons, there are really many odes of reasoning of which logicians have not taken much notice as yet. This was clearly pointed out more than two hundred years ago by the writers of the Port Royal Logic, a work first printed in the year 1662. but which has been since reprinted very often and translated into a great many languages. The book is n from a place near Paris where a small religious co munity lived, of which the authors of the book, na elv Arnauld and Nicole, and a contributor to it the great philosopher and mathematician Pascal, were the ost celebrated members. The Port Royal Logic was to a considerable extent the basis of the well-known Watts' Logic, but the reader can now be referred to admirable translation of the original work made by Professor Spencer Baynes, of St Andrew's.

Many improvements of Logic ay be found in this work, such as the doctrine of Extension and Intension explained in Lesson v. In the 9th Chapter of the 3rd P t moreover it is wisely pointed out that "little pains are taken in applying the rules of the syllogis to reasonings of which the propositions are complex, though this is often very difficult, d there e any argu ents of this nature which appear bad, but which e nevertheless very good; and besides, the use of such reaso in s is

uch ore frequent than that of syllogis s which are quite si ple." Some examples are given of the complex syllogisms here referred to; thus:

The sun is a thing insensible, The Persians worship the sun;

Therefore the Persians worship a thing insensible.

This is an gument which cannot be proved by the rules of the syllogism, and yet it is not only evidently true, but is an exceedingly co on kind of argument. Another exa ple is as follows:

The Divine Law com ands us to honour kings; Louis XIV. is a king;

Therefore the Divine Law commands us to honour Louis XIV.

The reader will also find that argu ents which are really quite valid and syllogistic are expressed in language so that they appear to have four distinct terms and thus to break one of the rules of the syllogism. Thus if I say "Diamonds are combustible, for they are composed of carbon and carbon is combustible," there are four terms employed, namely, diamonds, combustible, composed of carbon, and carbon. But it is easy to alter the construction of the propositions so as to get a si ple syllogis without really altering the sense, and we then have:

What is composed of carbon is combustible; Diamonds are composed of carbon; Therefore diamonds are co bustible.

Examples are given at the end of the book of concise arguents, taken from Bacon's Essays and other writings, which the student cereduce to the syllogistic form by easy alterations; but it should be clearly understood that these changes are of an extra-logical character, and belon ore properly to the science of language.

I may here explain that the syllogis and the sorites can be expressed either in the order of extension or that of intension. In regard to the number of individual thin s the noble metals are part of the etals, and the etals are part of the ele ents; but in regard to intension, that is to say the qualities i plied in the na es, element is part of metal, and metal is part of noble etal. So again in extension the genus of plants Ane one is part of the order Ranunculaceæ, and this is part of the great cl s Exogens; but in intension the character of Exogen is p t of the character of Ranunculace , and this is part of the character of Anemone. Syllogistic reasoning is equally valid and evident in either c e, and we ight represent the two modes in ordinary language as follows:

Extensive Syllogis .

All Ranunculace are Exogens;
The Anemone is one of the Ranunculace;
Therefore the Anemone is an Exogen.

Intensive Syllogis .

All the qualities of Ranunculace are qualities of Ane one;

All the qualities of Exogen are qualities of Ranunculace :

Therefore all the qualities of Exogen e qualities of Anemone.

Any sorites can be similarly represented either in extension or intension.

Conce ing the Aristotelian doctrine of the Enthyme e, see Mansel's Aldrich, App. Note F, and H ilton's Lectures on Logic, Lecture xx. Port Royal Logic, translated by T. Spencer Baynes, 7th ed. Edinbur h.

LESSON XIX.

OF CONDITIONAL ARGUMENTS.

IT will be remembered that when treating of propositions we divided them into two distinct kinds, Categorical Propositions, and Conditional Propositions. The former kind alone has hitherto been considered, and we must now proceed to describe Conditional propositions and the arguents which may be coposed of them.

Logicians have commonly described Conditional propositions as composed of two or more Categorical propositions united by a conjunction. This union may happen in two ways, giving rise to two very different species of conditionals, which we shall call prothetic Propositions and Disj ctive Propositions. The way in which the several kinds of propositions are related will be seen in the following diagram:

 $Propositions \ are \left\{ \begin{aligned} &\text{Categorical.} \\ &\text{Conditional} \end{aligned} \right. \\ \left. \begin{aligned} &\text{Hypothetical.} \\ &\text{Disjunctive.} \end{aligned} \right.$

A conditional proposition may be further described as one which makes a statement under a certain condition or qualification restricting its application. In the hypothetical form this condition is introduced by the conjunction if, or some other word equivalent to it. Thus—

"If iron is impure, it is brittle"

is a hypothetical proposition consisting of two distinct categorical propositions, the first of which, "Iron is impure," is called the Antecedent; the second, "It is brittle," the Consequent. In this case "impurity" is the condition or qualification which limits the application of the predicate brittle to iron. It was asserted by Horne Tooke in his celebrated work *The Diversions of Purley*, that all conjunctions are the re ains or corrupted for s of verbs. This is certainly true in the case of the hypothetical conjunction; for the word if in old English is written gif, or gyf, and is undoubtedly derived from the verb to give. We may actually substitute at present any verb of similar meaning, as for instance—grant, allow, suppose Thus we may say—

"Grant that iron is impure, and it is brittle." Supposing that iron is impure, it is brittle."

The hypothetical proposition ight be employed in guments of various form, but only two of these are of sufficient importance to receive special names. The hypothetical syllogis consists of two premises, called the major and inor, as in the c e of the ordinary syllogis. The ajor premise is hypothetical in form; the minor pre ise is categorical, and according as it is affirmative or negative the argument is said to be a Co t ctive or a st ctive hypothetical syllogis. Thus the form,

If A is B, C is D; But A is B; Therefore C is D,

is a constructive hypothetical syllogism.

It ust be carefully observed that the minor premise affirms the antecedent of the major premise, whence the argument is said to be of the *modus ponens*, or mood which posits or affirms. It is probably one of the most familiar and co mon kinds of arguent. The form,

If A is B, C is D; ut C is not D; Therefo A is not B. represents the corresponding estructive h othetic syllogis, also called the *odus tollens*, or the ood which removes the consequent. It must be carefully observed a ain that it is the consequent, not the antecedent, which is denied.

The only rule which is requisite for testing the validity of such syllogisms embodies what we have observed above; viz. that either the antecedent must be affirmed, or the consequent denied. If either part of this rule be broken, a serious fallacy will be committed. Thus the apparent argument,

If A is B, C is D; But C is D; Therefore A is B,

is really a fallacy which we ay call the fallacy of affirming the consequent, and its fallacious nature is readily understood by reflecting that "A being B" is not stated to be the only condition on which C is D. It may happen that when E is F, or G is H, or under a hundred other circumstances, C is D, so that the ere fact of C be is no sufficient proof that A is B. Thus, if a an's character be avaricious he will refuse to give oney for useful purposes; but it does not follow that every person who refuses to give oney for such purposes is avaricious. any proper reasons or otives leading ay be There hi to refuse: he av have no oney, or he sider the purpose not a useful one, or he ay have ore useful purposes in view.

A corresponding fallacy arises from denying the antecedent, in the form—

> If A is B, C is D; But A is not B; Therefore C is not D.

The error may be explained in the same way; for as "A being B" is not stated to be the only condition of C being D, we may deny this one condition to be true, but it is possible that the consequent may happen to be true for other reasons, of which we know nothing. Thus if a man is not avaricious we cannot conclude that he will be sure to give money whenever asked. Or take the follong example:

"If the study of Logic furnished the mind with a multitude of useful facts like the study of other sciences, it would deserve cultivation; but it does not furnish the mind with a multitude of useful facts; therefore it does not deserve cultivation"

This is evidently a fallacious argument, because the acquiring of a multitude of useful facts is not the only ground on which the study of a science can be recommended. To correct and exercise the powers of judgment and reasoning is the object for which Logic deserves to be cultivated, and the existence of such other purpose is ignored in the above fallacious argument, which evidently involves the denial of the antecedent.

Although it is usual in logical works to describe the hypothetical proposition and syllogis as if they were different in nature from the categorical proposition and syllogism, yet it has long been known that the hypotheticals can be reduced to the categorical form, and brought under the ordinary rules of the syllogism. As a general rule the hypothetical proposition can be readily converted into a universal affirmative proposition (A) of exactly the s e eaning. Thus our instance, "If iron is impure, it is brittle," becomes simply "Impure iron is brittle." In making this alteration in a hypothetical syllogism it will be found necessary to supply a new inor term; thus in the case,

If iron is impure it is brittle; But it is impure; Therefore it is brittle,

we have to substitute for the indefinite pronoun *it*, the *iron in question*, and we obtain a correct categorical syllogis in the mood Barbara:

Impure iron is brittle;

The iron in question is impure iron;

Therefore the iron in question is brittle.

Sometimes the reduction requires a more extensive change of language. For instance,

If the barometer is falling, bad weather is coming;

But the barometer is falling;

Therefore bad weather is co ing,

may be represented in the following for :

The circumstances of the barometer falling are the circumstances of bad weather coming;

But these are the circumstances of the barometer falling;

Therefore these are the circumstances of bad weather coming.

As an instance of the Destructive Hypothetical syllogism we may take:

If Aristotle is right, slavery is a proper form of society; But slavery is not a proper form of society:

Therefore Aristotle is not right.

This becomes as a categorical:

The case of Aristotle being right is the case of slavery being a proper form of society;

But this is not the c e;

Therefore this is not the case of Aristotle being right.

If not reducible by any other form of expression, hypotheticals can always be reduced by the use of the words case of.

It will now be easily made apparent that the fallacy of affirmin the consequent is really a breach of the 3rd rule of the syllogism, leading to an undistributed iddle term. Our example ay be as before:

If a man is avaricious he will refuse money; But he does refuse money; Therefore he is avaricious.

This becomes as a categorical syllogism,

All avaricious en refuse money; But this man refuses money; Therefore this man is avaricious.

This is the mood AAA in the second figure; and the middle term, refusing oney, is undistributed in both premises, so that the argument is entirely fallacious.

Again, the fallacy of denying the antecedent is equivalent to the *illicit process of the major*. Our former example (p. 163) may thus be represented:

"A science which furnishes the mind with a multitude of useful facts deserves cultivation; but Logic is not such a science; therefore Logic does not deserve cultivation."

This apparent syllogism is of the mood E in the first figure, which breaks the fourth rule of the syllogism, because the major term, *deserving cultivation*, is distributed in the negative conclusion, but not in the affirmative ajor premise.

We now pass to the consideration of the disjunctive proposition, which instead of a single predicate has several alternatives united by the disjunctive conjunction or, any one of which ay be affirmed of the subject. "A member of the House of Commons is either a representative of a county, or of a borough, or of a University," is an instance of such a proposition, containing three alternatives; but there may be any nu ber of alternatives fro two upwards.

The j ctive syllogis consists of a disjunctive major premise with a categorical proposition, either affirmative or negative, forming the minor premise. Thus arise two moods, of which the affirmative mood is called by the Latin words odus ponendo tollens (the mood which by affirming denies), and ay be thus stated:

A is either B or C, But A is B; Therefore A is not C.

This form of argument proceeds on the supposition that if one alternative of a disjunctive proposition be held true, the others cannot also be true. Thus "the time of year ust be either spring, sum er, autu n or winter," and if it be spring it cannot be summer, autumn or winter; and so on. But it has been objected by Whately, Mansel, Mill, as well as many earlier logicians, that this does not always hold true. Thus if we say that "a good book is valued either for the usefulness of its contents or the excellence of its style," it does not by any means follow because the contents of a book are useful that its style is not excellent. We generally choose alternatives which are inconsistent with each other; but this is not logically necessary.

The other form of disjunctive syllogism, called the *odus tollendo ponens* (the mood which by denying affir s), is always of necessity cogent, and is as follows:

A is either B or C, But A is not B; Therefore A is C.

Thus if we suppose a book to be valued only for the usefulness of its contents or the excellence of its style, it follows that if a book be valued but not for the former re on it ust be for the latter; and vice versa. If the ti e of ye be not spring, it must be summer, autumn or

winter; if it be not autumn nor winter, it must be either sprin or summer; and so on. In short if any alt atives be denied, the rest remain to be affirmed as before. It will be noticed that the disjunctive syllogism is governed by totally different rules from the ordinary categorical syllogism, since a negative premise gives affirmative conclusion in the former, and a negative conclusion in the latter.

There yet remains a fo of argument called the ile a, because it consists in assuming two alternatives, usually called the horns of the dilemma, and yet proves something in either case (Greek $\delta\iota$ - two; $\lambda\eta\mu\mu$ a, assumption). Mr Mansel defines this argument as "a syllogism, having a conditional major premise with more than one antecedent, and a disjunctive minor." There are at least three forms in which it may be stated. The first form is called the Simple Const. ctive Dile a:

If A is B, C is D; and if E is F, C is D; But either A is B, or E is F; Therefore C is D.

Thus "if a science furnishes useful facts, it is worthy of being cultivated; and if the study of it exercises the reasoning powers, it is worthy of being cultivated; but either a science furnishes useful facts, or its study exercises the reasoning powers; therefore it is worthy of being cultivated."

The second form of dilemma is the Co plex Const ctive ite a, which is as follows:

If A is B, C is D; and if E is F, G is H; But either A is B, or E is F; Therefore either C is D, or G is H.

It is called complex because the conclusion is in the disjunctive form. As an instance we may take the argu-

ment, "If a statesman who sees his former opinions to be wrong does not alter his course he is guilty of deceit; and if he does alter his course he is open to a charge of inconsistency; but either he does not alter his course or he does; therefore he is either guilty of deceit, or he is open to a charge of inconsistency." In this case in the greater number of dilemmas the terms A, B, C, D, &c. are not all different.

The est ctive Dile a is always complex, because it could otherwise be resolved into two unconnected destructive hypothetical syllogisms. It is in the following fo:

If A is B, C is D; and if E is F, G is H; But either C is not D, or G is not H; Therefore either A is not B, or E is not F.

For instance, "If this man were wise, he would not speak irreverently of Scripture in jest; and if he were good, he would not do so in earnest; but he does it either in jest or earnest; therefore he is either not wise, or not good *."

Dilem atic guments are however more often fallacious than not, because it is seldom possible to find instances where two alternatives exhaust all the possible cases, unless indeed one of them be the simple negative of the other in accordance with the law of excluded middle (p. 119). Thus if we were to argue that "if a pupil is fond of learning he needs no stimulus, and that if he dislikes learning no stimulus will be of y avail, but as he is either fond of learning or dislik it, a stimulus is either needless or of no avail," we evidently sume improperly the disjunctive minor pre ise. Fondness and dislike are not the only two possible alternatives, for there may be

some who are neither fond of learnin nor dislike it, and to these a stimulus in the shape of rewards may be desirable. Almost ything can be proved if we are allowed thus to pick out two of the possible alternatives which are in our favour, and argue from these alone.

A dile a can often be retorted by producing cogent a dilem a to the contrary effect. Thus an Atheni mother, according to Aristotle, addressed her son in the following words: "Do not enter into public business; for if you say what is just, men will hate you; and if you say what is unjust, the Gods will hate you." To which Aristotle suggests the following retort: "I ought to enter into public affairs; for if I say what is just, the Gods will love me; and if I say what is unjust, men will love me."

Mansel's Aldrich, App. Note I, on the Hypothetical Syllogism.

LESSON XX.

LOGICAL FALLACIES.

In order to acquire a satisfactory knowledge of the rules of correct thinking, it is essential that we should become acquainted with the most common kinds of fallacy; that is to say, the modes in which, by neglecting the rules of logic, we often fall into erroneous reasoning. In previous lessons we have considered, as it were, how to find the right road; it is our task here to ascertain the turnings at which we are most liable to take the wrong road.

In describing the fallacies I shall follow the order d adopt the mode of classification which has been usual for the last 2000 years and more, since in fact the great

teacher Aristotle first explained the fallacies. According to this mode of arrangement fallacies are divided into two principal groups, containing the logical and the material fallacies.

- I. The logic fallactes are those which occur in the ere fo of the statement; or as it is said in the old Latin expressions, in dictione, or in voce. It is supposed accordingly that fallacies of this kind can be discovered without a knowledge of the subject-matter with which the arguent is concerned.
- 2. The aterial fallacies, on the contrary, arise outside of the mere verbal state ent, or as it is said, extra dictione; they are concerned consequently with the subject of the argument, or in re (in the atter), and cannot be detected and set right but by those acquainted with the subject.

The first roup of logical fallacies may be further divided into the *purely logical* and the *semi-logical*, and we may include in the former class the distinct breaches of the syllogistic rules which have already been described. Thus we ay enumerate as Purely Logical Fallacies:

- I. Fallacy of four terms (Quaternio Terminorum)—reach of Rule I;
 - 2. Fallacy of undistributed middle—Breach of Rule 3;
- Fallacy of illicit process, of the major or minor te —Breach of Rule 4;
- 4. Fallacy of negative premises—Breach of Rule 5; as well as breaches of the 6th rule, to which no distinct na e has been given. Breaches of the 7th and 8th rules ay be resolved into the preceding (p. 151), but they ay also be described as in p. 135.

The other part of the class of logical fallacies contains
-lo fallacies, which are six in number, as follows:

LXX

- 1g .'0
- al
- he old ed
- ed he
- ra .b-
- ith
- we of ed.
- 3; 10r
- nct les ley

ins 75:

- 1. Fallacy of Equivocation.
- Fallacy of Amphibology.
- 3. Fallacy of Composition.
- 4. Fallacy of Division.
- 5. Fallacy of Accent.
- 6. Fallacy of Figure of Speech.

These I shall describe and illustrate in succession.

Equivocation consists in the same term bein used in two dist ct senses; any of the three terms of the syllogism ay be subject to this fallacy, but it is usually the middle term which is used in one sense in one pre ise and in another sense in the other. In this case it is often called the fallacy of ambiguous middle, and when we distinguish the two meanings by using other suitable odes of expression it becomes apparent that the supposed syllogis contains four terms. The fallacy of equivocation

ay accordingly be considered a disguised fallacy of four te s. Thus if a person were to argue that "all criminal actio ought to be punished by law; prosecutions for theft are criminal actions; therefore prosecutions for theft ought to be punished by law," it is quite apparent that the te "criminal action" eans totally different things in the two premises, and that there is no true iddle term at all. Often, however, the ambiguity is of

a subtle and difficult character, so that different opinions may be held concerning it. Thus we might argue:

"He who harms another should be punished. He who communicates an infectious disease to another person harms him. Therefore he who comunicates an infectious disease to another person should be punished."

This may or may not be held to be a correct argument according to the kinds of actions we should consider to co e under the term harm, according as we reg d negligence or malice requisite to constitute harm. Many

difficult legal questions are of this nature, as for instance:

Nuisances are punishable by law; To keep a noisy dog is a nuisance; To keep a noisy dog is punishable by law.

The question here would turn upon the degree of nuisance which the law would interfere to prevent. Or again:

Interference with another man's business is illegal; Underselling interferes with another man's business; Therefore underselling is illegal.

Here the question turns upon the *kind of interference*, and it is obvious that underselling is not the kind of interference referred to in the ajor premise.

The Fallacy of Amphibolo consists in an ambiguous grammatical structure of a sentence, which produces misconception. A celebrated instance occurs in the prophecy of the spirit in Shakspeare's Henry VI.: "The Duke yet lives that Henry shall depose," which leaves it wholly doubtful whether the Duke shall depose Henry, or Henry the Duke. This prophecy is doubtless an imitation of those which the ancient oracle of Delphi is reported to have uttered; and it see s that this fallacy was a great resource to the oracles who were not confident in their own powers of foresight. The Latin language gives great scope to isconstructions, because it does not require any fixed order for the words of a sentence, and when there are two accusative cases with an infinitive verb, it may be difficult to tell except from the context which comes in regard to sense before the verb. The double meaning which may be given to "twice two and three" arises from amphibology; it may be 7 or 10, according as we add the 3 after or before multiplying. In the careless construction of sentences it is often impossible to

tell to what part any adverb or qualifying clause refers. Thus if a person says "I accomplished y business and returned the day after," it may be that the business w accomplished on the day after as well as the return; but it may equally have been finished on the previous day. Any ambiguity of this kind may generally be avoided by a si ple change in the order of the words; as for instance, "I accomplished my business, and, on the day after, returned." Amphibology may sometimes arise from confusing the subjects and predicates in a compound sentence, as if in "platinum and iron are very rare and useful metals" I were to apply the predicate useful to platinum and rare to iron, which is not intended. The word "respectively" is often used to shew that the reader is not at liberty to apply each predicate to each subject.

The Fallacy of Co position is a special case of equivocation, arising from the confusion of an universal and a collective term. In the premises of a syllogism we may affirm something of a class of things distributively, that is, of each and any separately, and then we ay in the conclusion infer the same of the whole put together. Thus we may say that "all the gles of a triangle are less than two right angles," meaning that any of the angles is less than two right angles; but we must not infer that all the put together are less than two right angles. We must not argue that because every member of a jury is very likely to judge erroneously, the jury as a whole are also very likely to judge erroneously; nor that because each of the witnesses in a law case is liable to give false or taken evidence, no confidence can be reposed in the concurrent testi ony of a number of witnesses. It is by a fallacy of Co position that protective duties are still sometimes upheld. Because any one or any few trades which enjoy protective duties are benefited thereby, it is supposed that all trades at once might be benefited similarly; but this is impossible because the protection of one

trade by raising prices injures all others.

The Fallacy of **Division** is the converse of the preceding, and consists in using the middle term collectively in the major premise but distributively in the minor, so that the whole is divided into its parts. Thus it ight be argued, "All the angles of a triangle are (together) equal to two right angles; ABC is an angle of a trian le; therefore ABC is equal to two right angles." Or again, "The inhabitants of the town consist of men, wo en and children of all ages; those who met in the Guildhall were inhabitants of the town; therefore they consisted of men, women and children of all ages;" or, "The judges of the court of appeal cannot misinterpret the law; Lord A.B. is a judge of the court of appeal; therefore he cannot misinterpret the law."

The Fallacy of Accent consists in any ambiguity arising from a misplaced accent or emphasis thrown upon some word of a sentence. A ludicrous instance is liable to occur in reading chapter xiii. of the First Book of Kings, verse 27, where it is said of the prophet "And he spake to his sons, saying, Saddle me the ass. And they saddled hi ." The italics indicate that the word him was supplied by the translators of the authorized version. but it may suggest a very different meaning. The Commandment "Thou shalt not bear false witness against thy neighbour" ay be ade by a slight e phasis of the voice on the last word to i ply that we are at liberty to false witness against other persons. Mr De Morgan who re arks this also points out that the erroneous quoting of an author, by unfairly separating a word from its context or italicising words which were not intended to be italicised, gives rise to cases of this fallacy.

It is curious to observe how many and various may be the eanings attributable to the same sentence according as emphasis is thrown upon one word or another. Thus the sentence "The study of Logic is not supposed to communicate a knowledge of many useful facts," may be ade to imply that the study of Logic does communicate

such a knowledge although it is not supposed to; or that it com unicates a knowledge of a fe useful facts; or that it communicates a knowledge of many useless facts. This ambiguity may be explained by considering that if you deny a thing to have the group of qualities A, B, C, D, the truth of your statement will be satisfied by any one quality being absent, and an accented pronunciation will often be used to indicate that which the speaker believes to be absent. If you deny that a particular fruit is ripe and sweet and well-flavoured, it may be unripe d sweet and well-flavoured; or ripe and sour and well-flavoured; or ripe and sweet and ill-flavoured; or any two or even all three qualities may be absent. But if you deny it to be ripe and sweet and well-flavoured, the denial would be understood to refer to the last quality. Jeremy uch afraid of being misled by this Bentham w SO fallacy of accent that he employed a person to read to I have heard, who had a peculiarly monotonous manner of reading.

The Fallacy of the gure of Speech is the sixth and last of the semi-logical fallacies, and is of a very trifling ch acter. It appears to consist in any gra matical mistake or confusion between one part of speech and other. Aristotle gravely gives the following instance: "Whatever a man walks he tramples on; a man walks the whole day; therefore he tramples on the day." Here an adverbial phre is converted into a noun object.

LESSON XXI.

MATERIAL FALLACIES.

THE Material fallacies are next to be considered; and their importance is very great, although it is not easy to illustrate them by brief examples. There are altogether seven kinds of such fallacies enumerated by Aristotle and adopted by subsequent logicians, as follows:

- 1. The Fallacy of Accident.
- 2. The Converse Fallacy of Accident.
- 3. The Irrelevant Conclusion.
- 4. The Petitio Principii.
- 5. The Fallacy of the Consequent or Non sequitur.
- 6. The False Cause.
- 7. The Fallacy of Many Questions.

Of these the two first are conveniently described together. The fallacy of accident consists in arguing erroneously fro a general rule to a special case, where a certain accidental circumstance renders the rule inapplicable. The converse fallacy consists in arguing fro a special case to a general rule. This latter fallacy is usually described by the Latin phrase a dicto secundum quid ad dictum simpliciter, eaning "from a state ent under a condition to a statement simply or without that condition." Mr De Morgan has remarked in his very interesting Chapter on Fallacies* that we ought to add a third fallacy, which would consist in arguing from one special case to another special c e.

^{*} Formal Logic, Chapt XIII.

I will try by a few exa ples to illustrate these kinds of fallacy, but uch difficulty is often encountered in sayin to which of the three any particular exa ple is best referred. A most ancient e mple repeated in almost every logical hand-book is as follows: "What you bought yesterday you eat to-day; you bought raw eat yesterday; therefore you eat raw eat to-day." The sertion in the conclusion is made of eat with the accidental quality of rawness added, where the first pre ise evidently speaks of the substance of the meat without regard to its accidental condition. This then is a case of the direct fallacy. If it is argued again that because wine acts as a poison when used in excess it is always a poison, we fall into the converse fallacy.

It would be a c e of the direct fallacy of accident to infer that a magistrate is justified in using his power to forward his own religious views, because every man has a right to inculcate his own opinions. Evidently a magistrate as a an has the rights of other men, but in his capacity of a magistrate he is distinguished from en, and he must not infer of his special powers in this respect what is only true of his rights as a man. For another instance take the following: "He who thrusts a knife into another person should be punished; a sur eon in operating does so; therefore he should be punished." Though the fallacy of this is absurdly manifest, it is not so manifest how we are to classify the error. We may for instance say that as a general rule whoever stabs or cuts another is to be punished unless it be shewn to have been done under exceptional circu stances, as by a duly qualified surgeon actin for the good of the person. In this case the example belongs to the direct fallacy of accident. In another view we mi ht interpret the first premise to ean the special c e of thrusting a knife maliciously; to argue from that to the case of a surgeon would be to infer from one special case other special case.

It is undoubtedly true that to give to beggars promotes mendicancy and causes evil; but if we interpret this to mean that assistance is never to be given to those who solicit it, we fall into the converse fallacy of accident, inferring of all who solicit alms what is only true of those who solicit alms as a profession. Similarly it is a very good rule to avoid lawsuits and quarrels, but only as a general rule, since there frequently arise circumstances in which resort to the law is a plain duty. Almost all the difficulties which we meet in matters of law and moral duty arise from the impossibility of always ascertaining exactly to what cases a legal or moral rule does or does not extend: hence the interminable differences

of opinion, even among the judges of the land.

The Third Material Fallacy is that of the Irrelev t Conclusion, technically called the Ignoratio Elenchi, or literally Ignorance of the Refutation. It consists in arguing to the wrong point, or proving one thing in such a manner that it is supposed to be something else that is proved. Here again it would be difficult to adduce concise examples, because the fallacy usually occurs in the course of long harangues, where the multitude of words and figures leaves room for confusion of thought and forgetfulness. This fallacy is in fact the great resource of those who have to support a weak case. It is not unknown in the legal profession, and an attorney for the defendant in a lawsuit is said to have handed to the barrister his brief marked, "No case; abuse the plaintiff's attorney." Whoever thus uses what is known as argumentum ad hominem, that is an argu ent which rests, not upon the merit of the case, but the character or position of those engaged in it, co mits this fallacy. If an is accused of a crime it is no answer to say that

the prosecutor is as bad. If a great change in the law is proposed in Parliament, it is an Irrelevant Conclusion to argue that the proposer is not the right man to bring it forward. Everyone who gives advice lays himself open to the retort that he who preaches ought to practise, or that those who live in glass houses ought not to throw stones. Nevertheless there is no necessary connection between the character of the person giving advice and the goodness of the advice.

The argumentum ad populum is another form of Irrelevant Conclusion, and consists in addressing arguents to a body of people calculated to excite their feelings and prevent them from forming a dispassionate judgment upon the matter in hand. It is the great weapon of rhetoricians and demagogues.

Fetitio cipil is a familiar name, and the nature of the fallacy it denotes is precisely expressed in the phrase begging the question. Another apt name for the fallacy is circulus in probando, or "a circle in the proof." It consists in taking the conclusion itself as one of the premises of an argument. Of course the conclusion of a syllogism must always be contained or implied in the premises, but only when those premises are combined, and are distinctly different assertions from the conclusion. Thus in the syllogism.

 $B ext{ is } C$, $A ext{ is } B$, therefore $A ext{ is } C$.

the conclusion is proved by being deduced from two propositions, neither of which is identical with it; but if the truth of one of these premises itself depends upon the following syllogism,

 $C ext{ is } B,$ $A ext{ is } C,$ therefore $A ext{ is } B,$

it is plain that we attempt to prove a proposition by itself, which is as reasonable as attempting to support a body upon itself. It is not easy to illustrate this kind of fallacy by examples, because it usually occurs in long arguments, and especially in wordy metaphysical writings. We are very likely to fall into it however when we employ a mixture of Saxon and Latin or Greek words, so as to appear to prove one proposition by another which is really the same expressed in different ter s, as in the following: "Consciousness must be immediate cognition of an object; for I cannot be said really to know a thin unless my mind has been affected by the thing itself."

In the use of the disjunctive syllogism this fallacy is likely to happen; for by enu erating only those alternatives which favour one view and forgetting the others it is easy to prove anything. An instance of this occurs in the celebrated sophism by which some of the ancient Greek philosophers proved that motion was impossible. For, said they, a moving body must ove either in the place where it is or the place where it is not; now it is absurd that a body can be where it is not, and if it moves it cannot be in the place where it is; therefore it cannot move at all. The error arises in the assumption of a premise which begs the question; the fact of course is that the body moves between the place where it is at one moment and the place where it is at the next oment.

Jere y Bentham however pointed out that the use even of a single name may imply a Petitio Principii. Thus in a Church assembly or synod, where a discussion is taking place as to whether a certain doctrine should be conde ned, it would be a Petitio Principii to argue that the doctrine is heresy, and therefore it ought to be condemned. To assert that it is heresy is to beg the question, because every one understands by heresy a doctrine which is to be condemned. Similarly in Parliament a

bill is often opposed on the ground that it is unconstitutional and therefore ought to be rejected; but as no precise definition can be given of what is or is not constitutional, it means little more than that the measure is dist teful to the opponent. Names which are used in this fallacious manner were aptly called by Bentham Question-begging Epithets. In like manner we beg the question when we oppose any change by saying that it is un-English.

The Fallacy of the Co equent is better understood by the familiar phrase non sequitur. We may apply this name to y argument which is of so loose and inconsequent a character that no one can discover any cogency it. It thus amounts to little more than the assertion of a conclusion which has no connection with the premises. Prof. De Morgan gives as an example the following: "Episcopacy is of Scripture origin; the Church of England is the only episcopal Church in England; ergo, the Church established is the Church that should be supported."

y the Fallacy of the False Cause I denote that which has generally been referred to by the Latin phr e non causa pro causa. In this fallacy we sume that one thin is the cause of another without any sufficient grounds. A change in the weather is even yet attributed to the new moon or full moon which had occurred shortly before, although it has been de onstrated over and over again that the oon can have no such effect. In former centuries any plague or other public calamity which followed the appearance of a comet or eclipse was considered to be the result of it. The Latin phrase post hoc ergo propter hoc (after this and therefore in consequence of this) exactly describes the character of these fallacious conclusions. Though we no longer dread si ns and o ens. yet we often enough commit the fallacy;

when we assu e that all the prosperity of England is the result of the national character, forgetting that the plentiful coal in the country and its maritime position have contributed to our material wealth. It is no doubt equally fallacious to attribute no importance to national character, and to argue that because England has in past centuries misgoverned Ireland all the present evils of Ireland are due to that misgovernment.

Lastly there is the somewhat trivial Fallacy of uestions, which is co itted by those who so combine two or three questions into one that no true answer can be given to the . I cannot think of a better example than the vulgar pleasantry of asking, "Have you left off beating your mother?" Ouestions equally as unfair are constantly asked by barristers examining witnesses in a court of justice, and no one can properly be required to answer Yes or No to every question which may be addressed to hi . As Aristotle says, "Several questions one should be at once deco posed into their several parts. Only a single question admits of a single answer: so that neither several predicates of one subject, nor one predicate of several subjects, but only one predicate of one subject, ought to be affirmed or denied in a single answer."

Read Prof. de Morgan's excellent and amusin Chapter on Fallacies, *Formal Logic*, Ch. XIII.

Whately's remarks on Fallacies, Elements of Logic, Book III., e often very original and acute.

LESSON XXII.

THE QUANTIFICATION OF THE PREDICATE.

THE syllogis h been explained in the preceding three lessons almost exactly in the form in which it has been taught for more than two thousand ye s. Just as Geometry has been taught in the way and order first adopted by the ancient Greek writer Euclid, so Logic h been taught nearly as Aristotle taught it about the year 335 B.C.

But within the last few years teachers have at 1 t come to the conclusion in England that Euclid's ide of Geometry are not perfect as could be desired. During the last 30 or 40 years also it has been gradually made apparent that Aristotle's syllogis is not an absolutely perfect syste of logical deduction. In fact, certain eminent writers, especially Sir William Hamilton, Professor De Morgan, Archbishop Thomson and Dr Boole, have shewn that we need to make improvements from the very basis of the science.

This reform in Logic is called by the somewhat mysterious name of the qu tification of the pre cate, but the reader who has found no insuperable difficulty in the precedin lessons need not fear one here. To quantify the predicate is simply to state whether the whole or the part only of the predicate agrees with or differs fro

the subject. In this proposition,

[&]quot;All metals are elements,"

the subject is qu tified, but the predicate is not; we know that all etals are elements, but the proposition does not distinctly assert whether metals make the whole of the elements or not. In the quantified proposition

"All metals are some elements,"

the little word some expresses clearly that in reality the etals form only a part of the elements. Aristotle avoided the use of any m k of quantity by assuming, as we have seen, that all affirmative propositions have a particular predicate, like the example just given; and that only ne ative propositions have a distributed or universal predicate. The fact however is that he was entirely in error, and thus excluded fro his system an infinite number of affirmative propositions which are universal in both terms. It is true that—

"All equilateral triangles are all equiangular triangles," but this proposition could not have appeared in his system except in the utilated form—

"All equilateral triangles are equiangular."

Such a proposition as

or

"London is the capital of England,"

"Iron is the cheapest etal,"

had no proper place whatever in his syllogism, since both terms are singular and identical with each other, and both are accordingly universal.

As soon as we allow the quantity of the predicate to be stated the forms of re oning beco e much si plified. We ay first consider the process of conversion. In our lesson on the subject it w necessary to distinguish between conversion by li itation and si ple conversion. But now one single process of ple conversion is sufficient for all kinds of propositions. Thus the quantified proposition of the form A,

"All metals are some elements,"

is simply converted into

"Some elements are all metals."

The particular affirmative proposition

"Some etals are some brittle substances" becomes by mere transposition of terms

"Some brittle substances are some metals."

The particular negative proposition

"Some men are not (any) trustworthy persons" is also converted simply into

"Not any trustworthy persons are some men," though the result may appear less satisfactory in this form than in the affirmative form, as follows,

"Some men are some not-trustworthy persons," converted simply into

"Some not-trustworthy persons are some en."

The universal negative proposition is converted simply as before, and finally we have a new affirmative proposition universal both in subject and predicate; as in

"All equilateral triangles are all equiangular triangles," which may obviously be converted simply into

"All equiangul triangles are all equilateral triangles."

This doubly universal affirmative proposition is of most frequent occurrence; as in the c e of all definitions and singular propositions; I may give as instances "Honesty is the best policy," "The greatest truths are the simplest truths," "Virtue alone is happiness below," "Self-exaltation is the fool's paradise."

When affirmative propositions are expressed in the quantified form all immediate inferences can be readily drawn from them by this one rule, that whatever we do with one term we should do with the other term. Thus from the doubly universal proposition, "Honesty is the best policy," we infer that "what is not the best policy is

not honesty," and also "what is not honesty is not the best policy." From this proposition in fact we can draw two contrapositives; but the reader will carefully remember that fro the ordinary unquantified proposition A we can only draw one contrapositive (see p. 84). Thus if "etals e elements" we must not say that "what e not etals are not ele ents." But if we quantify the predicate thus, "All etals are some elements," we may infer that "what are not metals are not some elements." Immediate inference by added determinant and complex conception can also be applied in either direction to quantified propositions without fear of the errors noticed in pp. 86-7.

It is clear that in admitting the mark of quantity before the predicate we shall double the number of propositions which must be admitted into the syllogism, because the predicate of each of the four propositions A, , I, O may be either universal or particular. Thus we arrive at a list of eight conceivable kinds of propositions, which are stated in the following table.

 \mathbf{U} All X is all Y.

I Some X is some Y. Affirmative

A All X is some Y. propositions

Y Some X is all Y.

No X is (any) Y.

ω Some X is not some Y. \ Negative

 η No X is some Y. propositions

O Some X is no Y.

The letters X and Y are used to stand for any subject and predicate respectively, and the reader by substituting various terms can e ily make propositions of each kind. The sy bolic letters on the left-hand side were proposed by Archbishop Thomson as a convenient mode of refer-

ring to each of the eight propositions, and are very suitably chosen. The doubly universal affirmative proposition is called \mathbf{U} ; the simple converse of \mathbf{A} is called \mathbf{Y} ; the Greek letter $\mathbf{\eta}$ (Eta, $\mathbf{\bar{e}}$) is applied to the proposition obtained by changing the universal predicate of into a particular predicate; d the Greek ω (O ega, \bar{o}) is applied to the proposition similarly determined from 0. All these eight propositions are employed by Sir W. Ha-

ilton, but Archbishop Thomson considers that two of them, η and ω , are never really used. It is remarkable that a complete table of the above eight propositions w given by Mr George Bentham in a work called *Outline* of a New System of Logic, published in 1827, several years previous to the earliest of the logical publications of Sir W. Hamilton. But Mr Bentham considered that some of the propositions are hardly to be distinguished from others; as \forall from Δ , of which it is the simple converse; or η from Ω .

The employment even of the additional two propositions **U** and **Y** introduced by Thomson much extends the list of possible syllogisms, making them altogether 62 in number, without counting the fourth figure, which is not employed by Hamilton and Thomson. When the whole eight propositions are admitted into use we are obliged to extend the list of possible syllogisms so as to contain 12 affirmative and 24 negative moods in each of the three first figures. The whole of these moods are conveniently stated in the table on the next page, given by Archbishop Thomson at p. 188 of his *Laws of Thought*.

Sir W. Hamilton also devised a curious syste of notation for exhibiting all the moods of the syllogis in a clear manner. He always employed the letter M to denote the middle term of the syllogism, and the two letters C and Γ (the Greek capital letter Gamma) for the two terms appearing in the conclusion. The copula of the

Table of Moods of the Syllogis .

	First Figure.		SECOND FIG.		THIRD FIGURE.	
	Affirm.	Neg.	Affirm.	Neg.	Affirm.	Neg.
1	עעע	EUE	עעע	EUE	บบบ	EUE
		UEE		UEE		UEE
ii	AYI	ηΥω	YYI	ОΥω	AAI	ηΑω
		ΑΟω		YΟω		Αηω
iii	AAA	ηΑη	YAA	ΟΑη	AYA	ηΥη
		Αηη		Υηη		ΑΟη
iv	YYY	OYO	AYY	ηΥО	YAY	OAO
		YOO		A00	_	ΥηΟ
v	AII	ηΙω	YII	ΟΙω	AII	ηΙω
		Αωω		Υωω		Αωω
vi	IYI	ωΥω	IYI	ωΥω	IAI	ωΑω
		ΙΟω		ΙΟω		Ιηω
vii	UYY	EYO	UYY	EYO	UAY	EAO
		noo		TOO		UηO
viii	AUA	η U η	YUA	ΟUη	AUA	η U η
		AΕη		YΕη		ΑΕη
ix	UAA	EAE	UAA	EAE	UYA	EYE
		$U\eta\eta$		Uηη		UOη
x	YUY	OUO	AUY	ηUO	YUY	ouo
		YEE		AEE		YEE
хi	UII	EIO	UII	EIO	UII	EIO
		Uωω	-	Uωω		Uωω
xii	IUI	ωυω	IUI	ωUω	IUI	ωυω
	ł	IΕη		IΕη		IΕη

proposition was indicated by a line thickened towards the subject; thus C — M means that "C is M." To indicate the quantity of the tessel Hamilton inserted a

colon (:) between the te d the copula when the quantity is universal, d a comma (,) when the quantity is particular. Thus we readily express the followin affirmative propositions.

<i>C</i> :	, M	All C's are some M's	$(\dot{\mathbf{A}})$
C .	. 7.5	A 11 (C) 11 3(4) -	(TT)

$$C:$$
 : M All C 's are all M 's (U)

C, , M So e C's are some M's (I)

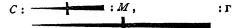
and so on. Any affirmative proposition can be converted to the corresponding negative proposition by drawing a stroke through the line denoting the copula, as in the following—

$$C:$$
 : M No C is any M (E)

Any syllogism can be represented by placin M the 'ddle term in the c ntre and connecting it on each side with the other terms. The copula representing the conclusion can then be placed below; Barbara is expressed as follows—

$$:M$$
, $:\Gamma$

The negative mood Celarent is si il ly-



Cesare in the second figure is thus represented-

$$C:$$
 , $M:$: I

Sir W. Hamilton also proposed a new law or supreme canon of the syllogis by which the validity of all forms of the syllogism might be tested. This was stated in the following words: "What worse relation of subject and predicate subsists between either of two terms and a common third term, with which both are related, and one at least positively so—that relation subsists between these two terms themselves."

By a worse relation, Sir William means that a negative relation is worse than an affirmative and a particular than a universal. This canon thus expresses the rules that if there be a negative premise the conclusion must be negative, and if there be a particular premise the conclusion must be particular. Special canons were also developed for each of the three figures, but in thus rendering the system complex the advantages of the question of proposition seed to be lost.

Prof. De Morgan also discovered the adv tages of the quantified predicate, and invented a system differing greatly from that of Sir W. Ha ilton. It is fully explained in his For al Logic, The Syllabus of a new Syste of Logic, and various important emoirs on the Syllogism in the Transactions of the Cambridge Philosophical Society. In these works is also given a complete explanation of the "Numerically Definite Syllogism." Mr De Morgan pointed out that two particular premises may often give a valid conclusion provided that the actual quantities of the two terms are stated, and when added together exceed the que tity of the iddle term. Thus if the ajority of a public meeting vote for the first resolution, and a majority also vote for the second, it follows necessarily that some who voted for the first voted also for the second. The two majorities added together exceed the whole number of the eeting, so that they could not consist of entirely different people. They indeed consist of exactly the same people; but all that deduce fro the premises is that the excess of the we c

two majorities added together over the number of the meeting ust have voted in favour of each resolution. This kind of inference has by Sir W. Hamilton been said to depend on *ultra-total* distribution; and the n e of Pl attve Propositions has been proposed for all those which give a distinct idea of the fraction or number of the subject involved in the assertion.

T. Spencer Baynes, Essay on the new Analytic of Logical Forms; Edinburgh, 1850.

Prof. Bowen's Treatise on Logic or the Laws of Pure Thought, Cambridge, U. S. 1866 (Trübner and Co.) gives a full and excellent account of Hamilton's Logic.

LESSON XXIII.

BOOLE'S SYSTEM OF LOGIC

IT would not in the least be possible to give in an elementary work a notion of the system of indirect inference first discovered by the late Dr Boole, the Professor of Mathematics at the Queen's College, Cork. This system was founded as mentioned in the last lesson upon the Quantification of the Predicate, but Dr Boole regarded Logic as a branch of Mathematics, and believed that he could arrive at every possible inference by the principles of algebra. The process as actually employed by hi is very obscure and difficult; and hardly any atte pt to introduce it into ele entary text-books of Logic has yet been made.

I have been able to arrive at exactly the same results

as Dr Boole without the use of any mathematics; and though the very simple process which I am oing to describe can hardly be said to be strictly Dr Boole's logic, it is yet very similar to it and can prove everything that Dr Boole proved. This ethod of direct Inference is founded upon the three primary Laws of Thought stated in Lesson XIV., and the reader who ay have thought them mere useless truisms will perhaps be surprised to find how extensive delegant a syste of deduction may be derived from them.

The law of excluded middle enables us to assert that anything must either have a given quality or must have it not. Thus if *iron* be the thing, and *combustibility* the quality, anyone must see that

"Iron is either combustible or incombustible."

This division of alternatives may be repeated as often as we like. Thus let Book be the class of things to be divided, and English and Scientific two qualities. Then any book ust be either English or not English; again an English book must be either Scientific or not Scientific, and the same may be said of books which are not English. Thus we can at once divide books into four classes—

Books, English and Scientific. Books, English and not-Scientific. Books, not-English and Scientific. ooks, not-English and not-Scientific.

This is what we may call e austive vision of the class Books; for there is no possible book which does not fall into one division or other of these four, on account of the simple reason, that if it does not fall into

y of the three first it ust fall into the last. The process can be repeated without end, as long as any new circumst ce can be suggested as the ground of division. Thus we ight divide each class again according as the

books are octavo or not octavo, bound or unbound, published in London or elsewhere, and so on. We shall call this process of twofold division, which is really the process of Dichotomy entioned in p. 107, the develop ent of a term, because it enables us always to develope the utmost number of alternatives which need be considered.

As a general rule it is not likely that all the alte atives thus unfolded or developed can exist, and the n t point is to ascertain how any do or may exist. The Law of Contradiction asserts that nothing can co bine contradictory attributes or qualities, and if we eet with any term which is thus self-contradictory we are authorized at once to strike it out of the list. Now consider our old example of a syllogism:

Iron is a etal;
All metals are ele ents;
Therefore iron is ele ent.

We can readily prove this conclusion by the 'direct method. For if we develope the term iron, we have four alternatives, thus—

Iron, metal, element.
Iron, etal, not-ele ent.
Iron, not-metal, element.
Iron, not-metal, not-element.

But if we compare each of these alternatives with the premises of the syllogis, it will be apparent that several of the are incapable of existin. Iron, we are fo ed, is a etal. Hence no class of things "iron, not-metal" can exist. Thus we are enabled by the first pre ise to strike out both of the last two alternatives which combine iron and not-metal. The second alternative, again, cobines metal and not-element; but the second pre ise infor s us that "all etals e ele ents," it ust be struck out. There re ns, th, only one alternative

which is capable of existing if the premises be true, and as there cannot conceivably be more alternatives than those considered, it follows demonstratively that iron occurs only in combination with the qualities of etal and ele-

ment, or, in brief, that it is an element.

We can, however, prove not only the ordinary syllogistic conclusion, but any other conclusion which can be drawn from the s e premises; the syllogistic conclusion is in fact only one out of many which can usually be obtained from given pre ises. Suppose, for instance, that we wish to know what is the nature of the term or class not-ele ent, so far as we can learn it from the premises just considered. We can develope the alternatives of this term. just we did those of iron, and get the following-

> Not-element, iron, metal. Not-element, iron, not-metal. Not-ele ent, not-iron, etal. Not-element, not-iron, not-metal.

Co pare these co binations as before with the premises. The first it is easily seen ca ot exist, because all metals are ele ents; for the s e reason the third ca the second is likewise excluded, because iron is a metal and c not exist in combination with the qualities of notetal. Hence there remains only one combination to represent the cl s desired-namely,

Not-ele ent, not-iron, not-metal.

Thus we learn from the premises that every not-eleent is not a metal and is not iron.

As other exa ple of this kind of deductive process I will take a c e of the Disjunctive Syllogis, in the neative ood, follows :--

> A fungus is either plant or ani al. A fungus is not an ani al; Therefore it is a pl .t.

Now if we develope all the possible ways in which fungus, plant and animal can be combined together, we obtain for the term fungus—

- (1) Fungus, plant, animal.
 - 2) Fungus, plant, not-animal.
- (3) Fungus, not-plant, animal.
 - 4) Fungus, not-plant, not-animal.

Of these however the 4th cannot exist because by the pre ise a fungus must be a plant, or if not a pl t an animal. The 1st and 3rd again cannot exist because the minor premise informs us that a fungus is not an animal. There re ains then only the second combination,

Fungus, plant, not-animal,

fro which we learn the syllogistic conclusion that "a fungus is a plant."

The chief excellence of this mode of deduction consists in the fact that it is not restricted to any definite series of for s like the syllogism, but is applicable, without any additional rules, to all kinds of propositions or problems which c be conceived and stated. There may be any nu ber of pre ises, and they ay contain any number of terms; all we have to do to obtain any possible inference is to develope the term required into all its alternatives and then to examine how many of these agree with the pre-

ises. What remain after this examination necessarily form the description of the term. The only inconvenience of the ethod is that, as the number of terms increases, the number of alternatives to be exa ined increases very rapidly, and it soon becomes tedious to write them all out. This work may be abbreviated if we substitute single letters to stand for the terms, somewhat as in algebra; thus we ay take A, B, C, D, &c., to stand for the affirmative te s, and a, b, c, d, &c., for the corresponding negative ones. Let us take as a first example the premises—

Org ic substance is either vegetable or animal.

Vegetable subst ce consists mainly of carbon, hydrogen, and nitrogen.

Animal substance consists mainly of carbon, hydrogen, and nitrogen.

It would take a long time to write out all the combinations of the four terms occurring in the above; but if we substitute letters follows—

A = organic substance,

B =vegetable substance,

C=animal substance,

D=consisting ainly of carbon, hydrogen, and nitrogen,

we can readily represent all the combinations which can belong to the term $\mathcal{A}.$

(1)	ABCD	AbCD	(5)
(2)	ABCd	AbCd	(6)
(3)	ABcD	AbcD	(7)
(4)	ABcd	Abcd	(8)

Now the premises amount to the statements, that

A must be either B or C,

B must be D,

C ust be D.

The combinations (7) and (8) are inconsistent with the first premise; the cobinations (2) and (4) with the second preise; and (6) is inconsistent with the third premise. There reain only,

ABCD ABcD AbCD.

Whence we learn at once that "org ic subst ce (A) always co ists ainly of carbon, hydrogen and nitro en,"

because it always occurs in connexion with D. The reader ay perhaps notice that the term ABCD i plies that organic subst ce ay be both vegetable (B) and animal (C), If the first precise be interpreted as eaning that this is not possible, of course this combination should also be struck out. It is an unsettled point whether the alternatives of a disjunctive proposition can coexist or not (see p. 166), but I much prefer the opinion that they C; define a atternof fact it is quite likely that there exist very simple kinds of living beings, which cannot be distinctly asserted to be vegetable only or animal only, but p take of the nature of each.

As a more coplicated proble to shew the powers of this system, let us consider the premises which were treated by Dr Boole in his Laws of Thought, p. 125, follows:

"Si il figures consist of all whose corresponding angles are equal, and whose corresponding sides are proportional.

Triangles whose corresponding angles e equal have their corresponding sides proportional; and vice versâ.

Triangles whose corresponding sides are proportional have their corresponding angles equal."

Now if we take our symbol letters as follows:

A = similar figure,

B = triangle,

C=having corresponding gles equal,

D=having corresponding sides proportional,

the premises will be seen to amount to the state ents that A is identical with CD.

and that

BC is identical with BD:

other words, all A's ou ht to be CD's, CD's ou ht to

be A's, all BC's ought to be BD's and all BD's ought to be BC's.

The possible combinations in which the letters may be united are 16 in number and are shewn in the following table:

ABCD	aBCD
ABCd	aBCd
ABcD	aBcD
ABcd	aBcd
$A\ b\ CD$	a b CD
AbCd	abCd
AbcD	abcD
Abcd	abcd

Comparing each of these combinations with the precises we see that ABCd, ABcD, ABcd, and others, are to be struck out because every A is also to be CD. The cobinations aBCD dabCD are struck out because every CD should also be A. Again, aBCd is inconsistent with the condition that every BC is also to be BD; and if the reader carefully follows out the same process of examination, there will remain only six combinations, which agree with all the precises, thus—

ABCD	aBcd
$A\ b\ CD$	abCd
	abcD
	ahed

From these combinations we can draw any description we like of the class of things agreeing with the premises. The class A or similar figures is represented by only two combinations or alternatives; the negative class a or dissimilar figures, by four combinations, whence we ay draw the following conclusion: "Dissimilar figures consist of all triangles which have not their corresponding gles equal, disides proportional (aBcd), and of all

figures, not being triangles, which have either their angles equal and sides not proportional (abCa), or their corresponding sides proportional d angles not equal (abcD), or neither their corresponding angles equal nor corresponding sides proportional (abca)."

In performing this ethod of inference it is soon seen to proceed in a very simple mechanical manner, and the only inconvenience is the large number of alte atives or combinations to be examined. I have, therefore, devised odes by which the labour can be decreased: several the simplest of these consists in engraving the series of 16 co binations on the opposite pa e, which occur over and over again in problems, with 1 ger and smaller sets, upon a common writing slate, so that the excluded ones may be readily struck out with a common slate pencil, and yet the series may be employed again for any future logical question. A second device, which I have called the "Logical abacus," is constructed by printing the letters upon slips of wood furnished with pins, contrived so that any part or cl s of the combinations can be picked out mechanically with very little trouble; and a logical problem is thus solved by the hand, rather than by the head. More recently however I have reduced the system to a completely mechanical for , d have thus embodied the whole of the indirect process of inference ay be called a Logic achine. In the front in what of the achine are seen certain oveable wooden rods carrying the set of 16 co binations of letters which are seen on the preceding pa e. At the foot are 21 keys like those of a piano; eight keys towards the left hand marked with the letters A, a, B, b, C, c, D, d, and are intended to represent these terms when occurring in the subject of a proposition. Eight other keys towards the right hand represent the sa e letters or terms when occurring in the predicate. The copula of a proposition is

represented by a key in the middle of the series; the full stop by one to the extreme right, while there are two other keys which serve for the disjunctive conjunction or, according as it occurs in subject or predicate. Now if the letters be taken to stand for the terms of a syllogism or any other logical argument, and the keys of the instrument be pressed exactly in the order corresponding to the words of the premises, the 16 combinations will be so d arranged thereby that at the end only the possible combinations will remain in view. Any question can then be ked of the machine, and an infallible answer will be obtained fro the combinations re aining. internal construction of the machine is such, therefore, as actually to perform the work of inference which, in Dr oole's system, was performed by a very co plicated athe atical calculation. It should be added, that there is one remaining key to the extre e left which has the effect of obliterating all previous operations and restoring all the combinations to their original place, so that the ach e is then ready for the performance of any new problem.

An account of this logical machine may be found in the *Proceedings of the Royal Society* for Jan. 20th, 1870, the achine having on that day been exhibited in action to the Fellows of the Society. The principles of the method of inference here described are more completely stated in *The Substitution of Si ilars**, and the *Principles of Science*†, which I published in the ye s 1869 and 1874. I ayadd, that each of these works contains certain views as to the real nature of the process of inference which I do

† The Principles of Sc. ce: a Treatise on Logic and Scientific Method. 2 vols. Macmill d.Co.

^{*} The Substitution of Similars, the true Principle of Reasoning, dived from a modification of Aristotle's Dictum. Macmill d Co. 1869.

not think it desirable to introduce into an elementary work like the present, on account of their speculative character. The process of inference, on the other hand, which I have derived from Boole's system is of so self-evident a character, and is so clearly proved to be true by its reduction to a mechanical form, that I do not hesitate to bring it to the reader's notice.

George Boole, Mathematical Analysis of Logic, 1847. An Investigation of the Laws of Thought. London, Walton and Maberly, 1854.

LESSON XXIV.

ON METHOD, ANALYSIS AND SYNTHESIS.

IT has been held by many writers on Logic that, in addition to the three parts of logical doctrine which treat successively of Terms, Propositions and Syllogisms, there was a fourth part, which treats of method. Just as the doctrine of Judgment considers the arranging of terms and their combination into Propositions, and the doctrine of Syllogism considers the arranging of propositions that they may form arguments, so there should in like manner be a fourth part, called Method, which should govern the arrange ent of syllogis s and their combination into a complete discourse. ethod is accordingly defined as consisting in such a disposition of the parts of a discourse that the whole may be most easily intelligible.

The celebrated l'eter Ramus, who perished in the massacre of St Bartholomew, first proposed to ake ethod in this ner a part of the science of Logic; but

it may well be doubted whether any definite set of rul or principles can be given to guide us in the arrange ent of "gu ents. Every different discourse must consist of argu ents arranged in accordance with the peculiar nature of the subject; and no general rules can be given for treating things which are infinitely various in the mode of treat-

ent required. Accordingly the supposed general rules of ethod e no better th truis s, that is, they tell us nothing more than we ust be supposed to know beforeh d. Thus, we are instructed in co posing any discourse to be careful that—

- 1. Nothing should be wanting or redundant.
- 2. The separate parts should agree with each other.
- 3. Nothing should be treated unless it is suitable to the subject or purpose.
- 4. The separate parts should be connected by suitable tr sitions.

ut it is evident that the whole difficulty consists in decidin what is wantin or redundant, suitable consistent. Rules of this kind simply tell us to do what we ought to do, 'thout defining what that is.

There ist nevertheless certain general modes of treating any subject which can be clearly distinguished, and should be well understood by the logical student. Logic cannot teach him exactly how d when to use each kind of ethod, but it can teach hi the natures and powers of the methods, so that he 'll be ore likely to use the rightly. We ust distinguish,

- 1. The ethod of discovery,
- 2. The ethod of inst ction.

The ethod of scovery is e ployed in the acquisition of knowledge, and really consists in those processes of inference and induction, by which general truths e certained fro the collection and examination of p ticular facts. This ethod will be the subject of most of our re ainin Lessons. The second ethod only applies when knowledge has already been acquired and expressed in the form of general laws, rules, principles or t ths, so that we have only to make ourselves acquainted with these and observe the due ode of applying them to particular cases, in order to possess a complete acquaintce with the subject.

A student, for exa ple, in learning Latin, Greek, French, German, or any well-known language, receives a complete Grammar and Syntax setting forth the whole of the principles, rules and nature of the language. receives these instructions, and takes them to be true on the authority of the teacher, or the writer of the book; and after rendering them fa iliar to his mind he has nothing to do but to co bine and apply the rules in reading or composing the language. He follows, in short, ethod of Instruction. But this is an entirely different and opposite process to that which the scholar must pursue who has received some writings in an unknown language, and is endeavouring to make out the alphabet, words, grammar, and syntax of the language. possesses not the laws of grammar, but words and sentences obeying those laws, and he has to detect the laws if possible by observing their effects on the written language. He pursues, in short, the method of discovery consisting in a tedious comparison of letters, words, and phrases, such as shall disclose the more frequent combinations and forms in which they occur. The process would be a strictly inductive one, such as I shall partially exemplify in the Lessons on Induction; but it is far more the method of Instruction, and depends to a difficult th great extent on the happy use of conjecture and hypothesis, which demands a certain skill and inventive ability.

Exactly the same may be said of the investigation of

natural things and events. The principles of ech ics of the lever, inclined plane, and other Mechanical Powers. or the Laws of Motion, see comparatively si ple and obvious as explained to us in books of instruction. But the early philosophers did not possess such books; they had only the Book of Nature, in which is set forth not the laws but the results of the laws, and it was only after the most patient and skilful investigation, and after hundreds of mistakes, that those laws were ascertained. It is very easy now to understand the Copernican system of Astronomy, which represents the planets as revolving round the sun in orbits of various agnitude. Once knowing the theory we can readily see why the planets have such various ovements and positions, and why they so etimes stand still; it is easy to see, too, why in addition to their own proper motions they all go round the th apparently every day in consequence of the earth's diurnal rotation. But all these changes were exceedingly puzzling to the ancients, who re arded the earth as standing still.

The covery thus begins with facts apethod of parent to the senses, and has the difficult t k of detecting those universal laws or general principles which can only be co prehended by intellect. It has been aptly said that the method of discovery thus proceeds from things better known to us, or our senses (nobis notiona), to those which are more simple or better known in nature (notiona naturæ). The method of Instruction proceeds in the opposite direction, beginning with the things notiora natura, and proceeding to show or explain the things The difference is almost like that between nobis notiora. hiding and seeking. He who has hidden a thing knows where to find it; but this is not the position of a discoverer, who has no clue except such as he may meet in his own dili ent d sagacious se ch.

Closely corresponding to the distinction between the methods of Discovery and Instruction is that between the methods of Analys and Synthesis. It is very important indeed that the reader should clearly apprehend the eanings of these terms in their several applications. Analysis is the process of separating a whole into its parts, d synthesis the combination of parts into a whole. The analytical chemist, who receives a piece of mineral for examination, may be able to separate completely the several chemical elements of which it is composed and ascertain their nature and comparative quantities; this is chemical analysis. In other cases the chemist mixes together carefully weighed quantities of certain simple substances and combines them into a new compound substance; this is chemical synthesis. Logical analysis and synthesis must not be confused with the physical actions, but they are nevertheless actions of mind of an analogous character.

In logical synthes we begin with the simplest possible notions or ideas, and combine them together. We have the best possible example in the elements of Geometry. In Euclid we begin with certain simple notions of points, straight lines, angles, right angles, circles, &c. Putting together three straight lines we make a triangle: joining to this the notion of a right-angle, we form the notion of a right-angled triangle. Joining four other equal lines at right angles to each other we gain the idea of a square, and if we then conceive such a square to be formed upon each of the sides of a right-angled tri gle, and re on fro the necessary qualities of these figures, we discover that the two squares upon the sides containing the right an le ust together be exactly equal to the square upon the third side, shewn in the 47th Proposition of Euclid's first book. This is a perfect inst ce of co -

binin simple ideas into more complex ones.

We have often, however, in Geometry to pursue the opposite course of Anal is. A complicated geo etrical figure ay be given to us, and we ay have, in order to prove the properties which it possesses, to resolve it into its sep ate parts, and to consider the properties of those parts each distinct from the others.

A si il distinction between the analytical d synthetic ethods c be traced throughout the natural sciences. By keeping exact registers of the appearance

d changes of the weather we may readily acquire an mense collection of facts, each such recorded fact i plying a multitude of different circumstances occurring to ether. Thus in any storm or shower of rain we have to consider the direction and force of the wind; the temperature and oistness of the air; the height d forms of the clouds; the quantity of rain which falls, or the lightning and thunder which occur with it. If we proceed by

alysis only to explain the changes of the weather we should have to try resolving each sto or change of w ther into its separate circu stances, and comparing

ch with every other to discover what circu stances usually go together. We might thus ascertain no doubt with considerable certainty what kinds of clouds, and what changes of the wind, temperature, moisture, &c., usually precede any kind of sto, and we might even in ti e give some imperfect explanation of what takes place in the atmosphere.

But we might also apply with advantage the synthetical ethod. By previous chemical investigations we know that the atmosphere consists mainly of the two fixed es, oxygen and nitrogen, with the vapour of water, the latter being very variable in quantity. We can try experi entally what takes place when portions of such air of v 'ous degrees of oistness e copressed or allowed to expand, or are 'ed to ether,

often happens in the at osphere. It is thus discovered that whenever moist air is allowed to expand cloud is produced, and it ay be drops of rain. Dr Hutton, too, found that whenever cold moist air is mixed with warm oist air cloud is again produced. We c safely argue from such s all experi ents to what takes place in the atmosphere. Putting together synthetically, fro the sciences of chemistry, ech ics, and electricity, all that we know of air, wind, cloud d lightning, we are able to explain what takes place in a thunder-storm far ore co pletely than we could do by merely observing directly what happens in the storm. We are here however anticipating the ethods of inductive investigation. which we ust consider in the followin lessons. It will appear that duction is equivalent to alvsis, and that the deductive kinds of reasoning which we have treated in prior lessons *e of a synthetic character.

It has been said that the synthetic method usually corresponds to the method of instruction and the ethod to that of discovery. But it ay be possible to discover new truths by synthesis d to teach old ones by analysis. Sir John Herschel in his well-known Outlines of Astrono vy partially adopts the analytic ethod; he supposes a spectator in the first place to survey the appearances of the heavenly bodies and the surface of the earth, and to seek an explanation; he then leads through a course of arguments to show that these appearances really indicate the rotundity of the earth, its revolution about its own axis and round the sun, subordinate position as one of the s aller planets of the solar system. Mr Norman Lockyer's Elementary Lessons in Astronomy is a clear example of the synthetic method of instruction; for he commences by describing the sun, the centre of the system, and successively adds the planets d other e bers of the system, until at last we have 208

the complete picture; and the reader who has tempor ily received everything on the writer's authority, sees that the description corresponds with the truth. Each method, it ust be allowed, has its own advantages.

ust be carefully observed that the meaning of analysis, and therefore that of synthesis, varies according as we look to the intension or extension of terms. To divide or analyse a cl s of things in extension I must add a quality or difference. Thus I divide the class organism when I add the quality vegetable, d separate vegetable organism fro what is not vegetable. Analysis sion is therefore the sa e process as synthes in intend vice versá, whenever I separate or analyse a group of qualities each part belongs to a larger class of things in extension. When I analyse the notion vegetable org ism, and regard the notion organism apart from vegetable, it is apparent that I really add the whole class of ani al organis s to the class I a considering-so that analys in tension synthesis in e ension. The reader who has well considered the contents of Lessons v. d XII. will probably see that this connection of the two processes is only a re-statement of the law, (p. 40). that "as the intension of a term is increased the extension is decreased."

To express the difference between knowledge derived deductively and that obtained inductively the Latin phrases à priori and à posteriori are often used. By A priori re oning we mean argu ent based on truths previously known; A posteriori reasoning, on the contrary, proceeds to infer from the consequences of a general truth what that general truth is. Many philosophers consider that the ind is naturally in possession of certain laws or truths which it ust recognise in every act of thought; all such, if they exist, would be à priori truths. It cannot be doubted, for instance, that we must always

recognise in thought the three Primary Laws of Thought considered in Lesson XIV. We have there an a priori knowledge that "matter c not both have weight and be without weight," or that "every thing must be either self-luminous or not self-luminous." But there is no law of thought which can oblige us to think that matter has weight, and luminous ether h not weight; that Jupiter and Venus are not self-lu inous, but that comets are to some extent self-luminous. These are facts which are no doubt necessary consequences of the laws of nature and the general constitution of the world; but we are not naturally acquainted with all the secrets of creation, we have to learn them by observation, or by the a posteriori method.

It is not however usual at the present time to restrict the name à priari to truths obtained altogether without recourse to observation. Knowledge may originally be of an à posteriori origin, and yet having been long in possession, and having acquired the greatest certainty, it may be the ground of deductions, and ay then be said to give à priori knowledge. Thus it is now believed by all scientific men that force cannot be created or destroyed by any of the processes of nature. If this be true the force which disappears when a bullet strikes a target must be converted into something else, and on à priori grounds ay assert that heat will be the result. It is true that ight easily learn the same truth à posteriori, by picking up portions of a bullet which has just struck a target and observing that they are warm. But there is a great advantage in à priori knowledge; we can often apply it in cases where experiment or observation would be difficult. If I lift a stone and then drop it, the delicate instruments could hardly show that the stone was heated by striking the earth; yet on à priori grounds I know that it ust have been so and can easily calculate the amount of heat produced. Similarly we know, thout the trouble of observation, that the Falls of Niagara and all other waterfalls produce heat. This is fairly an instance of à priori knowledge because no one that I have heard of has tried the fact or proved it à posteriori; nevertheless the knowledge is originally founded on the experiments of Mr Joule, who observed in certain well-chosen cases how much force is equivalent to a certain amount of heat. The reader, however, should take care not to confuse the meaning of à priori thus explained with that given to the words by the philosophers who hold the mind to be in the possession of knowledge independently of all observation.

It is not difficult to see that the à priori method is equivalent to the synthetic method (see p. 205) considered in intension, the à posteriori method of course being equivalent to the analytic ethod. But the same difference is really expressed in the words deductive and inductive; and we shall frequently need to consider it in the following lessons.

For general remarks upon Method see the *Port Royal Logic*, Part IV.

LESSON XXV.

PERFECT INDUCTION AND THE INDUCTIVE SYLLOGISM.

WE have in previous lessons considered deductive reasoning, which consists in co bining two or ore propositions synthetically, and thus arrivin at a conclusion which is a proposition or truth of less enerality than

the re ises, that is to say, it applies to fewer individual instances than the separate premises from which it was inferred. When I combine the general truth that "metals are good conductors of heat," with the truth that "aluminium is a metal," I am enabled by a syllogism in the mood Barbara to infer that "aluminium is a good conductor of heat." As this is a proposition concerning one metal only, it is evidently less general than the premise, which referred to all metals whatsoever. In induction, on the contrary, we proceed from less general, or even from individual facts, to more general propositions, truths, or, as we shall often call them. Laws of Nature. When it is known that Mercury moves in an elliptic orbit round the Sun, as also Venus, the Earth, Mars, Jupiter, &c., we are able to arrive at the simple and general truth that "all the planets move in elliptic orbits round the sun." This is an example of an inductive process of reasoning.

It is true that we may reason without rendering our conclusion either more or less general than the premises, as in the following:—

Snowdon is the highest mountain in England or Wales.

Snowdon is not so high as Ben Nevis.

Therefore the highest mountain in England or Wales is not so high as Ben Nevis.

Again:

Lithium is the lightest metal known.

Lithium is the metal indicated by one bright red line in the spectrum *.

Therefore the lightest metal known is the metal indicated by a spectrum of one bright red line.

In these examples all the propositions are singul propositions, and merely assert the identity of singular

^{*} Roscoe's Lessons in Elementary Ch istry.

ter s, so that there is no alteration of generality. Each conclusion applies to just such an object as each of the premises applies to. To this kind of reasoning the apt

name of Traduction has been given.

Induction is a much more difficult and more important kind of reasoning process than Traduction or even Deduction; for it is engaged in detecting the general laws or uniformities, the relations of cause and effect, or in short all the general truths that may be asserted concerning the numberless and very diverse events that take place in the natural world around us. The greater part, if not, as some philosophers think, the whole of our knowledge, is ultimately due to inductive reasoning. The mind, it is plausibly said, is not furnished with knowledge in the form of general propositions ready made and stamped upon it, but is endowed with powers of observation, comparison, and reasoning, which are adequate, when well educated and exercised, to procure knowledge of the world without us and the world within the human ind. Even when we argue synthetically and deductively from simple and truths which seem to be ready in the mind, as in the case of the science of geometry, it may be that we have gathered those simple ide and truths fro previous observation or induction of an almost unconscious kind. This is a debated point upon which I will not here speak positively; but if the truth be as stated, duction will be the mode by which all the materials of knowledge are brought to the mind and analysed. Deduction will then be the almost equally i portant process by which the knowledge thus acquired is utilised, and by which new Inductions of a more complicated character, as we shall see, are rendered possible.

An Induction, that is an act of Inductive reasoning, is called **Perfect** when all the possible cases or instances to which the conclusion can refer, have been examined and

enumerated in the premises. If, usually happens, it is impossible to exa ine all cases, since they may occur at future times or in distant parts of the earth or other regions of the universe, the Induction is called Imperfect. The assertion that all the onths of the year are of less length than thirty-two days is derived from Perfect Induction, and is a certain conclusion because the calendar is a human institution, so that we know beyond doubt how many months there are, and can readily ascertain that each of them is less than thirty-two days in length. the assertion that all the planets move in one direction round the sun, from West to E t, is derived from Imperfect Induction; for it is possible that there exist planets more distant than the most distant-known planet Neptune, and to such a planet of course the assertion would apply.

Hence it is obvious that there is a great difference between Perfect d Imperfect Induction. The latter includes so e process by which we are enabled to make

sertions concerning things that we have never seen or ined or even known to exist. But it must be carefully remembered also that no Imperfect Induction can give a certain conclusion. It ay be highly probable or nearly certain that the cases unexamined will resemble those which have been examined, but it can never be certain. It is quite possible, for inst ce, that a new planet might go round the sun in an opposite direction to the other planets. In the case of the satellites belonging to the planets more than one exception of this kind h been discovered, and mistakes have constantly occurred in science from expectin that all new c es would exactly resemble old ones. Imperfect Induction thus gives only a certain degree of probability or likelihood that all instances will agree with those exa ined. Perfect Induction, on the other hand, gives a necessary and certain conclusion, but it asserts nothing beyond what

w serted the premises.

Mr Mill, 'deed, differs fro al ost all other logicians in holding that Perfect Induction is properly called Induction, because it does not lead to any new knowledge. He defines duction as inference from the known to the unknown, and considers the unex ined cases which e apparently brought into our knowledge as the only gain from the process of reasoning. Hence Perfect Induction see s to h' to be of no scientific value whatever, because the conclusion is a mere reassertion in a briefer fo , a ere su ing up of the premises. I may point out, however, that if Perfect Induction were no ore than a process of abbreviation it is yet of great i portance, and requires to be continually used in science and common life. Without it we could never ake a comprehensive state ent, but should be obliged to enumerate every particul. After ex ining the books in a library and finding the to be all English books we should be unable to sum up our results in the one proposition, "all the books in this library e En lish books:" but should be required to go over the list of books every time we desired to make any one acquainted with the contents of the library. The fact is, that the power of expressing a great nu ber of particul facts in a very brief space is essential to the progress of science. Just the whole art of arith etic consists in nothing but a series of processes for abbreviating addition and subtraction, and enable g us to deal with a great n ber of u ts in a very short time, so Perfect Induction is absolutely necessary to enable us to deal with a great nu ber of particular facts in a very brief space.

It is usual to represent Perfect Induction in the form of an due ve Sy ogism, in the following instance:—
Mercury, V us, the Earth, &c., all ove round the sun

fro West to East.

Mercury, Venus, the Earth, &c., are all the known Planets. Therefore all the known planets move round the sun fro West to East.

This gu ent is a true Perfect Induction because the conclusion only akes an assertion of all known planets, which excludes all reference to possible future discoveries: and we may suppose that all the known planets have been enumerated in the pre ises. The form of the argument appears to be that of a syllogism in the third figure, na elv Darabti, the middle term consisting in the group of the known pl ets. In reality, however, it is not an ordinary syllogism. The minor premise states not that Mercury, Venus, the Earth, Neptune, &c., are contained among the known pl ets, but that they are those pl ets, or are identical with them. This pre ise is then a doubly universal proposition of a kind (p. 184-7) not recognised in the Aristotelian Syllogism. Accordin ly we av observe that the conclusion is a universal proposition, which is not allowable in the third figure of the syllogis .

As another ex ple of a Perfect Induction we may take—

January, February,...........December, each contain less than 32 days.

January......December e all the months of the y r.

Therefore all the onths of the year contain less th 32 days.

Although Sir W. H ilton has entirely rejected the notion, it seems worthy of inquiry whether the Inductive Sy ogis be not really of the Disjunctive form of Syllogis. Thus I should be inclined to represent the last exa ple in the fo :

A onth of the year is either January, or Feb ary, or March.....or Dece ber; but Janu y has less

than 32 days; and February has less than 32 days; d so on until we come to December, which has less than 32 days.

It follows clearly that a month must in any case have less than 32 days; for there are only 12 possible cases, and in each c e this is affirmed. The fact is that the major premise of the syllogism on the last page is a compound sentence with twelve subjects, and is therefore equivalent to twelve distinct logical propositions. The minor premise is either a disjunctive proposition, as I have represented it, or so ething quite different from anything we have elsewhere had.

From Perfect Induction we shall have to pass to Imperfect duction; but the opinions of Logicians are not in agreement as to the grounds upon which we are warranted in taking a part of the instances only, d concluding that what is true of those is true of all. Thus if we adopt the example found in many books and say—

This, that, d the other agnet attract iron; This, that, and the other magnet are all magnets; Therefore all magnets attract iron,

we evidently e ploy a false minor premise, because this, that, and the other magnet which we have examined, cannot possibly be all existing magnets. In whatever form we put it there must be an sumption that the agnets which we have examined are a fair specimen of all magnets, so that what we find in so e we may expect in all. Archbishop Whately considers that this assumption should be expressed in one of the pre 'ses, d he reprents Induction a Syllogism in Barbara as follows:—

That which belongs to this, that, d the other magnet, belon s to all;

Attracting iron belongs to this, that, and the other; Therefore it belongs to all.

But though this is doubtless a correct expression of the assumption ade in Imperfect Induction, it does not in the least explain the grounds on which we are allowed to make the assu ption, and under what circu stances such an assumption would be likely to provetrue. So e writers have asserted that there is a Principle called the Uniformity of at e, which enables us to affirm that what has often been found to be true of anything will continue to be found true of the same sort of thing. It must be observed, however, that if there be such a principle it is liable to exceptions; for many facts which have held true up to a certain point have afterwards been found not to be always true. Thus there was a wide d unbroken induction tending to show that all the Satellites in the planetary system went in one uniform direction round their planets. Nevertheless the Satellites of Uranus when discovered were found to move in a retrograde direction, or in an opposite direction to all Satellites previously known, and the same peculiarity attaches to the Satellite of Neptune more lately discovered.

We may defer to the next lesson the question of the varying degree of certainty which belongs to induction in the several branches of knowledge.

The advanced student may consult the following with advantage:—Mansel's Aldrich, Appendix, Notes G and H. Hamilton's Lectures on Logic, Lecture XVII., and Appendix VII., On Induction and Example, Vol. II., p. 358. J. S. Mill's System of Logic, Book III. Chap. 2, Of Inductions improperly so-called.

LESSON XXVI.

GEOMETRICAL AND MATHEMATICAL INDUC-TION, ANALOGY AND EXAMPLE.

IT is now indispensable that we should consider with great care upon what grounds I perfect Induction is founded. No difficulty is encountered in Perfect Induction because all possible cases which can come under the general conclusion are enu erated in the pre ises, so that in fact there is no infor ation in the conclusion which w not given in the premises. In this respect the Inductive Syllogism perfectly agrees with the general principles of deductive reasoning, which require that the information contained in the conclusion should be shown only from the data, and that we should merely unfold, or tr sfo into explicit state ent what is contined in the pre 'ses i plicitly.

duction the process see s to be of a In perfect wholly different character, since the instances concerning which we acquire knowledge ay be infinitely more nu erous than those fro which we acquire the knowledge. Let us consider 'the first place the process of asoning which has a close rese blance to o etri inductive reason' g. When in the fifth proposition of the first book of Euclid we prove that the angles at the base isosceles trian le e equal to each other, it is done of by takin one particul triangle as an example. A figure is given which the reader is requested to regard as havin two equal sides, d it is conclusively proved that if the sides be really equal then the angles opposite to those sides ust be equal also. But Euclid says nothin about other isosceles trian les; he treats one sin le triangle a su cient speci en of all isosceles triangles,

and we easked to believe that what is true of that is true of any other, whether its sides be so s all as to be only visible in a 'croscope, or so large as to reach to the furthest fixed st . There ay evidently be number of isosceles triangles as regards the length of the equal sides, and each of these ay be infinitely v ied by increasing or diminishing the contained angle, so that the number of possible isosceles triangles is infinitely infinite; and yet we are asked to believe of this inco prehensible nu ber of objects what we have proved only of one single specimen. This might seem to be the most extremely Imperfect Induction possible, and yet every one allows that it gives us really certain knowledge. We do know uch certainty as knowledge can possess, that if lines be conceived as drawn from the e th to two stars equally distant, they will make equal angles with the line joining those stars; and yet we can never have tried the experiment.

The generality of this geometrical reasoning evidently depends upon the certainty with which we know that all isosceles tri gles exactly resemble each other. The proposition proved does not in fact apply to a tri gle unless it agrees with our speci en in all the qualities essential to the proof. The absolute length of any of the sides or the absolute magnitude of the angle contained between any of them were not points upon which the proof depended—they were purely accidental circumst ces; hence we are at perfect liberty to apply to all new c es isosceles triangle what we learn of one case. Upon a similar ground rests all the v t body of certain knowledge contained in the mathematical sciences—not only all the geometrical truths, but all general algebraical truths. It was shown, for instance, in p. 58, that if d δ be two quantities, and we ultiply together d difference, we get the difference of the their su

squares of a and b. However often we try this it will be found true; thus if a = 10 and b = 7, the product of the sum and difference is $17 \times 3 = 51$; the squares of the quantities are 10 x 10 or 100 and 7 x 7 or 49, the difference of which is also 51. But however often we tried the rule no certainty would be added to it; because when proved algebraically there was no condition which restricted the result to any particular numbers, and a and b might consequently be any numbers whatever, This generality of algebraical reasoning by which a property is proved of infinite varieties of numbers at once, is one of the chief advantages of algebra over arithmetic. There is also in algebra a process called athe atical Induction or De onstrative Induction, which shows the powers of reasoning in a very conspicuous way. A good example is found in the following problem:-If we take the first two consecutive odd numbers, 1 and 3, and add them together the sum is 4, or exactly twice two; if we take three such numbers 1+3+5, the sum is 9 or exactly three times three; if we take four, namely 1+3+5+7 the sum is 16, or exactly four times four; or generally, if we take any given number of the series, 1+3+5+7+... the sum is equal to the number of the terms multiplied by itself. Anyone who knows a very little algebra can prove that this remarkable law is universally true, as follows-Let n be the number of terms, and assume for a ornent that this law is true up to n terms, thus—

$$1+3+5+7+.....+(2n-1)=n^2$$
.

Now add 2n+1 to each side of the equation. It follows that—

$$1+3+5+7+\ldots+(2n-1)+(2n+1)=n^2+2n+1$$
.

But the last quantity $n^2 + 2n + 1$ is just equal to $(n + 1)^2$; so that if the law is true for n terms it is true also for n + 1 te s. We are enabled to argue from each single case of

the law to the next case; but we have already shown that it is true of the first few cases, therefore it ust be true of all. By no conceivable labour could a person ascertain by trial what is the sum of the first billion odd numbers, and yet symbolically or by general reasoning we know with certainty that they would amount to a billion billion, and neither ore nor less even by a unit. This process of Mathematical Induction is not exactly the sa e as Geometrical Induction, because each c e depends upon the last, but the proof rests upon an equally narrow basis of experience, and creates knowledge of equal certainty and generality.

Such mathematical truths depend upon observation of a few cases, but they acquire certainty fro the perception we have of the exact similarity of one c e to another, so that we undoubtingly believe what is true of one case to be true of another. It is very instructive to contrast with these cases certain other ones where there is a like ground of observation, but not the same tie of similarity. It was at one time believed that if any integral number were multiplied by itself, added to itself d then added to 41, the result would be a prime number, that is a number which could not be divided by any other integral number except unity; in sy bols,

 $x^2 + x + 41 = prime number.$

This was believed solely on the ground of trial and experience, and it certainly holds for a great many values of x. Thus when x is successively made equal to the numbers in the first line below, the expression x^2+x+41 gives the values in the second line, and they are all prime numbers:

o 1 2 3 4 5 6 7 8 9 10 41 43 47 53 61 71 83 97 113 131 151

No reason however could be given why it should

always be true, and accordingly it is found that the rule does not always hold true, but fails when x=40. Then we have $40 \times 40 + 40 + 41 = 1681$, but this is clearly equal to $41 \times 40 + 41$ or 41×41 , and is not a prime number.

In that branch of mathematics which treats of the peculiar properties and kinds of numbers, other propositions depending solely upon observation have been asserted to be always true. Thus Fermat believed that $2^{\frac{\pi}{2}} + 1$ always represents a prime number, but could not give any reason for the assertion. It holds true in fact until the product reaches the large number 4294967297, which was found to be divisible by 641, so that the generality of the statement was disproved.

We find then that in some cases a single instance proves a general and certain rule, while in others a very great number of instances are insufficient to give any certainty at all; all depends upon the perception we have of similarity or identity between one case and another. We can perceive no similarity between all prime numbers which assures us that because one is represented by a certain formula, also another is; but we do find such similarity between the sums of odd numbers, or between isosceles triangles.

Exactly si ilar conside tions apply to inductions in physical science. When a chemist analyses a few rains of water and finds that they contain exactly 8 parts of oxygen d I of hydrogen for 9 parts of water, he feels warranted in asserting that the same is true of all pure water whatever be its origin, and whatever be the part of the world from which it comes. But if he analyse a piece of granite, or a s ple of sea-water from one part of the world, he does not feel any confidence that it will reseble exactly a piece of granite, or a saple of sea-water froother part of the earth; hence he does not venture to sert of all granite or sea-water, what he finds true of

a single sample. Extended experience shows that granite is very variable in composition, but that sea-water is rendered pretty uniform by constant mixture of currents. Nothing but experience in these cases could inform us how far we may assert safely of one sample what we have ascertained of another. But we have reason to believe that chemical compounds are naturally fixed and invariable in composition, according to Dalton's laws of combining proportions. No à priori reasoning fro principles of thought could have told us this, and we only learn it by extended experiment. But having once shown it to be true with certain substances we do not need to repeat the trial with all other substances, because we have every reason to believe that it is a natural law in which all chemical substances rese ble each other. It is only necessary then for a single accurate analysis of a given fixed compound to be made in order to inform us of the composition of all other portions of the same substance.

It must be carefully observed however that inductions in physical science are only probable, or that if certain, it is only hypothetical certainty they possess. Can I be absolutely certain that all water contains one part of hydrogen in nine? I am certain only on two conditions:—

 That this w certainly the composition of the sample tried.

 That any other substance I call water exactly rese bles that sample.

But even if the first condition be undoubtedly true, I cannot be certain of the second. For how do I know what is water except by the fact of its being a tr sp ent liquid, freezing into a solid and evaporating into ste, possessing a high specific heat, and a number of other distinct properties? But can I be absolutely certain that every liquid possessing all these properties is water?

Practically I can be certain, but theoretically I cannot. Two substances may have been created so like each other that we should never yet have discovered the difference. we might then be constantly misled by assuming of the one what is only true of the other. That this should ever happen with substances possessing the very distinct qualities of water is excessively improbable, but so far is it from being impossible or improbable in other cases, that it has often happened. Most of the new elements discovered in late years have, without doubt, been mistaken previously for other elements. Cæsium and Rubidium had been long mistaken for each other, and for Potassium. before they were distinguished by Bunsen and Kirchhoff by means of the spectroscope. As they are now known to be widely distributed, although in small quantities, it is certain that what was supposed to be Potassium in many thousands of analyses was partly composed of different substances. Selenium had probably been confused with Sulphur, and there are certain metals-for instance, Rhodium, Ruthenium, Iridium, Osmium, and Beryllium-Yttrium, Erbium, Cerium, Lanthanu, and Didymium-Cad ium and Indium-which have only recently been distinguished. The progress of science will doubtless show that we are mistaken in many of our identifications, and various difficulties thus arising will ultimately be explained.

Take again a very different case of induction. Are we certain that the sun will rise again to-morrow morning as it has risen for many thousand years, and probably for some hundred illion years? We are certain only on this condition or hypothesis, that the planetary system proceeds to-morrow as it has proceeded for so long. Many causes ay exist which might at any oment defeat all our

calculations; our sun is believed to be a variable star, and for what we know it ight at any oment suddenly

explode or flare up, as certain other stars have been observed to do, and we should then be all turned into thin lu inous vapour in a moment of ti e. It is not at all i possible that a collision did once occur in the planetary system, and that the minute planets or asteroids are the result. Even if there is no large eteor, comet or other body capable of breaking up the e th by collision, yet it is probable that the sun moves through space at the rate of nearly 300 miles per minute, and if so e other star should meet us at a similar rate the consequences would be inconceivably terrible. It is highly improbable however that such an event should come to pass even in the course of a million years.

The reader will now see that no mere Imperfect Induction can give certain knowledge; all inference proceeds upon the assumption that new instances will exactly resemble old ones in all material circumstances; but in natural phenomena this is purely hypothetical, and we may constantly find ourselves in error. In Mathematical Induction certainty arose from the cases being hypothetical in their own nature, or being made so as exactly to correspond with the conditions. We cannot assert that any triangle existing in nature has two equal sides or two equal angles, and it is even impossible in practice that any two lines or angles can be absolutely equal. But it is nevertheless true that if the sides are equal the angles are equal. All certainty of inference is thus relative and hypothetical. Even in the syllogism the certainty of the conclusion only rests on the hypothesis of certainty in the premises. It is probable, in fact, that all reasoning reduces itself to a single type—that what is tr of one thing will be true of another thing, on condition of there being an exact resemblance between them in all aterial circu stances.

The reader will now understand with ease the nature

of reasoning by analo. In strictness an analogy is not identity of one thing with another, but an identity of relations. In the case of numbers 7 is not identical with 10 nor 14 with 20, but the ratio of 7 to 10 is identical with the ratio of 14 to 20, so that there is an analogy between these numbers. To multiply two by two is not the same thing as to construct a square upon a line two units long; but there is this analogy—that there will be just as many units of area in the square as there are units in the product of two by two. This analogy is so evident that we fearlessly assert a square mile to consist of 1760 × 1760 square yards without any trial of the truth. In ordinary language, however, analogy has come to mean any resemblance between things which enables us to believe of one what we know of the other.

Thus the planet Mars possesses an atmosphere, with clouds and mist closely rese bling our own; it has seas distinguished from the land by a greenish colour, and polar regions covered with snow. The red colour of the planet seems to be due to the atmosphere, like the red colour of our sunrises and sunsets. So much is similar in the surface of Mars and the surface of the Earth that we readily argue there ust be inhabitants there as here. All that we can certainly say however is, that if the circu stances be really similar, and si ilar ger s of life have been created there as here, there be inhabitants. The fact that many circumstances are similar increases the probability. But between the Earth and the Sun the analogy is of a much fainter character; we speak indeed of the sun's atmosphere being subject to storms and filled with clouds, but these clouds are heated probably beyond the temperature of our hottest furnaces; if they produce rain it ust resemble a shower of melted iron; and the sun-spots are perturbations of so tremendous a size and character, that the earth together with

half-a-dozen of the other planets could readily be swallowed up in one of them*. It is plain then that there is little or no analogy between the Sun and the Earth, and we can therefore with difficulty form a conception of anything going on in a sun or star.

Argument from analogy may be defined as direct inductive inference from one instance to any similar instance. It may, as Mr Mill says, be reduced to the following formula:—

"Two things resemble each other in one or more respects; a certain proposition is true of the one; therefore it is true of the other." This is no doubt the type of all reasoning, and the certainty of the process depends entirely upon the degree of resemblance or identity between the cases. In geometry the cases are absolutely identical in all material points by hypothesis, and no doubt attaches to the inference; in physical science the identity is a question of probability, and the conclusion is in a like degree probable. It should be added that Mr Mill considers Geometrical and Mathematical Induction not to be properly called Induction, for reasons of which the force altogether escapes my apprehension; but the reader will find his opinions in the 2nd chapter of the 3rd book of his System of Logic.

One form of analogical or inductive argument consists in the constant use of ex ples and inst ces. The best way to describe the nature of a class of things is to present one of the things itself, and point out the properties which belong to the class as distinguished from those peculiar to the thing. Throughout these Lessons, as throughout every work on Logic, instances of propositions, of compound or complex sentences, of syllogisms, &c., are continually used, and the reader is asked to apply to all

^{*} Lockyer's Elementary Lessons in Astronomy, § 108.

si ilar c es what he observes in the examples given. It is ass ed that the writer selects such examples as t ly exhibit the properties in question.

While all inductive and analogical inferences rest upon the same principles there are wide differences between the sources of probability. In alogy we have two c es which resemble each other in a great many properties, and we infer that some additional property in one is probably to be found in the other. The very narrow basis of experience is co pensated by the high degree of similarity. In the processes more co only treated under the name Induction, the things usually rese ble each other only in two or three properties, and we require to have more instances to assure us that what is true of these is probably true of all similar instances. The less, in short, the intension of the resemblance the greater must be the extension of our inquiries.

We proceed to the ordinary processes of Induction in the following Lessons.

r Mill's System of Logic, Book III. Chap. XX. Of Analogy. Mansel's Aldrich, App. Note H. On Example and Analogy.

LESSON XXVII.

OBSERVATION AND EXPERIMENT.

ALL knowled e, it ay be safely said, must be ulti ately founded upon e rien, which is but a general n e for the various feelings i pressed upon the mind at any period of its existence. The ind never creates entirely new knowledge independent of experience, d all that the re oning powers can do is to arrive at the full eaning

of the facts which are in our possession. In previous centuries men of the highest ability have held that the

ind of its own power alone could, by sufficient cogitation, discover what things outside us should be, and would be found to be on examination. They thought that we were able to anticipate Nature by evolving from the human mind an idea of what thin s would be made by the Creator. The celebrated philosopher D cartes thus held that whatever the mind can clearly conceive may be considered true; but we can conceive the existence of mountains of gold or oceans of fresh water, which do not as a fact exist. Anything that we can clearly conceive must be conformable to the laws of thought, and its existence is then not impossible, so far as our intellect is concerned: but the forms and sizes and manners in which it has pleased the Creator to ake thin s in this or any other part of the universe, cannot possibly be anticipated by the exceedingly limited wisdom of the human mind, and can only be learnt by actual examination of existing things.

In the latter part of the 13th century the great Roger Bacon clearly taught in England the supreme importance of experience as the basis of knowledge; but the same doctrine was also, by a curious coincidence, again upheld in the 17th century by the great Chancellor Francis Bacon, after whom it has been called the aconian P-losophy. I believe that Roger Bacon was even a greater man than Francis, whose fame is best known; but the words in which Fr cis Bacon proclaimed the importance of experience and experiment must be ever memorable. In the beginning of his great work, the o Organ, or New Instrument, he thus points out our proper position as learners in the world of nature.

"Man, the Servant and Interpreter of Nature, can do and underst d as much as he has observed concernin the order of nature in outward things or in the ind; more, he can neither know nor do."

The above is the first of the aphorisms or paragraphs with which the *Novum Organum* commences. In the second aphorism he asserts that the unaided mind can effect little and is liable to err; assistance in the form of a definite logical method is requisite, and this it was the purpose of his New Instrument to furnish. The 3rd and 4th aphorisms must be given entire; they are:—

"Human science and human power coincide, because ignorance of a cause deprives us of the effect. For nature is not conquered except by obedience; and what we discover as a cause by contemplation becomes a rule in

operation."

"Man can himself do nothing else than move natural bodies to or from each other; nature working within does the rest."

It would be impossible more clearly and completely to express the way in which we discover science by interpreting the changes we observe in nature, and then turn our knowledge to a useful purpose in the promotion of the arts and manufactures. We cannot create and we cannot destroy a particle of matter; it is now known that we cannot even create or destroy force; nor can we really alter the inner nature of any substance that we have to deal with. All that we can do is to observe carefully how one substance by its natural powers acts upon another substance, and then by moving them together at the right time we can effect our object; as Bacon says, "Nature working within does the rest." Had it not been the nature of heat when applied to water to develope steam possessing elastic power, it is needless to say that the steam-engine could never have been made, so that the invention of the steam-engine arose from observing the utility of the force of steam, and employing it accordingly.

It is in this sense that Virgil has proclaimed hi happy who knows the causes of things—

Felix qui potuit reru cognoscere causas,

and that Bacon has said, Knowledge is Power. So far as we have observed how things happen in nature, and on what occasion particular effects are brought to pass, we are enabled to avoid or utilise those effects as we may desire, not by altering the natures of things, but by allowing them in suitable times and circumstances to manifest their own proper powers. It is thus, as Tennyson h excellently said, that we

"Rule by obeying Nature's Powers."

ductive logic treats of the methods of reasoning by which we may successfully interpret nature and learn the natural laws which various substances obey in different circumstances. In this lesson we consider the first requisite of induction, namely, the e erience or examination of nature which is requisite to furnish us with facts. Such experience is obtained either by observation or e eri ent. To observe is merely to notice events and changes which are produced in the ordinary course of nature, without being able, or at least attempting, to control or vary those changes. Thus the early astronomers observed the motions of the sun, moon and planets among the fixed stars, and gradually detected many of the laws or periodical returns of those bodies. Thus it is that the eteorologist observes the ever-changing weather, and notes the height of the barometer, the temperature and oistness of the air, the direction and force of the wind, the height and character of the clouds, without being in the least able to govern any of these facts. The geologist again is genenerally a simple observer when he investigates the nature and position of rocks. The zoologist, the botanist, and the ineralogist usually employ mere observation when they examine animals, plants, and minerals, as they are et with in their natural condition.

In e eriment, on the contrary, we vary at our will the combinations of things and circumstances, and then observe the result. It is thus that the chemist discovers the composition of water by using an electric current to separate its two constituents, oxygen d hydrogen. The mineralogist may e ploy experiment when he melts two or three substances together to ascertain how a particular mineral ay have been produced. Even the botanist and zoologist are not confined to passive observation; for by re oving animals or plants to different cli ates and different soils, and by what is called domestication, they ay try how far the natural forms and species are capable of alteration.

It is obvious that experiment is the most potent and direct ode of obtaining facts where it can be applied. We ight have to wait years or centuries to meet accidentally with facts which we can readily produce at any

o ent in a laboratory; and it is probable that most of the che ical substances now known, and many excessively useful products, would never have been discovered at all by waiting till nature presented them spontaneously to our observation. Many forces and changes too ay go on in nature constantly, but in so slight a degree to escape our senses, d render so e experimental e s necessary for their detection. Electricity doubtless opetes in every particle of matter, perhaps at every

ment of ti e; and even the ancients could not but notice its action in the loadstone, in lightning, in the Aurora orealis, or in a piece of rubbed amber (electrum). But in li htnin electricity was too intense and dangerous; in the other cases it was too feeble to be properly understood. The science of electricity and magnetism could

only advance by getting regular supplies of electricity fro the common electric achine or the galvanic battery, and by making powerful electroagnets. Most if not all the effects which electricity produces must go on in nature, but altogether too obscurely for observation.

Experiment, again, is rendered indispensable by the fact that on the surface of the earth we usually meet substances under certain unifor conditions, so that we could never learn by observation what would be the nature of such substances under other conditions. Thus carbonic acid is only met in the form of a gas, proceeding from the combustion of carbon; but when exposed to extreme pressure and cold, it is condensed into a liquid, and may even be converted into a snow-like solid substance. Many other gases have in like manner been liquefied or solidified; and there is reason to believe that every substance is capable of taking all the three forms of solid, liquid and gas, if only the conditions of temperature and pressure can be sufficiently varied. Mere observation of nature would have led us, on the contrary, to suppose that nearly all substances were fixed in one condition only, and could not be converted from solid into liquid and from liquid into gas.

It must not be supposed however that we can draw any precise line between observation and experiment, and say where the one ends and the other begins. The difference is rather one of degree than of kind; and all we can say is that the more we vary the conditions artificially the more we employ experiment. I have said that meteorology is a science of *nearly* pure observation, but if we purposely ascend mountains to observe the rarefaction and cooling of the atmosphere by elevation, or if we ake balloon ascents for the same purpose, like Gay Lussac and Glaisher, we so vary the mode of observation as al ost to render it experimental. Astrono ers a ain

ay almost be said to experiment instead of merely observing when they simultaneously employ instruments f: to the north, and as far to the south, upon the earth's surface possible, in order to observe the apparent difference of place of Venus when crossing the sun in a transit, so thus to compare the distances of Venus and the sun with the dimensions of the earth.

Sir John Herschel has excellently described the difference in question in his Discourse on the Study of Natural Philosophy*. "Essentially they are much alike, and differ rather in degree than in kind; so that perhaps the terms passive and active observation might better express their distinction; but it is, nevertheless, highly important to mark the different states of mind in inquiries carried on by their respective aids, as well as their different effects in promoting the progress of science. In the former, we sit still and listen to a tale, told us, perhaps obscurely, piecemeal, and at long intervals of time, with our attention more or less awake. It is only by after rumination that we gather its full import; and often, when the opportunity is gone by, we have to regret that our attention was not more particularly directed to some point which, at the time, appeared of little moment, but of which we at length appreciate the importance. latter, on the other hand, we cross-examine our witness, and by comparing one part of his evidence with the other. while he is yet before us, and reasoning upon it in his presence, are enabled to put pointed and searching questions, the answer to which may at once enable us to make up our minds. Accordingly it has been found invariably, that in those departments of physics where the phenoe beyond our control, or into which experimental

ena e beyond our control, or into which experimental enquiry, from other causes, has not been carried, the pro-

ress of knowledge has been slow, uncertain and irregu; while in such as admit of experiment, and in which ankind have agreed to its adoption, it has been rapid, sure, and steady."

Not uncommonly, however, nature has, so to speak, ade experiments upon a scale and for a duration with which we cannot possibly compete. Thus we do not need to try the soil and situation which suits any given plant best: we have but to look about and notice the habitat or situation in which it is naturally found in the most flourishing condition, and that, we av be sure, indicates the result of ages of natural experiment. The distances of the fixed stars would probably have been for ever unknown to us did not the earth by describing an orbit with a diameter of 182,000,000 miles make a sort of experimental base for observation, so that we can see the stars in very slightly altered positions, and thus judge their distances compared with the earth's orbit*. Eclipses, transits, occultations and remarkable conjunctures of the planets, are also kinds of natural experiments which have often been recorded in early times, and thus afford data of the utmost value.

Logic can give little or no aid in making an acute or accurate observer. There are no definite rules which can be laid down upon the subject. To observe well is an art which can only be acquired by practice and training; and it is one of the greatest advantages of the pursuit of the Natural Sciences that the faculty of clear and steady observation is thereby cultivated. Logic can however give us this caution, which has been well pointed out by Mr Mill—to discriminate accurately between what we really do observe and what we only infer from the facts observed. So long as we only record and describe what our senses

^{*} See Lockyer's Elementary Lessons in Astronomy, Nos. LVI, XLVII.

have actually witnessed, we cannot co it an error; but the o ent we presu e or infer anythin we are liable to istake. For instance, we examine the sun's surface with a telescope and observe that it is intensely bright except where there are small breaks or circular openings in the surface with a dark interior. We are irresistibly led to the conclusion that the inside of the sun is colder and darker than the outside, and record as a fact that we saw the dark interior of the sun through certain openings in its luminous atmosphere. Such a record, however, would involve mistaken inference, for we saw nothing but dark spots, and we should not have done more in observation than record the shape, size, appearance and change of such spots. Whether they are dark clouds above the luminous surface, glimpses of the dark interior, or, as is now almost certainly inferred, something entirely different from either, can only be proved by a comparison of many unprejudiced observations.

The reader cannot too often bear in ind the caution against confusing facts observed with inferences fro those facts. It is not too much to say that nine-tenths of what we seem to see and hear is inferred, not really felt. Every sense possesses what are called acquired perceptions, that is, the power of judging unconsciously, by long experience, of many things which cannot be the objects of direct perception. The eye cannot see distance, yet we constantly imagine and say that we see things at such and such distances, unconscious that it is the result of judgment. As Mr Mill remarks, it is too much to say "I saw my brother." All I positively know is that I saw so e one who closely resembled my brother as far as could be observed. It is by judgment only I can assert he was y brother, and that judgment may possibly be wrong:

Nothing is ore important in observation and experi-

ment than to be uninfluenced by any prejudice or theory in correctly recording the facts observed and allowing to them their proper weight. He who does not do so will almost always be able to obtain facts in support of an opinion however erroneous. Thus the belief still exists with great force in the majority of uneducated persons, that the moon has great influence over the weather. changes of the moon, full, new and half oon, occur four times in every onth, and it is supposed that any change may influence the weather at least on the day preceding or following that of its occurrence. There will thus be twelve days out of every 28 on which any change of weather would be attributed to the moon, so that during the any changes will probably be thus recorded as favourable to the opinion. The uneducated observer is struck with these instances and remembers them carefully, but he fails to observe, or at least to remember, that changes of weather often occur also when there is no change of the moon at all. The question could only be decided by a long course of careful and unbiassed observation in which all facts favourable or unfavourable should be equally recorded. All observations which have been published negative the idea that there can be any such influence as the vulgar mind attributes to the moon.

But it would at the same time be an error to suppose that the best observer or experientalist is he who holds no previous opinions or theories on the subject he investigates. On the contrary, the great experimentalist is he who ever has a theory or even a crowd of theories or ideas upon his mind, but is always putting the to the test of experience and dismissin those which are false. The number of things which can be observed and experiented on e infinite, and if we merely set to work to record facts without any distinct purpose, our cords will have

no value. We must have some opinion or so e theory to direct our choice of experiments, and it is more probable that we hit upon the truth in this way than merely by haphazard. But the great requisite of the true philosopher is that he be perfectly unbiassed and abandon every opinion as soon as facts inconsistent with it are observed.

It has been well said by the celebrated Turgot, that "the first thing is to invent a system; the second thing is to be disgusted with it;" that is to say, we ought to have some idea of the truth we seek, but should imediately put it to a severe trial as if we were inclined to distrust and dislike it rather than be biassed in its favour. Few en probably have entertained more false theories than Kepler and Faraday; few men have discovered or established truths of greater certainty and importance. Faraday has himself said that—

"The world little knows how many of the thoughts and theories which have passed through the mind of a scientific investigator, have been crushed in silence and secrecy by his own severe criticism and adverse examination; that in the ost successful instances not a tenth of the suggestions, the hopes, the wishes, the preliminary conclusions have been realized *."

The student is strongly recommended to read Sir J. Herschel's *Preliminary Discourse on the Study of Natural Philosophy* (Lardner's *Cabinet Cyclopædia*), especially Part II. Chaps. 4 to 7, concerning Observation, Experi ent, and the Inductive Processes generally.

^{*} Modern Culture, edited by Youmans, p. 222. [Macmillan and Co.]

LESSON XXVIII.

METHODS OF INDUCTION.

WE have now to consider such methods as can be laid down for the purpose of guiding us in the search for general truths or laws of nature among the facts obtained by observation and experiment. Induction consists in inferring from particulars to generals, or detecting a general truth among its particular occurrences. But in physical science the truths to be discovered generally relate to the connection of cause and effect, and we usually call them laws of causation or natural laws. By the Cause of an event we mean the circumstances which must have preceded in order that the event should happen. Nor is it generally possible to say that an event has one single cause and no more. There are usually many different things, conditions or circumstances necessary to the production of an effect, and all of them must be considered causes or necessary parts of the cause. Thus the cause of the loud explosion in a gun is not simply the pulling of the trigger, which is only the last apparent cause or occasion of the explosion; the qualities of the powder; the proper form of the barrel; the existence of some resisting charge; the proper arrangement of the percussion cap and powder; the existence of a surrounding atmosphere, are among the circumstances necessary to the loud report of a gun: any of them being absent it would not have occurred.

The cause of the boiling of water again is not erely the application of heat up to a certain degree of temperature, but the possibility also of the escape of the vapour when it acquires a certain pressure. The freezing of water similarly does not depend merely upon the withdrawal of heat below the temperature of oo Centigrade. It is the work of Induction then to detect those circumstances which uniformly will produce any given effect; and as soon as these circumstances become known, we have a law or uniformity of nature of greater or less generality.

In this and the following Lessons I shall often have to use, in addition to cause and effect, the words antecedent and consequent, and the reader ought to notice their meanings. By an tecedent we mean any thing, condition, or circumstance which exists before or, it may be, at the same time with an event or phenomenon. By a consequent we mean any thing, or circumstance, event, or phenomenon, which is different from any of the antecedents and follows after their conjunction or putting together. It does not follow that an antecedent is a cause, because the effect might have happened without it. Thus the sun's light may be an antecedent to the burning of a house, but not the cause, because the house would burn equally well in the night. A necessary or indispensable antecedent is however identical with a cause, being that without which the effect would not take place.

The word pheno enon will also be often used. It means simply anything which appears, and is therefore observed by the senses; the derivation of the word fro the Greek word φαινόμενον, that which appears, exactly corresponds to its logical use.

The first ethod of Induction is that which Mr Mill has aptly called the ethod of a ee ent. It depends upon the rule that "If two or ore instances of the pheno enon under investi ation have only one circumstance in common, the circu stance in which alone all the in-

stances a ree, is the cause (or effect) of the given phenoenon." The meaning of this First C on of inductive inquiry ight, I think, be more briefly expressed by saying that the sole invariable antecedent of a phenomenon is probably its cause.

To apply this method we must collect as many instances of the phenomenon as possible, and compare together their antecedents. Among these the causes will lie, but if we notice that certain antecedents are present or absent without appearing to affect the result, we conclude that they cannot be necessary antecedents. Hence it is the one antecedent or group of antecedents always present, when the effect follows, that we consider the cause. For example, bright prismatic colours are seen on bubbles, on films of tar floating upon water, on thin plates of mica, as also on cracks in glass, or between two pieces of glass pressed together. On examining all such cases they seem to agree in nothing but the presence of a very thin layer or plate, and it appears to make no appreciable difference of what kind of matter, solid, liquid, or gaseous, the plate is made. Hence we conclude that such colours are caused erely by the thinness of the plates, and this conclusion is proved true by the theory of the interference of light. Sir David Brewster beautifully proved in a similar way that the colours seen upon Mother-of-pearl are not caused by the nature of the substance, but by the form of the surface. He took impressions of the Motherof-pearl in wax, and found that although the substance was entirely different the colours were exactly the s And it was afterwards found that if a plate of metal had arked by very fine close grooves, it would have iridescent colours like those of Mother-of-pearl. Hence it is evident that the form of the surface, which is the only invariable antecedent or condition requisite for the production of the colours, must be their cause. 16

The method of agreement is subject to a serious difficulty, called by Mr Mill the Plurality of Causes, consisting in the fact that the same effect may in different instances be owing to different causes. Thus if we inquire accurately into the cause of heat we find that it is produced by friction, by burning or combustion, by electricity, by pressure, &c.; so that it does not follow that if there happened to be one and the same thing present in all the cases we exa ined this would be the cause. The second method of induction which we will now consider is free from this difficulty, and is known as the ethod of D erence. It is stated in Mr Mill's Second C on as follows:—

"If an instance in which the phenomenon under investigation occurs, and an instance in which it does not occur, have every circu stance in common save one, that one occurring only in the for er; the circu stance in which alone the two instances differ, is the effect, or the cause, or an indispensable part of the cause, of the phenomenon."

In other words, we may say that the antecedent which is invariably present when the phenomenon follows, and invariably absent when it is absent, other circumstances re aining the same, is the cause of the phenomenon in those circumstances.

Thus we c clearly prove that friction is one cause of heat, because when two sticks are rubbed together they beco e heated; when not rubbed they do not become heated. Sir Humphry Davy showed that even two pieces of ice when bbed together in a vacuum produce heat, as shown by their elting, and thus co pletely de onstrated that the friction is the source and cause of the heat. We prove that air is the cause of sound being communicated to our ears by striking a bell in the rece ver of air-pu p, as Hawksbee first did in 1705, and

then observing that when the receiver is full of air we hear the bell; when it contains little or no air we do not hear the bell. We le n that sodiu or any of its co pounds produces a spectrum having a bright yello double line by noticing that there is no such line in the spectru of light when sodium is not present, but that if the smallest quantity of sodium be thrown into the flame or other source of light, the bright yellow line instantly appears. Oxygen is the cause of respiration d life, because if an animal be put into a jar full of atmospheric air, from which the oxygen has been withdrawn, it soon beco es suffocated.

This is essentially the great ethod of e eriment, d its utility mainly depends upon the precaution of only varying one circumstance at a time, all other circumstances being n intained just as they were. This is expressed in one of the rules for conducting experiments given by Thomson and Tait in their great treatise on Natural Philosophy, Vol. I. p. 307, as follows:—

"In all cases when a particular agent or cause is to be studied, experiments should be arranged in such a way as to lead if possible to results depending on it alone; or, if this cannot be done, they should be arranged so as to incre e the effects due to the cause to be studied till these so far exceed the unavoidable concomitants, that the latter ay be considered as only disturbing, not essentially odifying the effects of the principal agent."

It would be an imperfect and unsatisfactory experiment to take air of which the oxygen h been converted into carbonic acid by the burning of carbon, and argue that, because animal dies in such air, oxygen is the cause of respiration. Instead of merely withdrawing the oxy en we have a new substance, carbonic acid, present, which is quite capable of killing the ani al by its own poisonous properties. The i al in fact would be suffo-

16-2

cated even when a considerable proportion of oxy en re ained, so that the presence of the carbonic acid is a disturbing circumstance which confuses and vitiates the experiment.

It is possible to prove the existence, and even to measure the amount of the force of gravity, by delicately suspending a small ball about the size of a arble and then suddenly bringing a very heavy leaden ball weighing a ton or more close to it. The small ball will be attracted and set in motion; but the experiment would not be of the least value unless performed with the utmost precaution. It is obvious that the sudden motion of the large leaden ball would disturb the air, shake the room, cause currents in the air by its coldness or warmth, and even occasion electric attractions or repulsions; and these would probably disturb the small ball far ore than the force of gravitation.

Beautiful instances of experiment according to this ethod e to be found, as Sir John Herschel has pointed out, in the researches by which Dr Wells discovered the cause of dew. If on a clear calm night a sheet or other covering be stretched a foot or two above the earth, so

to screen the ground below from the open sky, dew will be found on the grass around the screen but not beneath it. As the temperature and moistness of the air, and other circu stances, are exactly the same, the open sky must be an indispensable antecedent to dew. The same experi ent is indeed tried for us by nature, for if we make observations of dew during two nights which differ in nothin but the absence of clouds in one d their presence in the other, we shall find that the cle open sky is requisite to the foundation of dew.

It ay often happen that we cannot apply the method of difference perfectly by varying only one circumstance at a time. Thus we cannot, generally speaking, try the

qualities of the same substance in the solid and liquid condition without any other change of circumstances, because it is necessary to alter the temperature of the substance in order to liquefy or solidify it. The te perature might thus be the cause of what we attribute to the liquid or solid condition. Under such circumstances we have to resort to what Mr Mill calls the joint ethod of a eeerence, which consists in a double application of the method of agreement, first to a number of instances where effect is produced, and secondly, to a number of quite different instances where the effect is not produced. It is clearly to be understood, however, that the negative instances differ in several circumstances from the positive ones; for if they differed only in one circumstance we might apply the simple method of difference. Icel d spar, for instance, has a curious power of rendering thin s seen through it apparently double. This phenomenon, called double refraction, also belongs to many other crystals; and we might at once prove it to be due to crystalline structure could we obtain any transparent substance crystallized and uncrystallized, but subject to no other alteration. We have, however, a pretty satisfactory proof by observing that uniform transparent uncrystallized substances agree in not possessing double refraction, and that crystalline substances, on the other hand, with certain exceptions which are easily explained, agree in possessing the power in question. The principle of the joint ethod may be stated in the following rule,

"If two or more instances in which the phenomenon occurs have only one circumstance in common, while two or more instances in which it does not occur have nothing in co on save the absence of that circumstance; the circu stance in which alone the two sets of instances (always or invariably) differ, is the effect, or the cause.

which is Mr Mill's Third C on :--

or indispensable part of the cause, of the phe enon."

I have inse ed the words in parentheses, as witho the the canon seems to me to express exactly the opposite of what Mr Mill intends.

It ay facilitate the exact co prehension of these i ductive ethods if I give the following symbolic representation of them in the manner adopted by Mr Mill. Let A, B, C, D, E, &c., be antecedents which ay be variously combined, and let a, b, c, d, e, &c., be effect following fro them. If then we can collect the following sets of antecedents and effects—

Consequents.
аbc
ade
afg
ahk

we ay apply the ethod of ee ent, d little doubt will re ain that A, the sole invariable antecedent, is the cause of a.

e e od of difference is sufficiently represented by

Antecedents. Consequents. ABC abc BC bc

Here while B and C re ain perfectly unaltered we find that the presence or absence of A occasions the presence or absence of a, of which it is therefore the cause, in the presence of B and C. But the reader and be caution and and is thinking that this proves A to be the cause of under all circ stances whatever.

jo t ethod of ee ent d e ce is si il 1-y resented by—

Antecedents.	Consequents.
ABC	abc
ADE	ade
AFG	afg
AHK	ahk
	•••
PQ	pq
RS	rs
TV	tv
XY	xy

Here the presence of A is followed as in the simple ethod of agreement by a; and the absence of A, in circuest ces differing from the previous ones, is followed by the absence of a. Hence there is a very high probability that A is the cause of a. But it will easily be seen that A is not the only circumstance in which the two sets of insteed cest differ, otherwise to any pair we might apply the simple ethod of difference. But the presence of A is a circuestance in which one set invariably, or uniformly, or always, differs, from the other set. This joint method is thus a substitute for the simpler method of difference in cases where that cannot be properly brought into action.

Herschel's Discourse, part II. chap. 6, p. 144. Mill's Syste of Logic, book III. chaps. 8 and 9.

LESSON XXIX.

ETHODS OF QUANTITATIVE INDUCTION.

T E ethods of Induction described in the l t Lesson related erely to the happening or not happenin of the event, the cause of which was sought. Thus we learnt that friction was one cause of heat by observin that two

solid bodies, even two pieces of ice, rubbed together, produced heat, but that when they were not rubbed there was no such production of heat. This, however, is a very ele entary sort of experiment; and in the progress of an investigation we always require to eas e the exact ou tity of an effect, if it be capable of being more or less, and connecting it with the quantity of the cause. There is in fact a natural course of progress through which we proceed in every such inquiry, as may be stated in the following series of questions.

- I. Does the antecedent invariably produce an effect?
- 2. In what direction is that effect?
- 3. How much is that effect in proportion to the cause?
- 4. Is it uniformly in that proportion?
- 5. If not, according to what law does it vary?

Take for instance the effect of heat in altering the dimensions of bodies. The first question is, whether the heating of a solid body, say a bar of iron, alters its length; the simple method of difference enables us to answer that it does. The next inquiry shows that almost all substances are lengthened or increased in dimensions by heat, but that a very few, such as india rubber, and water below 4.08° Cent., are decreased. We next ascertain the proportion of the change to each degree of temperature, which is called the coefficient of expansion. Thus iron expands 0.0000122 of its own length for every 1° Centigrade between 0° and 100°.

Still more minute inquiry shows, however, that the expansion is not uniformly proportional to temperature; most metals expand more and more rapidly the hotter they are, but the details of the subject need not be considered here.

The fixed stars, again, have often been mentioned in these Lessons, but the reader is probably aware that they are not really fixed. Taking any particular star, the LXIXX

249

astronomer has really to answer the several five questions stated below.

Firstly. Does the star move?

2ndly. In what direction does it move?

3rdly. How much does it move in a year or a century?

4thly. Does it move uniformly?

5thly. If not, according to what law does the motion vary in direction and rapidity?

Every sci ce and every question in science is first a atter of fact only, then a matter of quantity, and by degrees becomes more and more precisely quantitative. Thirty ye s ago most of the phenomena of electricity and electroagnetis were known merely as facts; now they can be for the most part exactly measured and calculated.

As soon as phenomena can thus be measured we can apply a further Method of Induction of a very iportant character. It is the ethod of Difference indeed applied under far ore favourable circumstances, where every degree and quantity of a phenomenon gives us a new experient and proof of connection between cause and effect. It may be called the ethod of Concomit to Variation, and is thus stated by Mr Mill, in what he entitles the Conformation:

"Whatever phenomenon varies in any manner whenever another phenomenon varies in some particular manner, is either a cause or an effect of that phenomenon, or is connected with it through some fact of causation."

Sir John Herschel's statement of the same method is as follows:—"Increase or diminution of the effect, with the increased or di inished intensity of the cause, in cases which admit of increase and diminution," to which he adds, "Reversal of the effect with that of the cause."

The illustrations of this method are infinitely numerous. Thus Mr Joule, of Manchester, conclusively proved that friction is a cause of heat by expending exact

quantities of force in rubbing one substance a ainst another, and showed that the heat produced was exactly greater or less in proportion as the force was greater or less. We can apply the method to many cases which had previously been treated by the simple method of difference; thus instead of striking a bell in a complete vacuum we can strike it with a very little air in the receiver of the air-pump, and we then hear a very faint sound, which increases or decre es every time we increase or decre e the density of the air. This experient conclusively satisfies any person that air is the cause of the transmission of sound.

It is this method which often enables us to detect the aterial connection which exists between two bodies. For a long time it had been doubtful whether the red flames seen in total eclipses of the sun belonged to the sun or the moon; but durin the 1 t eclipse of the sun it was noticed that the flames oved ith the sun, and were gradually covered and uncovered by the moon at

successive instants of the eclipse. No one could doubt thenceforth that they belonged to the sun.

Whenever, again, phenomena go through Perio c es, alternately increasing and decreasing, we should seek for other phenomena which go through changes in exactly the same periods, and there will probably be a connection of cause and effect. It is thus that the tides are proved to be due to the attraction of the moon and sun, because the periods of high and low, spring and neap tides, succeed each other in intervals corresponding to the apparent revolutions of those bodies round the earth. The fact that the moon revolves upon its own is in exactly the s e period that it revolves round the earth, so that for unkno ages p t the sa e side of the oon h always been turned towards the earth, is a ost perfect c e of conco itant variations, conclusively prov-

ing that the earth's attraction governs the otions of the oon on its own is.

The most extraordinary case of variations however consists the connection which has of late years been shown to exist between the Aurora Borealis, agnetic storms, and the spots on the sun. It has only in the 1 t 30 or 40 years become known that the magnetic co p s needle is subject at intervals to very slight but curious ovements; and that at the same time there are usually natural currents of electricity produced in telegraph-wires so as to interfere with the transmission of essages. These disturbances are known as magnetic storms,

e often observed to occur when a fine display of the Northern or Southern Lights is taking place in so e part of the earth. Observations during many years have shown that these storms come to their worst at the end of every eleven years, the mum taking place about the present year 1870, and then diminish in intensity until the next period of eleven years h passed. Close observations of the sun during 30 or 40 years have shown that d number of the dark spots, which are gigantic storms going on upon the sun's surface, increase and decre e exactly at the same periods of ti e netic storms upon the earth's surface. No one can doubt, then, that these strange pheno ena are connected together, though the mode of the connection is quite unknown. It is now believed that the planets Jupiter, Saturn, Venus and Mars, are the real causes of the disturb ces; for Balfour Stewart d Warren de la Rue have shown that exact correspondence exists between the otions of these planets d the periods of the sunspots. This is a ost remarkable and extensive case of conco it t variations.

We have now to consider a ethod of Induction which ust be e loyed when seve 1 causes act at once

heir effects are all blended together, producing a effect of the same kind as the separate effects. If e experiment friction, combustion, compression do it action are all going on at once, each of these is will produce quantities of heat which will be added her, and it will be difficult or impossible to say how it is due to each cause separately. We may call this e of the homogeneous intermixture of e ects, the name ating that the joint effect is of the same kind as sparate effects. It is distinguished by Mr Mill from

of the heterogeneous, or, as he says, the heteroic intermixture of effects, where the joint effect is
y different in kind from the separate effects. Thus
bend a bow too much it breaks instead of bending
er; if we warm ice it soon ceases to rise in temperaand melts; if we warm water it rises in temperageneously for a time but then suddenly ceases, and
ffect of a totally different kind, the production of
ir, or possibly an explosion, follows.

low when the joint effect is of a heterogeneous kind nethod of difference is sufficient to ascertain the cause occurrence. Whether a bow or a spring will break a given weight may easily be tried, and whether will boil at a given temperature in any given state barometer may also be easily ascertained. But in omogeneous intermixture of effects we have a more plicated task. There are several causes each prong a part of the effect, and we want to know how is due to each. In this case we ust employ a re Inductive Method, called by Mr Mill the ethod dues, and thus stated in his Fourth C on:—

Subduct fro any phenomenon such part as is known revious inductions to be the effect of certain teces, and the residue of the pheno enon is the effect of remaining antecedents."

XXIX.]

If we causes A b to B, i be a sir weight c and loac cart alor c thus due to t viously a which we the who tide the causes A to be care a to be considered.

Newt ent to in balls other, ar pared wi due part ance of t effect in swing was he was ended to the was ended be subtraction.

It is t
for the e
Few ther
ometer
perature
exactly 1
ercury
ought to
to ake
affected

If we know that the joint effect a, b, c is due to the causes A, B, and C, and can prove that a is due to A and b to B, it follows that c must be due to C. There cannot be a si pler case of this than ascertaining the exact weight of any commodity in a cart by weighing the cart and load, and then subtracting the tare or weight of the c t alone, which had been previously ascertained. We can thus too ascertain how much of the spring tides is due to the attraction of the sun, provided we have previously determined the height of the tide due to the moon, which will be about the average height of the tides during the whole lunar onth. Then subtracting the moon's tide the re ainder is the sun's tide.

Newton e ployed this method in a beautiful experient to dete ine the elasticity of substances by allowing balls ade of the substances to swing against each other, and then observing how far they rebounded copared with their original fall. But the loss of otion is due partly to i perfect elasticity and partly to the resistance of the air. He determined the amount of the latter effect in the simplest manner by allowing the balls to swing without striking each other, and observing how much each vibration was less than the last. In this way he was enabled easily to calculate the quantity that ust be subtracted for the resistance of the air.

It is this method that we employ in making allowance for the errors or necessary corrections in observations. Few thermometers are quite correct; but if we put a therometer into melting snow, which has exactly the te-

perature of 0° Centigrade, or 32° Fahr., we can observe exactly how much below or above the true point the mercury stands, and this will indicate how much we ought to add or subtract from readings of the thermometer to ake them correct. The height of the baro eter is affected by several causes besides the variation of the

pressure of the air. It is decreased by the capillary repulsion between the glass tube and the mercury; it is increased by the expansion of the ercury by heat, if the te perature be above 32° Fahr.; and it may be increed or decreased by any error in the length of the eure e ployed to determine the height. In an accurate observation all these effects are calculated and allowed for in the final result.

In chemical analysis this method is constantly e ployed to determine the proportional weight of substances which co bine together. Thus the composition of water is ascertained by taking a known weight of oxide of copper, passing hydrogen over it in a heated tube, and condensing the water produced in a tube containing sulphuric acid. If we subtract the original wei ht of the condensin tube from its final weight we learn how water is produced; the quantity of oxygen in it is found by subtractin the final weight of the oxide of copper fro its original weight. If we then subtract the wei ht of the oxy en fro that of the water we learn the weight of the hydrogen, which we have co bined with the oxygen. When the experiment is very carefully performed, as described in Dr Roscoe's Lessons in Elementary Chemistry, (p. 38), we find that 88.89 parts by weight of oxygen unite with II'II p ts of hydrogen to form 100 parts of water.

In all sciences which allow of measurement of quantities this method is employed, but more especially in trono y, the ost exact of all the sciences. Al ost all the causes and effects in astronomy have been found out

r ual pheno ena, that is, by calculating the effects of all known attractions upon a planet or satellite, d then observing how fi it is from the place thus predicted. When this was very carefully done in the case of U nus, it was still found that the planet w so eti es before and so eti behind its t e place. This residual effect

pointed to the existence of so e cause of attraction not then known, but which w in consequence soon discovered in the shape of the planet Neptune. The motions of several comets have in this way been calculated, but it is observed that they fail to return at the expected time. There is a discrep cy which points to the existence of so e obstructive power in the space passed through, the nature of which is not yet understood.

Mill's System of Logic, Book III. Chap. 10, Of the Plurality of Causes; and of the Intermixture of Effects.

LESSON XXX.

EMPIRICAL AND DEDUCTIVE METHODS.

WE have hitherto treated of Deduction and Induction if they were entirely separate and independent methods. In reality they are frequently blended or employed alternately in the pursuit of truth; and it may be said that all the more important and extensive investigations of science rely upon one as much as upon the other. It is probably the greatest merit in Mr Mill's logical writings that he points out the entire insufficiency of what is called the ethod to detect the ore obscure and difficult laws of nature. Bacon advised that we should always begin by collecting facts, classifying them according to their agreement and difference, and gradually gatherin from the laws of greater and greater generality. He protested altogether against "anticipating nature," that is, fo ing our own hypotheses d theories as to what the laws of nature probably e, and he see ed to think that an e ent of facts would take the lace of syste

all other methods. The reader will soon see that the progress of Science has not confirmed his opinions.

When a law of nature is ascertained purely by induction from certain observations or experiments, and has no other guarantee for its truth, it is said to be an e pirical law. As Mr Mill says, "Scientific inquirers give the name of Empirical Laws to uniformities which observation or experiment has shown to exist, but on which they hesitate to rely in cases varying much from those which have been actually observed, for want of seeing any reason why such a law should exist." The name is derived from the Greek word ἐμπειρία, meaning experience or trial. stances of such laws are abundant. We learn empirically that a certain strong yellow colour at sunset, or an unusual clearness in the air, portends rain; that a quick pulse indicates fever; that horned animals are always ruminants; that quinine affects beneficially the nervous system and the health of the body generally; that strychnine has a terrible effect of the opposite nature: all these are known to be true by repeated observation, but we can give no other re on for their being true, that is, we cannot bring them into harmony with any other scientific facts; nor could we at all have deduced them or anticipated them on the ground of previous knowledge. connection between the sun's spots, magnetic storms, auroras, and the motions of the planets mentioned in the last Lesson, is perhaps the most remarkable known instance of an empirical induction; for no hint has yet been given of the way in which these a netic influences are exerted throughout the vast di ensions of the planetary system. The qualities of the several alloys of metals

e also good instances of empirical knowledge. tell before m ing two or three metals for the first ti e any given proportions what the qualities of the ixture will be-that brass should be both harder

and more ductile than either of its constituents, copper and zinc; that copper alloyed with the very soft metal tin should make hard and sonorous bell-metal; that a certain mixture of lead, bismuth, tin and cadmium, should elt with a temperature (65° cent.) far below that of boiling water*.

However useful may be empirical knowledge, it is yet of slight importance compared with the well-connected and perfectly explained body of knowledge which constitutes an advanced and deductive science. fact in proportion as a science becomes deductive, and enables us to grasp more and more apparently unconnected facts under the same law, that it becomes perfect. He who knows exactly why a thing happens, will also know exactly in what cases it will happen, and what difference in the circumstances will prevent the event fro happening. Take for instance the simple effect of hot water in cracking glass. This is usually learnt empirically. Most people have a confused idea that hot water has a natural and inevitable tendency to break glass, and that thin glass, being more fragile than other glass, will be more easily broken by hot water. Physical science, however, gives a very clear reason for the effect, by showing that it is only one case of the general tendency of heat to expand substances. The crack is caused by the successful effort of the heated glass to expand in spite of the colder glass with which it is connected. But then we shall see at once that the same will not be true of thin glass vessels; the heat will pass so quickly throu h that the glass will be nearly equally heated; d accordingly chemists habitually use thin uniform glass vessels to hold or boil hot liquids without fear of the fractures which would be sure to take place in thick glass vessels or bottles.

The history of science would show conclusively that

^{*} Roscoe's Lessons in Elementary Ch istry.

TLESS.

deduction was the clue to all the greatest discoveries. Newton, after Galileo the chief founder of experi ental philosophy, possessed beyond all question the greatest power of deductive thought which has ever been enjoyed by m. It is striking indeed to compare his results in optics with those in che istry or alchemy. It is not generally known that Newton w really an alchemist, and spent days and nights in constant experi ents in his laboratory, trying to discover the secret by which

etals could be transmuted into gold. But in these rese ches all w purely empirical, and he had no clue to guide hi to successful experiments. A few happy uesses given in his celebrated Queries are all the result of this labour. But in the science of Optics it was quite otherwise; here he gr ped general laws, and every experiment only led him to devise and anticipate the results of several others, each ore beautiful than the last. Thus he was enabled to establish beyond all doubt the foundations of the science of the Spectrum, now bearing such wonderful results. So e persons may suppose that Newton, living shortly after Bacon, adopted the aconian ethod, but I believe that there is no reference to Bacon in Newton's works; d it is certain that he did not

ploy the ethod of Bacon. The *Principia*, though containing constant appeals to experiment and observation, is nevertheless the result of a constant and sustained effort of deductive mather atical reasonin

What Mr Mill h called the eductive ethod, but which I think might be ore appropriately called the Co bined or Co plete ethod, consists in the alternate use of induction and deduction. It may be said to have thr steps. follows:—

- I. Direct Induction.
- 2. Deduction, or, as Mr Mill calls it, Ratiocination.
- 3. Verification.

The first process consists in such a rough d simple appeal to experience as may ive us a glimpse of the laws which operate, without being sufficient to establish their truth. Assuming them as provisionally true, we then proceed to argue to their effects in other cases, and a further appeal to experience either verifies or negatives the truth of the laws assumed. There are, in short, two appeals to experience connected by the intermediate use of reasoning. Newton, for instance, having passed a ray of sun-light through a glass prism found that it was spread out into a series of colours resembling those of the rainbow. He adopted the theory that white light was actually composed of a mixture of different coloured lights, which became separated in passing through the prism. He saw that if this were true, and he were to pass an isolated ray of the spectrum, for instance, the yellow ray, through a second prism, it ought not to be again broken up into different colours, but should remain vellow whatever was afterwards done with it. On trial he found this to be the case, and afterwards devised a succession of similar confirmatory experiments which verified his theory beyond all possible doubt.

It was no mere accident that led Pascal to have a barometer carried up to the top of the mountain Puy de Dôme in France. Galileo, indeed, became acquainted by accident with the fact that water will not rise in an ordinary pump more than 33 feet, and was thus led to assert that the limited weight of the atmosphere caused it to rise. Torricelli, reasoning from this theory, saw that mercury, which is fourteen times as heavy water, should not rise more than one-fourteenth part of the distance, or about 29 or 30 inches. The experiment being tried verified the theory. It was the genius of Pascal, however, which saw that the experi ent required to be varied in another way by carrying the ercurial baro e-

ter to the top of a ountain. If the weight of the atmosphere were really the cause of the suspension of the mercury, it ought to stand lower on the mountain than below, because only the higher parts of the atmosphere pressed upon the mountain. The success of the experiment copletely verified the original hypothesis. The progress of the experimental sciences mainly depends upon the ode in which one experiment thus leads to others, d disclos new facts, which would in all probability have never coeunder our notice had we confined ourselves to the purely Baconian ethod of collecting the facts first and performing induction afterwards.

The greatest result of the deductive ethod is no less than the theory of avitation, which akes a perfect instance of its procedure. In this case the preliminary induction consisted, we may suppose, in the celebrated fall of the apple, which occurred while Newton was sitting orchard during his retirement from London, on account of the Great Plague. The fall of the apple, we are told, led Newton to reflect that there must be a power tending to draw bodies towards the earth, and he asked himself the question why the moon did not on that account fall upon the earth. The Lancashire astronomer Horrocks suggested to his ind another fact, namely, that when a stone is whirled round attached to a string, it exerts a force upon the string, often called centrifugal force. Horrocks re arked that the planets in revolvin round the ust tend in a si ilar way to fly off fro the centre. Newton was acquainted with Horrocks' views, and was thus possibly led to suppose that the earth's attractive ht actly neutralise the oon's centrifu al force to a tain that satellite in constant tendency, so rotation.

ut it happened that the world w in possession of certain e cal laws conce in the motions of the pla-

nets, 'thout which Newton could scarcely have proceeded further. Kepler had passed a lifetime in observing the heavenly bodies, and forming hypotheses to explain their otions. In general his ideas were wild and unfounded, but the labours of a lifetime were rewarded in the establishment of the three laws which bear his name, and · describe the nature of the orbits traversed by the planets, and the relation between the size of such orbit and the time required by the planet to traverse it. Newton was able to show by geometrical reasoning that if one body revolved round another attracted towards it by a force decreasing as the square of the distance increases, it would necessarily describe an orbit of which Kepler's laws would be true, and which would therefore exactly resemble the orbits of the planets. Here was a partial verification of his theory by appeal to the results of experience. But several other philosophers had gone so far in the investigation of the subject. It is Newton's chief claim to ho nour, that he carried on his deductions and verifications until he attained complete demonstration. To do this it was necessary first of all to show that the moon actually does fall towards the earth just as rapidly a stone would if it were in the same circumstances. Using the best information then attainable as to the distance of the moon, Newton calculated that the moon falls through the space of 13 feet in one inute, but that a stone, if elevated so high, would fall through 15 feet. Most men would have considered this approach to coincidence of his theory, but Newton's love of certain truth rendered different even from most philosophers, and the discrepancy caused him to lay "aside at that time any further thoughts of this matter."

It w not till many years afterwards (probably 15 or 16) that Newton, hearing of some more exact data fro which he could calculate the distance of the moon,

was able to explain the discrepancy. His theory of gravitation was then verified so far as the moon was concerned: but this was to him only the beginning of a long course of deductive calculations, each ending in a verification. If the earth and moon attract each other, and also the sun and the earth, similarly there is no reason why the sun and moon should not attract each other. Newton. followed out the consequences of this inference, and showed that the moon would not move as if attracted by the earth only, but sometimes faster and sometimes slower. Comparisons with Flamsteed's observations of the moon showed that such was the case. Newton argued again. that as the waters of the ocean are not rigidly attached to the earth, they might attract the moon, and be attracted in return, independently of the rest of the earth. Certain daily motions would then be caused thereby exactly resembling the tides, and there were the tides to verify the fact. It was the almost superhuman power with which he traced out geometrically the consequences of his theory, and submitted them to repeated comparison with experience, which constitutes his preeminence over all philosophers.

What he began has been going on ever since. The places of the moon and planets are calculated for each day on the assumption of the absolute truth of Newton's law of gravitation. Every night their places are observed as far as possible at Greenwich or some other observatory; comparison of the observed with the predicted place is always in some degree erroneous, and if coincident would be so only by accident. The theory is never proved completely true, and never can be; but the more accurately the results of the theory are calculated, and the more perfect the instruments of the astronomer are rendered, the more close is the correspondence. Thus the rude observations of Kepler and the few slight facts which worked on New-

ton's mind, were the foundation of a theory which yielded indefinite eans of anticipating new facts, and by constant verification, as far as hum accuracy can go, has been placed beyond all reasonable doubt.

Were space available it might be shown that all other great theories have followed nearly the same course. The undulatory theory of sound was in fact almost verified hv Newton himself, though when he calculated from it the velocity of sound there was again a discrepancy, which only subsequent investigation could explain. This theory no doubt suggested the corresponding theory of light, which when followed out by Young, Fresnel, and others, always gave results which were ultimately in harmony with observation. It even enabled mathematicians to anticipate results which the most ardent i agination could hardly have guessed, and which mere haphazard experiment might never have revealed. Dalton's laws of equivalent proportions in chemistry, if not his atomic theory, were founded on experiments made with the simplest and rudest apparatus, but results deduced from are daily verified in the nicest processes of modern chemical analysis. The still ore modern theory of the Conservation of Energy, which had been vaguely anticipated by Bacon, Rumford, Montgolfier, Seguin, Mayer and possibly others, was by Mr Joule brought to the test of experimental verification in some of the most beautiful and decisive experiments which are on record. It will be long before scientific men shall have traced out all the consequences of this grand principle, but its correspondence with fact already places it far beyond doubt.

It will now be apparent, I think, that though ob rvation and induction must ever be the ground of all certain knowledge of nature, their unaided employment could never have led to the results of modern science. He who merely collects and digests facts will seldom acquire a co prehension of their laws. He who frames a theory and is content with his own deductions from it, like Descartes, 'll only surprise the world with his misused genius; but the best student of science is he who with a copious store of theories and fancies has the highest power of foreseeing their consequences, the greatest diligence in comparing them with undoubted facts, and the greatest candour in confessing the ninety-nine mistakes he has made in reaching the one true law of nature.

LESSON XXXI.

EXPLANATION, TENDENCY, HYPOTHESIS, THEORY, AND FACT.

In the preceding Lessons I have used several expressions of which the eaning has not been defined. It will now be convenient to exemplify the use of these terms, and to arrive as far possible at a clear understanding of their

proper meanings.

Explanation is literally the making plain or clear, so that there shall be nothing uneven or obscure to interpt our view. Scientific expl ation consists in harmonizing fact with fact, or fact with law, or law with law, av see them both to be cases of one uniform so that we law of causation. If we hear of a great earthquake in some part of the world and subsequently hear that a neighbouring volcano has broken out, we say that the earthquake is thus partially explained. The eruption shows that there were great forces operating beneath the earth's surface, and the earthquake is obviously an effect of such causes. The scratches which ay be plainly seen upon the surface of rocks in certain parts of Wales and Cu berland, are explained by the former existence of glacie in those ountains; the scratches exactly har onize

XXXI.] HYPOTHESIS, THEORY, AND FACT. 265

with the effects of glaciers now existing in Switzerland, Greenland, and elsewhere. These may be considered pl ations of fact by fact.

A fact may also be explained by a general law of nature, that is the cause and mode of its production be pointed out and shown to be the same as operates in many apparently different cases. Thus the cracking of glass by heat was explained (p. 257) as one result of the universal law that heat increases the di ensions of solid bodies. The trade-winds are explained one case of the eneral tendency of warm air to rise and be displaced by cold and dense air. The very same simple laws of heat echanics which cause a draught to flow up a chimney when there is a fire below, cause winds to blow fro each hemisphere towards the equator. At the same ti e the easterly direction from which the winds come is explained by the simplest laws of motion; for as the earth rotates from west to east, and moves uch more rapidly at the equator than nearer the poles, the air tends to preserve its slower rate of motion, and the earth near the equator moving under it occasions an apparent motion of the wind fro east to west.

There are, according to Mr Mill, three distinct ways in which one law may be explained by other laws, or brought into harmony with them.

The first is the c e where there are really two or ore separate causes in action, the results of which are combined or added together, homogeneously. As was before explained, no ogeneous intermixt e of effects (p. 252) means that the joint effect is simply the sum of the separate effects, and is of the same kind with them. Our l t exa ple of the trade-winds really comes under this case, for we find that there is one law or tendency which causes winds to blow from the arctic regions tow ds the equator, and a second tendency which causes them to blow

from east to west. These tendencies are combined together, and cause the trade-winds to blow from the North-East in the northern hemisphere, and from the South-East in the southern hemisphere. The law according to which the temperature of the air is governed in any part of the earth is a very complicated one, depending partly on the law by which the sun's heating power is governed, partly on the power of the earth to radiate the heat away into space, but even more perhaps on the effect of currents of air or water in bringing warmth or carrying it away. The path of a cannon-ball or other projectile is determined by the joint action of several laws; firstly, the simple law of motion, by which any moving body tends to move onward at an uniform rate in a straight line: secondly, the law of gravity, which continually deflects the body towards the earth's surface; thirdly, the resistance of the air, which tends to diminish its velocity.

The reader will perhaps have noticed the frequent use of the word tendency, and I have repeatedly spoken of a cause as tending to produce its effect. If the joint and homogeneous action of causes has been clearly explained. it will now be clear that a tendency means a cause which will produce an effect unless there be opposite causes. which, in combination with it, counteract and disguise that effect. Thus when we throw a stone into the air the attractive power of the earth tends to make it fall, but the upward otion we have impressed upon it disguises the result for a certain time. The interminable revolving otion of the moon round the earth is the result of two balanced tendencies, that towards the earth, and that to proceed onward in a straight line. The laws of motion and ravity are such that this balance must always be preserved; if the moon by any cause were brought nearer

to the earth its tendency to y off would be increased, and would exceed the effect of gravity until it had regained

XXXI.] HYPOTHESIS, THEORY, AND FACT. 267

its proper distance. A tendency then is a cause which may or may not be counteracted.

In the second case of explanation an effect is shown to be due, not to the supposed cause directly, but to an inte ediate effect of that cause. Instead of A being the cause of C, it is found that A is the cause of B, and B the cause of C, so that B constitutes an inte edia This explanation may seem to increase the complexity of the matter, but it really simplifies it; for the connection of A with B may be a case of a familiar and simple law, and so may that of B with C; whereas the law that A produces C may be purely empirical and apparently out of harmony with everything else. Thus in lightning it if electricity had the power of creating a loud explosion; but in reality electricity only produces heat, and it is the heat which occasions sound by suddenly expanding the air. Thus thunder comes into harmony with the sound of artillery, which is also occasioned by the sudden expansion of the heated gases emitted by the powder. When chlorine was discovered it was soon found to have a strong power of bleaching, and at the present day almost all bleaching is done by chlorine instead of the sun, as formerly. Inquiry showed however that it was not really the chlorine which destroyed colour, but that oxygen is the intermediate and active agent. Chlorine decomposes water, and taking the hydrogen leaves the oxygen in a state of great activity and ready to destroy the org ic colouring atter. Thus a number of facts are harmonized; we learn why dry chlorine does not bleach, and why there e several other substances which resemble chlorine in its bleaching power, for instance, ozone, peroxide of hydrogen, sulphurous acid, and a peculiar oxide of vanadium, lately discovered by Dr Roscoe. It would be impossible to understand the effect at all unless we knew that it is probably due to active oxygen or

ozone in all the cases, even in the old ethod of bleaching by exposure to the sun*.

The third and much more important case of explanation is where one law is shown to be a se of a ore gener law. As was explained in Lesson XXIV. we naturally discover the less general first, and gradually penetrate to the more simple but profound secrets of nature. It h often been found that scientific men were in possession of several well-known laws without perceiving the bond which connected them together. Men, for instance, had long known that all heavy bodies tended to fall towards the earth, and before the time of Newton it was known to Hooke, Huyghens, and others, that some force probably connected the earth with the sun and oon. It w Newton, however, who clearly brought these and any other facts under one general law, so that each fact or less eneral law throws light upon every other.

The science of Electricity now harmonizes a vast series of partial laws and facts between which it was a truly difficult task to discover any resemblance. chief properties of the magnet had been fairly known since the time of Gilbert, the physician of Queen Elizabeth; common frictional electricity was carefully studied by Otto von Guericke, Epinus, Coulomb, and others; Galvanism was elaborately investigated al ost as soon as Galvani and Volta discovered the fact that the chemical action of one substance on another ay produce electricity. In the early part of this century there were three distinct sciences, Magnetism, Electricity and Galvanism; now there is but one science. Oersted of Copenhagen gave in 1819 the first link between the , by pointin out that an electric current may cause moveents in a compass-needle. Ampère and Faraday worke

^{*} Watts' Dictionary of Chemistry, Vol. 1. p. 601.

out the complicated relations of the three sciences, comprehending the finally in a wider science, which may be called Electro- agnetism, or we may perhaps conveniently eneralize the name Electricity so as to comprehend all the phenomena connected with it.

A number of minor laws and detached facts are co prehended and explained in the theory now enerally accepted, that heat, electricity, light, and in fact all the phenomena of nature, are but anifestations in different forms of one same kind of energy. The total a ount of energy existing in the universe is held to be fixed and unalterable, like the quantity of matter; sometimes it is disguised by affecting only the insensible olecules: at other times it is seen to produce palpable mechanical effects, as in the fall of a stone, or the expansion of . Now it had been previously known, ever since the time of the Greeks, that a si ple lever, although greatly altering the character of force by making its action slower or fi ter, does not alter its amount, because the more intense the force the slower and more limited is its action. In odern times a similar truth was proved of every kind achine; and it was recognised that, apart fro friction, no kind of mechanis either creates or destroys energy. It had been independently recognised that electricity produced in the galvanic battery w exactly proportional to the amount of chemical action, and that almost one of the forces named could be converted into of the others. All such facts e now co prehended under one general theory, the details of which are being gradually rendered ore certain and accurate, but the ain principle of which is that a certain amount of ch ical energy is equal to a certain amount of heat, a ount of electricity, of che ical action, or even certain

The word hypoth is uch used in connection th

of uscular exertion.

the subject we are discussing, and its meaning must be considered. It is derived from the Greek words ύπό. under, and beaus, blacing, and is therefore exactly synonymous with the Latin word suppositio, a placing under. whence our common word supposition. It appears to mean in science the imagining of some thing, force or cause, which underlies the phenomena we are examining. and is the agent in their production without admitting of direct observation. In making an hypothesis we assert the existence of a cause on the ground of the effects observed, and the probability of its existence depends upon the number of diverse facts or partial laws that we are thus enabled to explain or reduce to harmony. To be of any value at all a hypothesis must harmonize at least two different facts. If we account for the effects of opium by saying with Molière that it possesses a dormitive power, or say that the magnet attracts because it has a magnetic power, every one can see that we gain nothing. We know neither more nor less about the dormitive or magnetic power than we do about opium or the magnet. But if we suppose the magnet to attract because it is occupied by circulating currents of electricity the hypothesis may seem a very improbable one, but is valid. because we thus draw a certain analogy between a magnet and a coil of wire conveying electricity. Such a coil of wire attracts other coils exactly in the way that one magnet attracts another; so that this hypothesis enables us to harmonize several different facts. The existence of intense heat in the interior of the earth is hypothetical in so far as regards the impossibility of actually seeing and measuring the heat directly, but it harmonizes so many facts derived from different sources that we can hardly doubt its existence. Thus the occurrence of hot springs and volcanoes are so e facts in its favour, though they might be explained on other grounds; the empirical law

that the heat increases as we sink mines in any part of the earth's surface is stronger evidence. The intensely heated condition of the sun and other stars is strongly confirmatory as showing that other bodies do exist in the supposed condition of the earth's interior. The cool state of the earth's surface is perfectly consistent with its comparatively small size and the known facts concerning the conduction and radiation of heat. the more we learn concerning the way in which the sun's heat is supplied by the fall of meteoric matter, the it is probable that the earth may have been intensely heated like the sun at some former time, although for an immense period it has been growing slowly colder. supposition coinciding with so many facts, laws, and other probable hypotheses, almost ceases to be hypothetical, and its high probability causes it to be regarded as a known fact.

Provided it is consistent with the laws of thought there is nothing that we may not have to accept as a probable hypothesis, however difficult it may be to conceive and understand. The force of gravity is hypothetical in so that we know it only by its effects upon the of bodies. Its decrease at a dist ce harmonizes exactly indeed with the way in which light, sound, electric or magnetic attractions, and in fact all influences which emanate from a point and spread through space, decr se; hence it is probable that the law of the inverse square is absolutely true. But in other respects gravity is strongly opposed to all our ideas. If sound could travel to the rapidly as in the earth's atmosphere it would require nearly fourteen years to reach its destination; were the sun and earth united by a solid continuous bar of iron, pull at one end would not be felt at the other until nearly three years had passed. Light indeed co es from the sun in rather more than eight minutes; but what

are we to think of the force of gravity, which appears to reach the sun in an instant—so short that no calculations have yet been able to detect any interval at all? In fact there seems some reason to suppose that gravity is felt instantaneously throughout the immeasurable regions of space.

The undulatory hypothesis of light presents features equally extraordinary and inconceivable. That light does consist of minute but excessively rapid vibrations of something occupying space, is almost certain, because of the great harmony which this hypothesis introduces into the exceedingly various and complicated pheno ena of light, and the explanation which it affords of the analogy of light to sound. It is difficult indeed to imagine that anything can oscillate so rapidly as to strike the retina of the eye 831,479,000,000,000 in one second, as must be the case with violet light according to this hypothesis. But this is nothing to the difficulty of i agining space to be filled with solid ether of extreme rigidity and elasticity, but which nevertheless offers no appreciable resistance to the passage through it of ordinary matter, and does not itself possess any gravity *. It has been asserted indeed that the retardation in the return of comets is due to friction against this ether, and Mr Balfour Stewart believes he has produced heat by friction of a metallic disc against the ether in a vacuum. Should these assertions prove to be true we have new facts in harmony with the theory of light, which would thereby become less hypothetical than before.

There is no difficulty now in perceiving the part which hypothesis plays in the deductive ethod of scientific investigation considered in the last lesson. The preli in y induction is replaced more or less co pletely by

^{*} See Sir John Herschel's Familiar Lectures, p. 315, &c.

imagining the existence of agents which we think adequate to produce the known effects in question. If it is our object to explain the causes of ebbing and flowing wells, which occur in many parts of the world, we cannot possibly proceed by first exploring the interior of the earth, until we can discover the source of a spring, and observe its circumstances. We are obliged to imagine cavities and channels of various forms, until we conceive such an apparatus as will, in accordance with known laws of hydrostatics, occasion the irregular flowing of water in the way observed. If we can show that cavities of a particular form will produce that effect, and can think of no other mode in which it could be produced, the hypothesis becomes established as almost a certain fact.

It is the sa e with any great hypothesis like that of the theory of light. We have no means of directly observing and measuring the qualities of the ether which is the

ediu of light. All we know about this ether at present is derived from the observed phenomena of light. Hence we are driven to invent something and endow it with qualities from which we may calculate, according to some of the principles of echanics, the effect to be expected: and findin that these effects may be made to h with those actually observed, we depend upon this coincidence to prove the existence of the ether. The truth of a hypothesis thus altogether depends upon subsequent verification and accordance with observed facts. invent hypotheses which cannot thus be verified, or to invent them and then neglect the verification, leads to no result at all, or to fallacy. But when the verification is careful and co plete no reproach can be brought against the employment of hypothesis. It becomes, perhaps, certain as any other mode of investigation, and is at any rate indispensable. There was, in fact, little truth or reason in Newton's celebrated protest a a t the e of hypothesis—"Hypotheses non fingo." The fact is that as his theory of gravitation rested upon the greatest and ost successful of hypotheses, so his views of the material nature of light and the causes of its peculiar phenomena involved a false hypothesis, which has long since been completely disproved.

The word theory has constantly been used in the last few lessons, and deserves some exa ination. It

comes fro the Greek θ pia, eaning contemplation, reflection or speculation; but this gives us little clue to its odern use. In reality the word is highly ambiguous, being so etimes used as equivalent to hypothesis, at equivalent to general law or truth. When other ti es people form theories concerning comets, the sun, the cause of earthquakes, &c., they i agine a great many things which may or may not exist; such theories ally co plicated hypotheses, and should be so called. In this sense there are two theories of electricity, one of which supposes the existence of a single fluid which accumulates in some places and h then a tendency to discharge itself tow ds places where there is a deficiency, just as water always tends to find its level; the other supposes the existence of two fluids which are co monly united, but when separated tend to rush back into union again. These so-called theories are really hypotheses, because we have no independent evidence of the existence of any fluid, and it is now almost certain that there is no such thin . The ato ic theory, again, is really a hypothesis suggested by Dalt to explain the remarkable laws which he detected in the proportions of che ical ele ents which co bine together. It is a valid hypothesis in so far it does really explain the fixedness of the quantities which co bine; but it is purely hypothetical as reg ds the shapes, properties or absolute agnitudes

of the at s. because we have no facts which it can har-

XXXI.] HYPOTHESIS, THEORY, AND FACT. 275

onise in these respects, and no apparent me s of gaining the .

In another and more proper sense theory is opposed to practice, just the general is opposed to the particular. The theory of gravitation means all the more general laws of motion and attraction on which Newton founded his system of the Universe. We may know what those laws are without being able to determine the place of a planet or make any practical use of them; the particular results must be calculated out by skilful astronomers before navigators, travellers or others can make practical use of them in the determination of the latitude or longitude. When we speak of the mathematical theory of sound, the lunar theory, the theory of the tides, the word is employed without any special reference to hypothesis, and is merely equivalent to general knowledge or science, implying the possession of a complete series of general and accurate laws, but in no way distinguishing them from accurate knowledge in general. When a word is really used in an equivocal manner like theory, it is not desirable to attempt to give it an accurate definition which would be imaginary and artificial.

The word fact is used very often in this in most books, and demands a few remarks. It is derived from factum, the past participle of facere, to do, and would thus mean something which is done, an act, or deed; but the meaning is evidently greatly extended by analogy. We usually oppose to each other fact and theory, but just as theory seems to have two ambiguous meanings, so I believe that fact is ambiguous. Someti es it me s what is certain and known by the evidence of the senses, as opposed to what is known only probably by hypothesis

d inference; at other times it is contrected to a general law, d is equivalent to a particular instance or case. A law of great enerality ay often be as certain and true,

especially in mathematics, as the particular facts coming under it, so that the contrast must in this case be that between the general and particular. We often use the word too in common life, as merely equivalent to truth; thus we might say, "It is a fact that the primary laws of thought are the foundation of reasoning." In short, as theory means ambiguously what is hypothetical, general, abstract or uncertain, so fact is equally ambiguous, and eans confusedly what is intuitively known, particular, concrete or certain.

Mill's System of Logic, Book III. Chapters 12, 13 and 14, Of Explanation, and Hypothesis.

LESSON XXXII.

CLASSIFICATION, AND ABSTRACTION.

In an earlier Lesson, upon the subject of the Predicables, we considered the doctrine of classification as it was treated by logicians many centuries ago. The progress of science, however, during the last two centuries has caused great attention to be given to the true principles on which we can arrange a great ultitude of diverse objects in order, and we have to consider what e the characteristics of a natural and perfect system of classification.

It ay be said, indeed, that the subject we are treating is coextensive the the science of logic. All thought, all re oning, so far it deals with general na es or general notions, ay be said to consist in classification. Every co on or eneral neisthen e of a class, devery name of a class is a co on na e. "Metal" is the name

of one class of substances so often used in our syllogistic ex ples; "Ele ent" of another class, of which the fo er class is part. Reasoning has been plausibly represented to consist in affirmin of the parts of a class whatever ay be affirmed of the whole. Every law of nature which we rive at enables us to classify together a n ber of facts, and it would hardly be too much to define logic as the theory of class cation.

Here we deal, however, with that more conscious and distinct arrangement of objects or notions, which is especially e ployed in the natural sciences, such Botany,

Zoology, Mineralogy d Palæontolo y.

The derivation of the word class is so ewhat curious. In ancient Rome it was the practice to su whole people together at certain periods, and this ceremony was known as a clāsis, from the Greek κλάσις, or κλήσις, derived from καλέω, to call together. Servius Tullius is said to have divided the people into six orders. according to the amount of tribute they could pay, these orders were not unnaturally called the classes of the people. Hence the name c e by degrees to be applied to any organized body of people, such an army; thence it was transferred to a fleet of vessels arshalled in a fixed order, and was finally extended by analogy to any. collection of objects carefully arranged. When, however, we now speak of the lower or higher cl ses of the people it is curious that we are restoring the word very ne ly to its original eaning.

Cl s cation may perhaps be best defined the arrangement of things, or our notions of the , according to their resemblances or identities. Every cl s should so be constituted as to contain objects exactly rese bling each other in certain definite qualities, which are stated in the definition of the class. The ore nu ous and extensive the resemblances which are thus indicated by

any syste of classes, the more perfect and useful must that system be considered.

Mr Mill thus describes his view of the meanin — "Cl sification is a contrivance for the best possible ordering of the ideas of objects in our minds; for causing the ide to accompany or succeed one another in such a way shall give us the greatest command over our knowledge already acquired, and lead most directly to the acquisition of more. The general problem of classification, in reference to these purposes, may be stated as follows: To provide that things shall be thought of in such groups, and those groups in such an order, as will best conduce to the remembrance, and to the ascertainment of their laws."

A collection of objects may generally be classified in an indefinite number of ways. Any quality which is possessed by some and not by others may be taken as the first

erence, and the groups thus distinguished may be subdivided in succession by any other qualities taken at will. Thus a library of books might be arranged, (1) according to their size, (2) according to the language in which they are written, (3) according to the alphabetic order of their authors' names, (4) according to their subjects; and in various other ways. In large libraries and in catalogues such modes of arrangement are adopted combined. Each different arrangement presents some peculiar convenience, and that mode must be selected which best meets the especial purpose of the library or catalogue. The population of a kingdom, again, may be classified in an almost endless number of ways with regard to different purposes or sciences. The population of the United Kingdom ay be divided according to their place of birth, English, Welsh, Scotch, Irish, colonial-born, and aliens. The ethnographer would divide the into Anglo-Saxons, Cymri, Gaels, Picts,

Scandinavians, &c. The statist arranges the according to age; to condition, as arried, unmarried, widowed, &c.; to state of body, as able, incapacitated, blind, imbecile. The political economist regards the innumerable trades which are carried on, and classifies them in a co plex manner. The lawyer a ain treats every one as a minor, an adult, a feme sole, a fe e couverte, a guardian, ward, trustee, felon, and so on.

In the natural world, again, we may make various cl sifications. Plants av be arranged according to the country from which they are derived; the kind of place or habitat in which they flourish; the time they live, as annual, biennial, perennial; their size, as herbs, shrubs, trees; their properties, as esculents, drugs, or poisons: all these are distinct from the classifications which the botanist devises to represent the natural affinities or relationships of plants. It is thus evident that in making a classification we have no one fixed method which can be ascertained by rule, but that an indefinite number of choices or alternatives are usually open to us. Logic cannot in such cases do uch; and it is really the work of the special sciences to investigate the character of the classification required. All that logic can do is to point out certain general requirements and principles.

The first requisite of a good classification is, that it shall be appropriate to the purpose in h d; that is to say, the points of resemblance selected to fo the leading classes shall be those of importance to the practical use of the cl sification. All those things ust be arranged together which require to be treated alike, and those things ust be separated which require to be treated separately. Thus a lawyer has no need to classify persons according to the counties of England they were born in, because the law is the same independently of counties; but so far as a Scotchman, a Manx man, or an alien, is

under different laws fro the English born man, we shall require to classify them apart. A gardener is quite right in classifying plants as annuals, biennials, perennials; as herbs, shrubs, trees; as evergreen and deciduous; or according to the soil, temperature and other circu stances which affect the , because these are points which ust guide him in treating so e differently from others.

Another and, in a scientific point of view, the most important requisite of a good classification, is that it sh eatest possible n ber of gener assertions to be made. This is the criterion, as stated by Dr Whewell, which distinguishes a natural fro an artificial system of classification, and we must carefully dwell upon its meaning. It will be apparent that a good classification is more than a mere orderly arrangement; it involves a process of induction which will bring to light all the more general relations which exist between the things classified. An arrangement of books will generally be artificial; the octavo volumes will not have any common character except being of an octavo size. An alphabetical arrangement of names again is exceedingly appropriate and convenient to any purposes, but is artificial because it allows of few or no general assertions. We cannot ake any general assertion whatever about persons because their names happen to begin with an A or a B, a P or a W. Even those who agree in bearing the n e Smith or Taylor or Robinson ight be sub itted to the inductive ethod of agreement without the discovery of any co on circu stance which could be stated in a general proposition or law. It is true that if we vestigated the antecedents of the Evanses and Joneses we should find the nearly all to be Welsh, and the Ca pbells to be Scotch, d those who bear a very peculiar name would often be found to d cend from common cestors. So far even an alphabetic arrangement embodies something

that is natural in it, and enables general assertions to be made. Hardly any arrangement can be made, in fact, which will not indicate some vestiges of important relations and resemblances; but what we want is a syste which will reveal all the most important general truths.

For this purpose we must select as the ground of union those characters which carry with the most other characters. In Lesson XII, we considered the propriu as a quality which belongs to the whole of a class without forming part of the definition of the class. Now we ought to frame the definition of a class that it may contain as few characters as possible, but that as many other characters, properties, or propria, as possible, shall be attributable to the things contained in the class. Every one can see, for instance, that animals form one great group of beings, which have many characters in com on, and that plants form another group. Animals have sensation, voluntary motion, consume carbonaceous food, and evolve carbonic acid, possess a stomach, and produce fat. Pl ts are devoid of sensation and voluntary motion. produce carbonaceous tissue, absorb carbonic acid, and evolve oxygen, possess no sto ach, and produce starch. At one time it ight have been thought that al ost any of the characters named was a sufficient ark of the group to which a being belonged. Whatever had a stomach, was an animal; whatever had not, was a plant; whatever produced starch or evolved oxygen w plant: whatever absorbed oxygen or produced fat w ani al. To the present day these state ents re ain generally true, so that we ay ake sertions in the form of the proposition U, that "all i als e all beings that evolve c bonic acid, d all plants e all beings that absorb carbonic acid." But in reality the exceptions are many, and incre ing research akes it continually more apparent that there is no definite line to be drawn between i al and vegetable life. This, of course, is not a failure of logical science, but a fact of reat signific ce concerning the things the selves.

In a classification of plants we eet again with deep and natural distinctions between the great classes called Exogens, Endogens, and Acrogens. The latter have no true sexual flowers and seeds, are formed almost wholly of cellular tissue, and have an epidermis without cuticular pores. The former two classes have common; they have true flowers, woody tissue and cuticular pores, and hence may be united into one wider class, Vasculares. But exogens and endogens are also most strongly distinguished. Exogens have a stem or trunk consisting of distinct bark, pith, and wood in concentric layers, leaves with reticular veins, seeds with two seed-leaves and a naked radicle; generally speaking, too. the parts of the flower are some multiple of two or five in number. Endogens, on the contrary, have no distinct bark, pith, and wood, no concentric layers, leaves with parallel veins, seeds with one seed-leaf, and a radicle not naked; they have, too, the parts of the flower generally a ultiple of three in number.

These are the very widest classes in what is called the natural syste of botanical a ge ent: but similar principles are observed in all its minor classes. continual efforts of botanists are directed to bringing the great multitudes of plants together in species, genera, orders, classes, and in various intermediate groups, so that the embers of each group shall have the greatest nu ber of points of utual resemblance and the fewest points of resemblance to me bers of other groups. Thus is best fulfilled the great purpose of classification, which reduces ultiplicity to unity, and enables us to infer of the other e be of a class hat we know of any one

e ber, provided we distinguish properly between those

qualities which e likely or are known to belong to the class, and those which are peculiar to the individual. is a necessary condition of correct classification, as remarked by Prof. Huxley, that the definition of a group shall hold exactly true of all e bers of the group, and not of the members of y other group. To carry out this condition in the natural sciences is, however, very difficult, because kinds of plants or animals are continually discovered which stand in an intermediate position between classes which would otherwise be well distinguished. Thus ferns much embarrass the fundamental division of pl ts, because though they have no true flowers, and in this and other respects agree with other acrogens, yet they have abundance of woody fibre, which would entitle them to rank with vasculares, the larger group of which exogens and endogens are the subdivisions.

It may be remarked that the progress of chemistry is rapidly rendering it a science of classification; and in fact the whole theory of chemical combination now depends on a correct grouping of elements and compounds. Roscoe in his Lessons in Elementary Chemistry enumerates no less than eleven classes of etals, each class having a number of properties in co mon. Thus the metals of the alkalies, namely, Potassium, Sodium, Cæsiu, Rubidium, Lithium, form a remarkably natural cl s. They are all soft, easily fusible, volatile at high temperatures; they co bine with great force with oxygen, decompose water at all temperatures, forming oxides which are very soluble in water, and beco e powerfully caustic alkaline bodies fro which water cannot be expelled by heat. Their c bonates are soluble in water, and each etal for s only one compound with chlorine.

The metals of the alkaline earths, Calciu, Strontium, and Barium, also form a very nat al class, distinguished by the fact that their c bonates are insoluble in pure

water, but soluble in water containing carbonic acid in solution. The gold class contains the r e or valuable metals Gold, Platinum, Palladium, Rhodium, Ruthenium, Iridiu, d Osmium, which are not acted on by nitric acid, and can only be dissolved by chlorine or the ixture of acids called aqua regia. The oxides can be reduced

or deoxidised by simply heating them.

Natural classifications give us the deepest rese blances and relations, and may lead us ultimately to a knowledge of the way in which the varieties of things are produced. They are, therefore, essential to a true science, and may almost be said to constitute the fra ework of the science. Yet it does not follow that they are appropriate for all purposes. When our purpose is merely to recognise the name of a chemical element, a plant or an animal, its character as defined in a natural system would give us little or no assistance. The chemist does not detect potassium by getting it into the state of etal, and trying whether it would decompose water. He erely observes ong all the compounds of potassiu . have the which. best arked and ost peculiar characters; thus a compound of potassiu, platinum, and chlorine is most distinctive or characteristic of the metal, and is generally eans of recognising it; but a fine violet used as a colour which potash gives to the flame of a lamp was also used as an indication of its presence long before the spectroscope was introduced to analyse such colours. An artificial classification of the elements is thus necessary to the detection of substances, and accordingly in any book on che ical analysis will be found arrangements of the elements accordin to characters of very minor import ce, but which are selected on account of the ease d certainty with which they can be observed.

In Bot y, again, the natural system of classification is form being well suited for determining the name of a

Plant, because the cl ses are often defined by the form of minute parts of the seed, the arrangement of the seedvessel, and other parts which it is usually difficult or sometimes impossible to examine. Accordingly botanists usually arrange their genera and species in the order of the natural system, but contrive a sort of key or artificial arrangement, in which the most simple and apparent characters, often called characteristics, are employed for the discrimination of the plants. The best arrange ent of this kind as regards British plants is to be found in Bentham's British Flora. In reality the celebrated Linn an arrangement of plants was intended by its author to serve in this way. Linnæus was too profound a philosopher to suppose that the numbers of stamens and pistils usually expressed the real relationships of plants. Many of his classes were really natural cl ses, but the stamens and pistils were selected as the general guide to the classes and orders, as bein very plain and evident marks.

Closely connected with the process of cl sification is that of abstraction. To abstract is to sepa te the qualities common to all individuals of a group fro the peculiarities of each individual. The notion "tri gle" is the result of abstraction so far as we can re on concerning trian les, without y regard to the particular size or shape of any one triangle. All c s cation imlies abst ction, for in fr ing and defining the class I must separate the common qualities from the peculiarities. When I abstract, too, I for a general conception. or one which, generally speaking, embraces many objects. If, indeed, the quality abstracted is a peculiar property of the class, or one which belongs to the whole and not to any other objects, I y not increase the extent of the notion, so that Mr Herbert Spencer is, perhaps, right in holdin that we c abstract without g eralizing. We

other curves.

often use this word generalization, and the process may be defined as inferring of a whole class what we know only of a part. Whenever we regard the qualities of a thing as not confined to that thing only but as extended to other objects; when, in fact, we consider a thing only as a ember of a class, we are said to generalize. If, after studying the properties of the circle, we proceed to those of the ellipse, parabola and hyperbola, it is soon found that the circle is only one case of a whole class of curves called the conic sections, corresponding to equations of the second degree; and I generalize when I regard cer-

tain of the properties of the circle as shared by many

Dr Whewell added to the superabundance of terms to express the same processes when he introduced the expression Colligation of facts. Whenever two things are found to have similar properties so as to be placed in the same class they may be said to be connected together. We connect together the places of a planet as it moves round the sun, when we conceive them as points upon a comon ellipse. Whenever we thus join together previously disconnected facts, by a suitable general notion or hypothesis, we are said to colligate them. Dr Whewell adds that the general conceptions employed must be (1) clear, and (2) appropriate; but it may well be questioned whether there is anything really different in these processes from the general process of natural classification which we have considered.

LESSON XXXIII.

REQUISITES OF A PHILOSOPHICAL LANGUAGE.

AMONG the subsidiary processes requisite to the successful prosecution of inductive reasoning must be placed the construction of a suitable language. It is in fact impossible to over-estimate the importance of an accurate and copious language in any science; and the study of things would be almost useless without names to denote those things and record our observations concerning them.

It is easily apparent, indeed, that language serves three distinct and almost independent purposes:—

- I. As a means of communication.
- 2. As a mechanical aid to thought.
- 3. As an instrument of record and reference.

In its first origin language was used chiefly if not exclusively for the first purpose. Savage tribes exist in great numbers at the present day who seem to accurulate no knowledge. We may even say that the lower ani als often possess some means of communication by sounds or natural signs which constitute language in the first sense, though they are incapable of reasoning by general notions.

Some philosophers have held that it is i possible to carry on reasonin without the use of language. The t e no inalist went so far as to say that there e no such thin s as eneral notions, and that general names therefore constitute all that is general in science d

reasoning. Though this is no doubt false (see p. 13), it must nevertheless be allowed that unless general ideas were fixed and represented by words, we could never attain to sustained thought such as we at present enjoy. The use of language in the second purpose is doubtless indispensable in a practical point of view, and reasoning may almost be considered identical with the correct use of words. When language is used solely to assist reasoning there is no need that the meaning of each word should be fixed; we ight use names, as the letters x, y, z, a, b, c, &c., are used in algebra to denote any quantity that happens to occur in a problem. All that is requisite is never to confuse the meaning attributed to a word in . one argument with the different meaning attributed in another argument. Algebra may, in fact, be said to consist of a language of a very perfect kind adapted to the second purpose only, and capable of leading a person to the solution of a problem in a symbolical or mechanical manner.

Language, as it is furnished to us ready ade by the habitual growth of centuries, is capable of fulfilling all three purposes, though by no means in a perfect anner. As words possess a more or less fixed customary meaning we can not only reason by their aid, but communicate our thoughts or record the ; and it is in this last respect we have now to treat the subject.

The multitude of facts required for the establish ent of a science could not be retained in the memory with sufficient accuracy. Hence an indispensable subsidiary of induction is the means of describing and recording our observations. Thus only can knowledge be accumulated, so that each observer shall start with the advantage of knowing what has been previously recorded and proved. It will be necess y then to consider the mode in which langua e serves for the registration of facts, and to investi-

ate the requisite qualities of a philosophical language suitable to the needs of science.

As an inst ent of record language ust evidently possess two principal requisites:

1. Precision or definiteness of eanin.

2. Co pleteness.

A name is worse than useless unless, when used to record a fact, it enables us to ascertain what was the nature of the fact recorded. Accuracy and precision is then a more important quality of language than abundance. The want of an appropriate word will seldo give rise to actual error and fallacy; it will erely oblige us to employ a circumlocutory phrase or else leave the fact unrecorded. But it is a self-evident convenience that whenever a thing, notion, or quality has often to be referred to there should be a name appropriated to the purpose, and there ought only to be one name. Let us consider in succession what must be the character of a precise and complete language.

ay not previously have struck the reader, but it is certainly true, that description is impossible without the assertion of resemblance between the fact described and some other fact. We can only describe a thing by giving it a name; but how can we learn the eaning of that name? If we describe the name by other n es we only have more names of which the meanings are required. ust ultimately learn the me ings, not from names but from things which bear those names. If anyone were ignorant of the meaning of blue he could not be infor ed but by reference to something that excited in hi the sensation of blueness, and had he been blind from birth he could not acquire any notion of what blueness was. There are indeed a nu ber of words so familiar to us fro childhood that we cannot tell when or how we learnt their e ings though it must have been by reference to things. But when we come to the more precise use of names we soon have to make fresh reference to physical objects. Then we should describe the several kinds of blue colour as sky-blue, ure-blue, indigo-blue. cobalt-blue; green colour we likewise distinguish as seagreen, olive-green, emerald-green, grass-green, &c. The shapes of leaves are described in Botany by such names as ovate, lanceolate, linear, pinnate, peltate, referring the mind respectively to an egg, a lance, a line, a feather. and a shield. In recording dimensions it is equally impossible to avoid comparison with the dimensions of other things. A yard or a foot has no meaning unless there be a definite standard yard or foot which fixes its meaning; and the reader is probably aware that when the physical standard of a length is once completely lost it can never be recovered. The word is nothing unless we somewhere have the thing to which it corresponds.

The first requisite of a p osophical language evidently is that "every general name must have a certain and knowable meaning." It need hardly be mentioned that singular or proper names, the names of distinct objects. ust likewise be known; but as such na es are merely arks imposed upon the things they do not need the same consideration. General names are a more difficult subject, because, as we have seen in Lesson v., they have a double meaning in denotation or extension, and connotation or intension. Of these two meanings the connotation is the one which must be fixed; the other cannot as a general rule be limited and defined. Had the na e planet been restricted to Jupiter, Saturn, Mars, Venus, and Mercury, the planets known before the invention of the telescope, we should have had to find a new name for those subsequently discovered, and should even then co mit the fault of calling by different names those things which are closely similar. But if by planet we mean any

round body revolving round the sun in an orbit of slight ellipticity, it will include all such bodies as may be discovered from ti e to time, of which ore than 100 are already known. Similarly locomotive engine is not merely the name of a number of engines now actually existing; for if so a new name must be needed every week as so e new engine is made or an old one destroyed. What is fixed in a general name is its connotation, or the qualities implied in the things bearing the name. We ought therefore as far as possible to define the meaning of every general name we use, not by naming the objects which it denotes, but the qualities, which it connotes. Having however considered the subject of definition in previous Lessons (XII. and XIII.), we need only inquire here how far it is desirable to employ words which are in current use in preference to newly invented terms.

The advantage of an old term is that it possesses force of meaning for all persons, and so far saves the necessity of learning the eaning of a strange technical expression. Every one knows what heat is, and the expression science of heat bears eaning to every person however unlearned. ut there is this objection against old terms to be noted, that they are almost always subject to a biguity; accordingly it will be found that the scientific man really uses the word heat differently fro other persons. All things ore or less hot in science, whereas in common life we could never say that ice was hot or contained heat. In fact heat eans ordinarily the excess of temperature above the ordinary me , and the notion is purely relative to that of cold. We also apply the word analogously to sensations of taste, as when we say pepper is hot, or even to purely ental pheno ena, as in a hot dispute, a hot te per, c. If to avoid these a biguities we invent a new ter, Caloric, we may give it any precision of eaning we like, but we raise one more obstacle to the

study of science, because there is one ore technical term to be learnt.

This difficulty is especially great in the science of political economy. We there deal with such fa iliar ideas as wealth, oney, value, currency, capital, labour, exchan e, but it is the very fa iliarity of the ideas which occasions the greatest difficulty, because different people attach different eanings to the words, and infinite logomachy (Greek λόγος, word; μάχη, battle), or disputes arising on erely verbal questions, is the result. Even if a writer carefully defines the e ing in which he uses those terms he c not obli e other persons to be definitions in mind. The other alternative of inventing wholly new terms is out of the question, it would undoubtedly render a work intolerable to ost readers. The only advice that can be given is to introduce a new term where it is likely to be readily accepted and to displace an old ambiguous term; but otherwise to endeavour to remove the ambiguity of the old ter by constantly keeping in view a precise definition of the intended meaning.

A complete philosophical language will be co posed of two distinct kinds of terms, which for respectively the descriptive terminology and the no enclature of the science.

A descriptive terminolo, as pointed out by Dr Whewell, must include all the terms required to describe exactly what has been observed concerning any object or phenomenon, in order that we may possess a per anent record of the observation. For every quality, shape, circu stance, degree or quantity there ust be an appropriate na e or mode of expression. Thus in recording the discovery of a new ineral we ou ht to be able to fix words its exact crystalline fo, its colour, its degree of hardness, its specific g vity, s ell d taste if any,

and any other qualities which ay possess i portance. Modern botany ose fro the efforts of Linn us to create a syste of te s by which every part and ch acter of a pl t c be accurately described. The language of bot v, as since i proved, presents the co plete inst ce of a scientific terminology. Geology suffers uch, as I apprehend, fro the difficulty of findaccurate te s; such names as trap, basalt, gneiss, ite, tuff, greenstone, trachyte, porphyry, lava, &c., are very vague, and there are no precise descriptive terms by which to define and distinguish them. Where a quality does not admit of degree or quantity it only requires a sin le name; otherwise we must find some mode of exact measure ent and expression. The invention of any instru ent for measuring a quality which has been before un easured is always an important step in science, and the construction of the thermometer by Fahrenheit and the pendulum clock by Huyghens were great eras in science.

On the other hand, each science requires a no enclat e or collection of names for the distinct objects or classes of objects treated in it. In mineralogy the names of separate minerals, such as hæmatite, topaz, amphibole, epidote, blende, polybasite, form the no enclature; in che istry we have all the na es of the elements, together with a vast apparatus of na es for organic and other co pounds, such ethyl, acetyl, cyanogen, napthalin, benzol, &c. In astronomy the na es of the planets, satellites, nebul, constellations or individual st s. for a no enclature of by no e s a perfect or convenient d geology h si ilarly a no enclature neceskind: s ily of an inco plete character, in the n es of the successive for ations, silurian, devonian, c boniferous, permian, triassic, eocene, iocene, pliocene, post-pliocene. &c.

It is evident that a no clat e must possess names

of various degrees of generality, including individual objects if they need separate record, infi a species if such there be, with der cl ses, up to the su ma genera, or widest notions e braced in the science. In astronomy we deal chiefly with the names of individual objects, and there is as yet but little scope for classification. In such natural sciences as botany or zoology there is seldom or never any need of names for individuals, as an indefinite multitude of individuals generally rese ble each other very closely in a great number of properties, so as to constitute what has been called a natural kind. Mr Mill uses this ter to denote "one of those classes which are distinguished fro all others, not by one or a few definite properties, but by an unknown multitude of the ; the combination of properties on which the class is grounded being a ere index to an indefinite number of other distinctive attributes."

According to Mr Mill's language he see s to include in a nomenclature only the names of supposed species: for he says :- "A no enclature ay be defined, the collection of names of all kinds with which any branch of knowledge is conversant; or more properly, of all the lowest kinds, or infimæ species, those which may be subdivided indeed, but not into kinds, and which generally accord with what in natural history are ter ed simply species." But the fact is that naturalists have now abandoned the notion that the species is any definite form; many species are divided already into subspecies and varieties, or even varieties of varieties; and according to the principles of Darwin's theory the subdivision might go on indefinitely. It is surely ost reasonable to regard the natural kin doms of vegetables and animals indefinite series of classes and subcl ses. ed in d all the names attachin to y such classes belong to the nomenclature

Again. Mr Mill does not include in the nomenclature such general names as denote conceptions artificially formed in the course of induction and investigation. Accordingly, besides a terminology suited for describing with precision the individual facts observed, there is a branch of language containing "a name for every co mon property of any i portance or interest, which we detect by comparing those facts: including (as the concretes corresponding to those abstract terms) na es for the classes which we artificially construct in virtue of those properties, or as many of them, at least, as we have frequent occasion to predicate any thing of." As exa ples of this class of names he mentions Circle, Limit, Momentum, Civilization, Delegation, Representation. While the nomenclature contains the names of natural classes, this third branch of language would apparently contain the names of artificial ideas or classes.

But I feel great difficulty in giving a clear account of Mr Mill's views on this subject, and, as y object in these Lessons does not allow of the discussion of unsettled questions, I must conclude by referring the reader who desires to continue the subject, to the 4th and 6th chapters of the 4th Book of Mr Mill's System of Logic, which treat of the Requisites of a Philosophical Language.

See Dr Whewell's "Aphorisms concerning the Language of Science," at the end of his *Philosophy of the Inductive Sciences*.

Thomson's Outline of the Laws of Thought, contains most interesting remarks on the general nature and use of Language, §§ 17—31.

QUESTIONS AND EXERCISES.

LESSON I .- Introduction.

I. What e the eanings of a Law of Nature, and a Law of Thought?

2. Explain the distinction between the For of

Thought, and the Matter of Thought.

3. In what sense ay Logic be called the Science of

Sciences?

4. What is the derivation of the na e Logic?

- 5. How does a Science differ from an Art, and why is

 Lo ic ore in the form of a Science than an

 Art?
- 6. Can we say that Logic is a nec sary aid in correct reasoning, when persons who have never studied logic reason correctly?

LESSON II.—Three Parts of Logic.

1. Name the parts of which a syllogism is co posed.

How far is it correct to say that Logic is concerned with language?

3. What are the three acts of ind considered in Logic? Which of them is ore especially the subject of the Science?

4. C you state exactly what is meant by a general

notion, idea, or conception?

5. How do the No inalists, Realists, d Conceptualists differ in their opinions as to the nature of a general notion?

6. What is the supposed fourth part of Logic?

LESSON III .- Terms.

- 1. Define a na e or ter .
- 2. What is a cate ore atic term?
- Explain the distinction between a collective and a general te .
- 4. Distinguish the collective d distributive use of the word all in the following:—
 - (1) Non o nis ori (i.e. I shall not all die).
 - (2) "All men find their own in all en's good, And all en join in noble brotherhood."

 Tennyson.
 - (3) Non omnia possumus omnes (i. e. we cannot all do all things).
 - 5. Which of the followin are abstract ter s?

 Act, ingratitude, ho e, hourly, homeliness, introduction, individuality, truth, true, trueness, yellow, yellowness, childhood, book, blue, intention, reason, rationality, reasonableness.
 - 6. Define a negative te, and mention the ark by which you may recognise it.
 - 7. Distinguish a privative from a negative ter, and find some instances of privative ter s.
 - 8. Describe the logical characters of the following ter s, with the precautions iven at p. 26.

Metropolis	Consciousness	Sect
ook	Lord Chancellor	Nation
Library	Vegetable Kingdom	Institution
Great Britain	Brilli	L' ht
Cæsar	Weight	Observation
Void	Se ation	Tongue
Gold	Cæ	Air
Prime Minister	С.	Mentor
Indig tibility	Application	A chy
Manchester	Individual	Retribution
Recollection	Volume	Solemnity

Insignificant	L guage	Understanding
Brilliant	Adornment	Geology
Independence	Agreement	Demeanour
Heaviness	Obliquity	Resemblance
Illustration	Motionless	Departure
Section	Henry VIII.	Nestor
Whiteness	Formal Logic	Alexander

LESSON IV.—Ambiguity of Terms.

- Define univocal terms, and suggest some terms which are perfectly univocal.
- 2. What are the other names by which equivocal ter s are often called?
- Distinguish the three kinds of ambiguous terms, and find instances of each.
- Distinguish the three causes by which the third and ost important class of ambiguous terms have been produced.
- 5. Explain the ambiguity of any of the following terms, referring each to its proper cause, and tracing out as far as possible the derivation of each separate meaning from the original meaning.

Bill	Minister	Subject	Letter
Table	Clerk	Object	Star
Term	Order	Earth	Pole
School	\mathbf{Wood}	Law	Reason
Air	Bull	Sensation	\mathbf{Bed}
Glass	Volume	Art	Bowl
Peer	Scale	Interest	\mathbf{End}
Se e	Feeling	Paper	Division
Ball	Kind	Bolt	Class

LESSON V.—Twofold meaning of Terms.

 Distinguish very carefully the meanings in extension and intension of the terms—

Quadruped, railway, human being, engine, mountain, Member of Parliament.

- 2. Enu erate the synony s or other names used instead of extension d intension.
- 3. According to what law is the quantity of extension connected with the quantity of intension? Show that the law holds true of the following series of terms—
 - (1) Iron, metal, ele ent, matter, substance.
 - (2) Matter, organized matter, animal, man.
 - (3) Ship, steamship, screw-steamship, iron screwsteamship, British iron screw steamship.
 - (4) Book, printed book, dictionary, Latin dictionary.
- Distinguish between the connotation and denotation of a term.
- Select from the list of terms under Lesson III., Question 8 (p. 297), such terms as are non-connotative according to Mr Mill's views.
- 6. Arrange the following te s in series as in question 3, placing each term of greater extension before a ter of less extension. Point out which are the terms of greatest and least intension in each series.

Emperor	Animal	Planet
Teacher	Dissenter	M malian
Baptist	Individual	Matter
Timber	Jupiter	Solicitor
Person	Ruler	Quadruped
Horse	Organized substance	Being
Heavenly body	Lawyer	Napoleon III.
Christian	Alex der	Episcopali

LESSON VI.-Growth of Language.

1. Trace out the generalization or specialization which has taken place in any of the following words:—

Kind, genus, class, species, order, rank, Au ustus, president, speaker, Utopia, rock, Com ons, doctor.

Point out etaphors derived from the notions of wei ht, strai htness, rock, wind.

3. Distinguish as accu tely as possible the eanings

of the followin synonyms:--

Sickness, alady; ud, ire; confutation, refutation; boundary, limit; ind, intellect; recollection, re iniscence; procrastination, dilatoriness; converse, reverse, obverse, inverse.

- 4. Form lists of all the words derived fro y of the following roots:—
 - (1) Tendere, to stretch, as in intention, attention.
 - (2) Ponere, to place, as in position, supposition.
 - (3) Genus, tribe or kind, as in genus, eneration.
 - (4) Munus, gift, in remuneration, common (Latin, Communis).
 - (5) Modus, shape or fashion, as in mood, moderate.
 - (6) Scribere, to write, as in scribe, inscription, describe.
 - (7) Capere to take, as in deception, incipient.

LESSON VII.—Leibnitz on Knowledge.

- I. What are the characters of perfect knowledge?
- Describe the character of the knowledge which we have of the followin notions or objects:—
 A syllogism.

Electricity.

Motion.

A tri gle.

Eternity.

The weight of the earth (5 52 trillions of tons). The colour of the sky.

Explain exactly what you mean by intuitive knowledge.

LESSON VIII .- Propositions.

 Define a proposition, and me the parts of which it is composed.

2. How are propositions classified?

Name the four kinds of categorical propositions, and their symbols.

4. Under which classes are s gular and indefinite

propositions placed?

Enumerate the most usual signs of the quantity of a proposition.

6. What are modal propositions according to early logicians, and according to Thomson?

7. How far do logici s consider propositions with regard to their truth or falsity?

LESSON IX.—Opposition of Propositions.

 State the quantity of the subject and predicate in each of the propositions A, E, I, O.

 Select out of the following propositions, pairs of contrary, contradictory, subaltern, and subcontrary propositions:—

(1) So e ele ents are known.

(2) No ele ents are known.

(3) All ele ents are known.

(4) Not all ele ents are known.

(5) Some ele ents are not known.

(6) All elements are not known.

3. What propositions are true, false, or doubtful,

(1) when A is false, (3) when I is false, (2) when is false, (4) when O is false?

4. Prove by means of the contradictory propositions

- that subcontrary propositions c not both be false.
- 5. Show by means of the subcontrary propositions that contrary propositions ay both be false.
- 6. What quantity would you assign to each of the following propositions?
 - (I) Knowledge is power.
 - (2) Nebul are aterial bodies.
 - (3) Light is the vibration of an ether.
 - (4) Men e more to be trusted than we think.
 - (5) The Chinese are industrious.
- 7. Why is it desirable in controversy to refute a statement by its contradictory and not by its contrary?

LESSON X.—Conversion and Immediate Inference.

- I. Define inference and conversion.
- 2. What e converse and convertend propositions?
- 3. State the rules of valid conversion.
- 4. N e all the kinds of conversion.
- 5. By what process do we pass fro each of the following propositions to the next?
 - (I) No knowledge is useless.
 - (2) No useless thing is knowledge.
 - (3) All knowledge is not useless.
 - (4) All knowledge is useful.
 - (5) What is not useful is not knowled e.
 - (6) What is useless is not knowledge.
 - (7) No knowledge is useless.
- 6. Give the lo ical opposites of the following proposition, d the converse of its contradictory:—
 "He c not become rich who will not labour."
- 7. Apply negative conception to the proposition "All en are fallible;" then convert d show that the result is the contrapositive of the original.

- Cl sify the propositions subjoined to the four follow groups:
 - a. Those which can be inferred fro (1).
 - b. Those fro which (1) can be inferred.
 - c. Those which do not contradict (I), but cannot be ferred from it.
 - d. Those which contradict (1).
 - (1) All just acts are expedient acts.
 - (2) No expedient acts are unjust.
 - (3) No just acts e inexpedient.
 - (4) All inexpedient acts are unjust.
 - (5) Some unjust acts e inexpedient.
 - (6) No expedient acts are just.
 - (7) Some inexpedient acts are unjust.
 - (8) All expedient acts are just.
 - (o) No inexpedient acts are just.
 - (10) All unjust acts are inexpedient.
 - (11) So e inexpedient acts are just acts.
 - (12) So e expedient acts are just.
 - (13) So e just acts are expedient.
 - (14) So e unjust acts e expedient.

LESSONS VIII. IX. and X.—Examples of Propositions.

The reader is desired to ascertain the logical character of each of the following propositions; he is to state of each whether it is affirmative or negative, universal, particular, singular or indefinite, pure or odal, exclusive or exceptive, &c.; when irregularly stated he is to reduce the proposition to the simple logical order; he is then to convert the proposition, and to draw immediate inferences fro it by y process which ay be applicable.

- (1) All birds e feathered.
- (2) No reptiles e feathered.
- (3) Fixed st s e self-lu inous.

304 QUESTIONS AND EXERCISES.

(4) Perfect happiness is impossible.

(5) Life every man holds dear.

(6) Every mistake is not a proof of ignorance.

(7) Some of the most valuable books are seldom read.

(8) He jests at scars who never felt a wound.

(9) Heated etals are softened.

(10) Not one of the Greeks at Thermopyl escaped.

(11) Few are acquainted with themselves.

(12) Whoso loveth instruction loveth knowledge.

(13) Nothin is harmless that is mistaken for a virtue.

(14) Some of our muscles act without volition.

(15) Metals are all ood conductors of heat.

(16) Fame is no plant that grows on mortal soil.

(17) Only the brave deserve the fair.

(18) No one is free who doth not command himself.

(19) Nothing is beautiful except truth.

(20) The wicked shall fall by his own wickedness.

(21) Unsafe e all things unbecomin .

(22) There is no excellent beauty that hath not some strangeness in the proportion.

(23) It is a poor centre of a man's actions, hi self.

(24) Mercy but murders, pardoning those that kill.

(25) I shall not all die. (Non omnis moriar.)
(26) A regiment consists of two battalions.

(27) 'Tis cruelty to load a falling an.

(28) Every istake is not culpable.

(29) Quadrupeds are vertebrate animals.

(30) Not any of the metals are brittle.

(31) Many are the deservin en who are unfortunate.

(32) Amalgams are alloys of mercury.

(33) One kind of metal at le t is liquid.

(34) Talents are often misused.

(35) Some parallelogr s have their adjoining sides equal.

(36) Britain is island.

(37) Romulus and Re us were twins.

(3) A an's a

(39) Heaven is all ercy.

(40) Every one is a good jud e of his own interests.

(41) All parallelograms have their opposite angles equal.

(42) Fa iliarity breeds conte pt.

(43) No one is always happy. (44) Many a little makes a mickle.

LESSON XI.—Logical Analysis of Sentences.

I. How does the grammatical predicate differ from the

logical predicate?

2. Distinguish between a compound and a co plex sentence; and between coordinate and subordinate propositions.

3. En erate the gram atical expressions which

fο

(1) A subject.

(4) An object.

(2) An attribute. (3) A predicate.

(5) An adverbial.

4. Examine the following sentences, ascertain which are compound or complex, d point out the coordinate or subordinate propositions.

(1) Happy is the man that findeth wisdo, d the

that getteth understanding.

otion, c be converted into (2) Heat, being chanical force.

(3) Ceres, Pallas, Juno, and Vesta e inor planets, or asteroids.

(4) Knowled e co es, but wisdom lingers.

(5) Fortune often sells to the h ty what she gives to those who wait.

Thous ds at His bidding speed, (6) And post o' 1 d doce thout rest: They also serve who only stand and w 't.

306

(7) Pride that dines on vanity, sups on contempt.

(8) Nobody can be healthful without exercise, neither natural body, nor politic.

(9) Nature is often hidden, so eti es overco e, seldo extinguished.

(10) It is i possible to love d be wise.

(II) Though ods they were, as en they died.

(12) He that is not industrious envieth him that is.

(13) Ye are y friends, if ye do whatsoever I co and you.—John xv. 14.

(14) The 'sdo that is from above is first pure, then peaceable, gentle, and easy to be intreated, full of ercy, d good fruits, without partiality, and without hypocrisy.—James iii. 17.

5. Analyse in the form of a sche e or diagram any of

the follow sentences:—

(I) The first aphoris of Bacon's Novum Organum, on p. 220.

(2) So e judg ents are merely explanatory of their subject, having for their predicate, a conception which it fairly i plies, to all who know d can define its nature.

(3) There be none of the affections which have been noted to fascinate or bewitch, but love and envy: they both have vehement wishes; they frame themselves readily into imaginations and sugg tions; d they co e easily into the eye, especially upon the presence of the objects, which e the points that conduce to fi cination, if y such there be.

Further ples for alysis ust be sought in Dal leish's Gra matical Analysis, ith Progressive Exerces. (Oliver and oyd.) Edinburgh, 1866. Price 9d.

LESSON XII.—The Predicables, etc.

- r. Define each of the five predicables.
- 2. In what sense ay we say that the genus is p t of the species, and in what sense that the species is part of the enus?

Select fro the te s in the 6th Question of Lesson v., p. 299, such as e enera, species, hi hest enera, or lowest species of other terms.

4. Explain the expressions sui generis, homo eneous, heterogeneous, sum u genus, infima species, tree of Porphyry.

 Na e a property and accident of each of the following classes:—Circle, Planet, Bird, Member of Parliament, Ru inant Animal.

6. What are the rules of correct logical division.

7. The first name in each of the followin series of te s is that of a class which you e to divide and subdivide so as to include all the subjoined inor classes in accordance with the laws of division.

(I) People. (2) Triangle. (3) Reasoning. Induction (Imperfect) Equi gular Laity Deduction Isoscel Aliens Mediate Inference Right-angled Naturalized Induction Scalene Subjects Hypotheti 1 Syllogism Obtuse-angled Peers Disjunctive Syllogism Natural-born Subjects Clergy

Baronets
Commons
8. Divide y of the following classes:

B. Divide y of the following classes: —Govern ents, Sciences, Logical te s, Propositions.

9. Of what does a logical definition consist?

- 10. What are the les of correct definition?
- 11. What rules do the following definitions break?
 - (1) Life is the su of the vital functions.
 - (2) Genus is the aterial part of the species.
 - (3) Illative conversion is that in which the truth of the converse can be inferred from that of the convertend.
 - (4) Mineral substances are those which have not been produced by the powers of vegetable or animal life.
 - (5) An equilateral triangle is a triangle whose sides and angles are respectively equal.
 - (6) An acute-angled triangle is one which has an acute angle.

LESSON XIII.—Pascal and Descartes on Method.

- (1) What is the use of nominal definitions?
- (2) How must we e ploy definitions in order to avoid confusion?
- (3) How far can we be said to be free to use any name for any object?
- (4) What according to Pascal is the true method of avoiding error?
- (5) How do we learn the eanings of words which cannot be defined?
- (6) Give instances of words which can be clearly defined and of others which cannot.
- (7) State the five rules of ethod given in the Port Royal Logic.
- (8) Explain Descartes' rules for the attain ent of truth.

LESSON XIV.—Laws of Thought.

 tate the three Funda ental Laws of Thought, and apply them to the following notions:— (I) Matter, or anic, inorganic.

(2) Undulations, pol zed, non-pola ed.

(3) Figure, rectilinear, curvilinear.

2. Is it wrong to sert that ani al cannot both be vertebrate d invertebrate, seeing that so e ani als are vertebrate and some are not?

Select from the following such te s e negatives of the others, and such are opposites:
 Light, plenu , ain, heat, decrease, loss, darkness, cold, crease, vacuu

4. How is Aristotle's dictu applicable to the following arguments?

ing arguments:

 ilver is a good conductor of electricity; for such are all the etals.

(2) Co ets c not be 'thout weight; for they are co posed of matter, which is not without wei ht.

LESSON XV .- Syllogism: the Rules.

1. Distinguish ediate and i mediate inference.

2. Define syllo is , d state with what it is synonyous.

3. What are the s' principal and two subordinate

rules of the syllogis ?

- 4. In the followin syllogis s point out in succession the conclusion, the iddle term, the major te , the inor te , the major premise and the inor premise, observing this precise order.
 - (I) All en e fallible;
 All kings are en;
 Therefore all kin s e fallible.
 - (2) Platinu is a etal;

All etals co b e with oxy en; Therefore Platinu co bines with oxygen. 310

- (3) Hottentots are capable of education; for Hottentots e en, and all en e capable of education.
- Explain carefully what is eant by non-distribution of the middle term.

LESSON XVI.—The Moods and Figures of the Syllogism.

I. N e the rules of the syllogism which are broken by any of the following oods, no regard being paid to figure:—

AIA, EEI, IEA, IOI, IIA, AEI.

- Write out all the 64 oods of the syllogism and strike out the 53 invalid ones.
- Show in what figures the following pre ises give a valid conclusion:—AA, AI, EA, OA.
- 4. In what figures are IEO and EIO valid?
- To what moods do the following valid syllogisms belong? Arr ge the in correct logical order.
 - (1) Some Y's are Z's.
 No X's e Y's.
 Some Z's are not X's.
 (2) All Z's are Y's.
 No Y's are X's.
 No Z's are X's.
 - (3) No fish suckles its young; The whale suckles its young; Therefore the whale is no fish.
- Deduce conclusions fro the following premises.
 d state to what mood the syllogism belongs.
 - (1) Some amphibious ani als are mammalian.
 All mali animals are vertebrate.
 - (2) All pl ets are heavenly bodies. No pl ets e self-lu inous.
 - (3) Ma ali i als are quadrupeds.

 No birds e quad peds.
 - (4) R in t als e not predacious.

 The lion is predacious.

- Invent ex ples to show that false pre ises ay give true conclusions.
- 8. Supply pre ises to the following conclusions:
 - (1) So e logicians are not good reasoners.
 - (2) The rings of Saturn are aterial bodies.
 - (3) Party government exists in every democracy.
 - (4) All fixed stars obey the law of gravitation.

LESSON XVII.-The Syllogism; Reduction.

- I. State and explain the ne onic lines bara, Celarent, &c.
- Construct syllogisms in each of the following oods, taking X, Y, Z, for the ajor, iddle, d inor terms respectively, d show how to reduce the to the first figure:—
 - Cesare, Festino, Darapti, Datisi, Ferison, Ca enes, Fesapo.
- 3. What is the use of Reduction?
- 4. Prove that the following premises cannot give a universal conclusion—EI, IA, OA, IE.
- Prove that the third fi ure must have an affir ative inor pre ise, and a particular conclusion.
- Reduce the oods Cesare and Ca enes by the Indirect ethod, or Reductio ad Impossibile.

LESSON XVIII.—Irregular and Compound Syllogisms.

- Describe the eaning of each of the terms—Enthyme e, Prosyllogis , Episyllogism, Epicheirema, Sorites.
- Make an exa ple of a syllogis in which there are two prosyllogis s.
- Construct a sorites of four pre ises and resolve it into distinct syllogis s.
- 4. What are the rules to which a sorites must confo

- 5. The reader is requested to analyse the following ar uments, to detect those which are false, and to ascertain the rules of the syllogism which they break; if the argument appears valid he is to ascertain the figure and mood to which it belongs, to state it in correct logical form, and then if it be in an imperfect figure to prove it by reduction to the first figure. The first six of the examples should be arranged both in the extensive and intensive orders.
 - 1. None but ortals are men.

Monarchs are men.

Therefore monarchs are mortals.

2. Personal defor ity is an affliction of nature.

Disgrace is not an affliction of nature.

Therefore personal deformity is not disgrace.

- So e statesmen are also authors; for such are Mr Gladstone, Lord Derby, Lord Russell, and Sir G. C. Lewis.
- This explosion must have been occasioned by gunpowder; for nothing else would have possessed su cient force.
- Every an should be moderate; for excess will cause disease.
- lessed are the merciful; for they shall obtain ercy.
- As al ost all the organs of the body have a known use, the spleen ust have so e use.
- 8. Cogito, ergo su . (I think, therefore I exist.)
- So e speculative men are unworthy of trust; for they are unwise, and no unwise man can be trusted.
- 10. No idle person can be a successful writer of history; therefore Hu e, Macaulay, Hallam and Grote must have been industrious.

- Who spareth the rod, hateth his child; the parent who loveth his child therefore spareth not the rod.
- 12. Co ets ust consist of heavy matter; for otherwise they would not obey the law of gravitation.
- Lithium is an element; for it is an alkali-produc g substance, which is a metal, which is an el ent.
- 14. Rational beings are accountable for their actions; brutes not being rational, are therefore exe pt fro responsibility.

15. A singular proposition is a universal one; for

it applies to the whole of its subject.

16. Whatever tends to withdraw the ind fro pursuits of a low nature deserves to be promoted; cl sical learning does this, since it gives us a taste for intellectual enjoyments; therefore it deserves to be pro oted.

17. Bacon was a great lawyer d states an; and as he was also a philosopher, we may infer that any philosopher ay be a great lawyer and statesman.

18. I oral co p ions should be avoided; but so e i moral co p ions are intelli ent persons, so that some intelligent persons should be avoided.

19. Mathematical study undoubtedly i proves the re oning powers; but, the study of logic is not athematical study, we may infer that it does not i prove the reasoning powers.

20. Every c did m acknowledges erit in a rival; every learned does not do so; therefore

every learned man is not candid.

LESSON XIX.—Conditional Arguments.

1. What are the kinds of conditional propositions, and by what signs can you recognise them? 2. What e the rules of the hypothetical syllogis?

3. To what categorical fallacies do breaches of these les correspond?

4. elect fro the following such are valid arguents, and reduce the to the categorical form; explain the fallacious reasoning in the others.

(1) Rain has fallen if the ground is wet; but the ground is not wet; therefore rain has not fallen.

(2) If rain h fallen, the ground is wet; but rain has not fallen; therefore the ground is not wet.

(3) The ground is wet, if rain has fallen; the ground is wet; therefore rain has fallen.

(4) If the ground is wet, rain has fallen; but rain has fallen; therefore the ground is wet.

N.B. In these as in other logical examples the student ust argue only from the pre ises, and not fro any other knowledge of the subject- atter.

 Show that the canons of syllogism (p. 121) ay be stated differently in the hypothetical or categorical form.

 State the following in the for of a Disjunctive of Dile atic gument, and name the kind to which it belongs.

If pain is severe it will be brief; and if it last long it will be sli ht; therefore it is to be patiently borne

LESSONS XX. d XXI-Fallacies.

1. Classify fallacies.

2. Explain the following expressions:

A dicto secund quid ad dict si pliciter; igno ratio elenchi; argu entu ad ho ine; argu entu ad popul ; petitio principii; circulu in prob do; non sequitur; post hoc er o propter hoc.

3. What is arguing in a circle; and what is a question-begging epithet?

4. What differences of ean g ay be produced the followin sentence by varying the accent?

"Newton's discovery of gravitation is not generally believed to have been at all ticipated by several philosophers in En l d d Holland."

5. Po't out the isinterpretations to which the following sentences ight be liable.

(I) He went to London and then to Brighton by the express train.

(2) Did you ake a long speech at the eeting?

(3) How uch is five times seven and nine?

MISCELLANEOUS EXAMPLES.

LESSONS IX. to XXI.

(Continued fr p. 313.)

The followin exa ples consist partly of t e and partly of false argu ents. The reader is requested to treat the as follows:

 If the ex ple is not in a si ple and co plete logical fo , to co plete it the fo which app rs ost appropriate.

. To cert 'n whether it is a valid or fallacious

argu ent.

To sign the exact name of the arguent or fallacy as the ceay be.

4. If a categorical syllogis, to reduce it to the first figure.

 If a hypothetical syllogism, to state it the categorical fo .

21. Ele entary substances alone e etals. Iron a metal; therefore it is an ele entary substance

- 22. No Athenians could have been Helots; for all the Helots were slaves, and all Atheni s were free en.
- 23. Aristotle must have been a of extraordinary industry; for only such a an could have produced his works.
- 24. Nothing is better than wisdom; dry bread is better the nothin; therefore dry bread is better than wisdom.
- 25. Pitt was not a great and useful inister; for though he would have been so had he carried out Ada Smith's doctrines of Free Trade, he did not carry out those doctrines.
- 26. Only the virtuous are t ly noble; some who are called noble e not virtuous; therefore so e who e called noble are not truly noble.
- 27. Ireland is idle d therefore starves; she starves, d therefore rebels.
- 28. No designing person ou ht to be trusted; engravers are by profession designers; therefore they ou ht not to be trusted.
- 29. Logic as it was cultivated by the school en proved a fruitless study; therefore Logic as it is cultivated at the present day must be a fruitless study likewise.
- 30. Is a stone a body? Yes. Then is not animal a body? Yes. Are you an animal? I think so. Er o, you e a stone, being a body.—*Lucian*.
- 31. If ye were Abraham's children, ye would do the works of Abraham.—John viii. 39.
- He that is of God he eth God's words: ye therefore he the not, because ye are not of God.

 —John viii. 47.
- 33. Mahomet w a wise lawgiver; for he studied the character of his people.

34. Every one desires virtue, because every one desires happiness.

35. His becility of chacter i ht have been inferred from his proneness to favourites; for all weak princes have this failing.—De Morgan.

36. He is brave who conquers his passions; he who resists temptation conquers his passions; so that he who resists temptation is brave.

37. Suicide is not always to be conde ed; for it is but voluntary death, and this has been gladly embraced by any of the greatest heroes of antiquity.

38. Since all etals are elements, the ost rare of all the etals ust be the most r e of all the ele ents.

39. The express train alone does not stop at this station; and as the 1 t train did not stop it ust have been the express train.

40. Peel's remission of t es was beneficial; the t es re itted by Peel were indirect; therefore the re 'ssion of indirect t es is beneficial.

41. Books e a source both of instruction and a usement; a table of logarithms is a book; therefore it is a source both of instruction and a useent.

42. All desires are not bla eable; all desires are liable to excess; therefore so e things liable to cess are not bl eable.

 Whosoever intentionally kills another should suffer death; a soldier, therefore, who kills his enemy should suffer death.

44. Projectors are unfit to be trusted; this m h fo ed a project; therefore he is unfit to be t sted.

45. Few towns in the United Kin do have more than

- 300, inhabitants; and as all such towns ou ht to be represented by three e bers in Parliaent, it is evident that few to s ought to have three representatives.
- 46. All the works of Shakspeare c not be read in a day; therefore the play of Hamlet, bein one of the works of Shakspeare, cannot be read in a day.
- 47. In moral atters we cannot st d still; therefore he who does not go forward is s e to fall behind.
- 48. The people of the country are suffering from famine;
 d you e one of the people of the country
 you ust be suffering from figure.
- 49. Those substances which are lighter than water c float upon it; those etals which can float upon it are potassiu, sodium, lithium, &c.; therefore potassiu, sodiu, lithiu, &c., are lighter than water.
- 50. The laws of nature ust be certained by Deduction, Traduction or Induction; but the former two e insufficient for the purpose; therefore the laws of nature ust be ascertained by Induction.
- 51. A successful author ust be either very industrious or very talented; Gibbon was very industrious, therefore he w not very talented.
 52. Very constant what I
- 52. You are not what I; I a a; therefore you e not a
- 53. The holder of so e sh es in a lottery is sure to gain a p e; d as I a the holder of so e sh es in a lottery I a sure to ain a prize.
- 54. Gold d silver are wealth; d therefore the di inution of the gold d silver in the country by exportation is the diminution of the wealth of the country.

- 55. Over credulous persons ought never to be believed; d as the Ancient Historians were y instances over credulous they ou ht never to be believed.
- 56. Some ineral compounds are not deco posed by heat; all organic substances e deco posed by heat; therefore no or ic subst ces are mineral co pounds.

57. Whatever schools exclude religion are irreligious; Non-sectarian schools do not allow the teachin of religious creeds; therefore they are irreligious.

58. Night ust be the cause of day; for it variably precedes it.

59. The ancient Greeks produced the greatest terpieces of eloquence d philosophy; the Laced moni s were cient Greeks; therefore they produced the greatest terpieces of eloquence and philosophy.

60. All presu ing en e contemptible; this , therefore, is contemptible; for he presu es to believe his opinions e correct.

61. If a substance is solid it possesses el ticity, d so also it does if it be liquid or g eous; but all subst ces e either solid, liquid or eous; therefore all substances possess el ticity.

62. If P r's life pills e of y value those who take the will improve health; now y friend who h been taking the has improved in health; therefore they are of value.

63. He who calls you a speaks truly; he who calls you a fool calls you a ; therefore he who calls you a fool speaks truly.

64. Who is ost hungry eats ost; who eats le t is ost hungry; therefore who eats le t eats ost.

65. What produces intoxication should be prohibited:

the use of spirituous liquors causes intoxication; therefore the use of spirituous liquors should be prohibited.

66. What we eat grew in the fields; loaves of bread e what we eat; therefore loaves of bread grew

in the fields.

67. If li ht consisted of aterial particles it would possess o entu; it c ot therefore consist of material particles, for it does not possess mo entu.

68. Everything is allowed by law which is orally ri ht; indulgence in pleasures is allowed by law; therefore indul ence in ple ures is morally ri ht.

69. All the trees in the park make a thick shade; this is one of the , therefore this tree makes a thick

shade.

70. All visible bodies shine by their own or by reflected light. The oon does not shine by its own, therefore it shines by reflected light; but the sun shines by its own light, therefore it c not shine by reflected li ht.

 Honesty deserves reward; and a negro is a fellowcreature; therefore, an honest negro is a fellow-

creature deserving of rew d.

72. Ne ly all the satellites revolve round their pl ets fro west to east; the oon is a satellite; therefore it revolves round its planet fro west to east.

73. Italy is a Catholic country d abounds in beggars; F nce is also a Catholic country, d

therefore abounds in be g s.

74. Every law is either useless or it occasions hurt to so e person; now a law that is useless ou ht to be abolished; d so ou ht every law that occasions hurt; therefore every law ou ht to be abolished.

- 75. The end of a thin is its perfection; death is the end of life; therefore death is the perfection of life.
- 76. When we hear that all the righteous people e happy, it is hard to avoid exclaiming, What! are all the unhappy persons we see to be thought unrighteous?
- 77. I am offered a sum of money to assist this person in gaining the office he desires; to assist a person is to do him good, and no rule of morality forbids the doing of good; therefore no rule of morality forbids me to receive the sum of money for assisting the person.
- 78. Ruminant animals are those which have cloven feet, and they usually have horns; the extinct animal which left this foot-print had a cloven foot; therefore it was a ruminant animal and had horns. Again, as no beasts of prey are minant animals it cannot have been a beast of prey.
- 79. We must either gratify our vicious propensities, or resist them; the former course will involve us in sin and misery; the latter requires self-denial; therefore we must either fall into sin and misery or practise self-denial.
 - O. The stonemasons are benefitted by the m ons' union; the bricklayers by the bricklayers' union; the hatmakers by the hatmakers' union; in short, every trade by its own union; therefore it is evident that if all workmen had unions all workmen would be benefitted thereby.
 - 81. Every moral aim requires the rational eans of attaining it; these means are the establishment of laws; and as happiness is the oral aim of an it follows that the attainment of happ ess requires the establishment of laws.

- 82. He that can swi needs not despair to fly; for to swim is to fly in a rosser fluid, and to fly is to swi in a subtler.
- 83. The Helvetii, if they went through the country of the Sequa, were sure to meet with v ious difficulties; and if they went through the Ro province, they were exposed to the dan er of opposition from C sar; but they were oblied to go one way or the other; therefore they were either sure of meeting with various difficulties, or exposed to the danger of opposition fro C sar,—De Bello Gallico, lib. 1. 6.
- 84. Riches are for spending, and spending for honour d good actions; therefore extraordinary expense must be limited by the worth of the occasion.—Bacon.
- 85. If light is not refracted ne the surface of the moon, there cannot be any twilight; but if the moon h no atmosphere light is not refracted near its surface; therefore if the moon h no atmosphere there cannot be any twilight.
- 86. The preservation of society requires exch ge; whatever requires exchange requires equitable valuation of property; this requires the adoption of a common measure; hence the preservation of society requires the adoption of a com on measure.
- 87. The several species of brutes being created to prey upon one another proves that the hum species were intended to prey upon the .
- 88. The more correct the logic, the more certainly the conclusion will be wrong if the premises are false. Therefore where the pre ises e wholly uncertain, the best logician is the least safe guide.

89. If our rulers could be trusted always to look to the best interests of their subjects, onarchy would be the best form of overn ent; but they cannot be trusted; therefore mon chy is not the best form of government.

90. If en were prudent, they would act orally for their own good; if benevolent, for the good of others. But many men will not act orally, either for their own good, or that of others; such men, therefore, are not prudent or benevolent.

91. He who bears arms at the command of the magistrate does what is lawful for a Christian; the Swiss in the French service, and the British in the American service, bore arms at the com and of the agistrate; therefore they did what was lawful for a Christian.—Whately.

92. A an that hath no virtue in himself ever envieth virtue in others; for en's minds will either feed upon their own ood or upon others' evil; and who wanteth the one will prey upon the other.— Bacon.

93. The object of w is durable peace; therefore soldiers are the best peace- akers.

94. Confidence in promises is essential to the tercourse of hu an life; for without it the greatest part of our conduct would proceed upon chance. ut there could be no confidence in promises, if en were not obliged to perform the ; the obligation, therefore, to perfo promises is essential to the same ends d in the s e degree.

95. If the majority of those who use ublic-ho es e prepared to close the , legislation is unnecessary; but if they are not prep ed for such a eas e, then to force it on the by outside pressure is both dangerous and unjust.

21---2

96. He who believes his self to be always in the right in his opinion, lays claim to infallibility; you always believe yourself to be in the right in your opinion; therefore you lay clai to infallibility. -Whately.

97. If we never find skins except as the teguments of animals, we may safely conclude that animals cannot exist without skins. If colour cannot exist by itself, it follows that neither c thing that is coloured exist without colour. So, if language without thought is unreal, thought without language must also be so.

98. No soldiers should be brought into the field who are not well qualified to perform their part; none but veterans are well qualified to perform their part; therefore none but veterans should be brought into the field. - Whately.

99. The minimu visibile is the le t magnitude which can be seen; no part of it alone is visible, and yet all parts of it ust affect the mind in order that it ay be visible; therefore, every part of it must affect the mind without being visible.

100. The scarlet poppy belongs to the genus Papaver, of the natural order Papaverace; which again is part of the subclass Thalamiflor, belonging to the great class of Dicotyledons. Hence the scarlet poppy is one of the Dicotyledons.

101. Improbable events happen almost every day; but what happens almost every day is a very probable event; therefore improbable events are very probable events.-Whately.

LESSON XXII.—Quantification of the Predicate.

1. What d s the quantification of the predicate mean?

Assign to each of the following propositions its proper symbol, and the symbol of its converse:

(1) Knowledge is power.

(2) So e rectangles are all squares.

(3) Only the honest ultimately prosper.

(4) Princes have but their titles for their glories.

(5) In man there is nothing great but mind.

(6) The end of philosophy is the detection of unity.

- Draw all the contrapositive propositions and immediate inferences you can from the following propositions:—
 - (1) London is a great city.

(2) London is the capital of England.

- (3) All ru inant i als e all cloven-footed anials.
- (4) Some embers of parliament e all the ministers.
- Write out in Hamilton's notation the moods aroko, Darapti, Felapton, Bokardo.

LESSON XXIII.—Boole's System of Logic.

Apply this system of inference to prove the syllogis s on p. 141, in Cesare, d Camestres.

Show that if all A's are not B's, then no B's are
A's; and that if all A's are all B's, then all not
A's are all not B's.

3. Develope the te substance, as reg ds the terms vegetable, ani al, organic; then select the cobinations which agree with these premises:

"What is vegetable is not animal but is orgic; what is ani alis orgic."

4. Test the validity of this argument: "Good always triumphs, and vice always fails; therefore the victor cannot be wrong, nor the v quished right." 5. It is known of a certain cl s of things that-

(1) Where the quality A is, B is not.

- (2) Where B is, and only where B is, C and D are. What can we infer from these pre ises of the cl s of things in which A is not present but C is present?
- If all A's are B's; all B's are C's; all C's are D's; shew that all A's are D's, and that all not D's are not A's.

LESSON XXIV.—Method.

- r. What is the supposed position of ethod accordin to former logical writers, and what are the rules of ethod?
- 2. Explain the expressions nobis notiora, and notiora naturæ.
- 3. Of what k' d is the usual ethod of instruction?
- Prove that analysis in extension is synthesis in intension, usin so e of the series of terms
 Question 6, Lesson v. illustrations.

5. Expl 'n the act meanings of the expressions à priori d à posteriori knowledge.

. To which kind belongs our knowledge of the followin facts?

- (1) The light of the stars takes a lon time to reach us.
- (2) Vaccination is a preservative against small-pox.
- (3) A eteor beco es heated in passing through the air.
- (4) There must be either so e inhabit ts or no inhabitants upon Jupiter.

L SON XXV.—Perfect Induction.

 Define and distinguish Deduction, Induction, d T duction.

- 2. Find an instance of reasoning in Traduction.
- 3. Distinguish Perfect and Imperfect Induction.
- 4. How does Mr Mill define Induction, and what is his opinion of Perfect Induction?
- 5. What is the use of Perfect Induction?
- Construct some instances of the inductive syllogism, and show that they may be thrown into a disjunctive form.

LESSON XXVI.—Induction, Analogy and Example.

- I. From what circumstance arises the certainty and generality of reasoning in geometry?
- Find other instances of certain and general re oning concerning the properties of numbers.
- Why are inductive conclusions concerning prime nu bers uncertain and not general?
- 4. Why is a single instance sometimes sufficient to warrant a universal conclusion, while in other cases the greatest possible number of concurring instances, without any exception, is not sufficient to w rant such a conclusion?
- 5. What are the strict d ordinary e ings of the word analogy?
- 6. Explain the use of Exa ples.
- Explain exactly the difference between alogical argument and ordinary induction.

LESSON XXVII.—Observation and Experiment.

- I. What is the false ethod of Science against which Bacon protested?
- Explain the exact eaning of Bacon's sertions, that man is the Serv t and Interpreter of Nature, and that Knowled e is Power.
- 3. How does experi ent differ from observation?

4. Classify the sciences according as they employ passive observation, experiment, or both.

5. Name the chief points in which experi ent is superior to mere observation.

6. What is the principal precaution needful in observation?

7. Explain how it is possible to anticipate nature and vet establish all conclusions upon the results of experience.

LESSONS XXVIII. and XXIX.—Methods of Induction.

- I. Define exactly what is meant by a cause of an event, and distinguish cause, occasion, antecedent.
- 2. Point out all the causes concerned in the following phenomena:

(1) The burning of a fire.

(2) The ordinary growth of vegetables.

(3) The cracking of a glass by hot water.

3. State and explain in your own words Mr Mill's first three Canons of Inductive Method.

4. Point out exactly how the Joint Method differs from the simple Method of Difference.

5. Give so e instances of simple experiments fulfilling completely the conditions of the Method of Difference.

6. What c you infer from the following instances?

> Antecedents. Consequents. ABDE.....stqp BCD.....gsr BFG.....vyu ADEtsp BHK....zqwABFGpquv ABE.....pqt.

- (1) Friction alters the temperature of the bodies rubbed together.
 - (2) The sun is supposed to move through space.
 - (3) A ray of light passing into or out of a denser medium is deflected.
 - Point out the successive questions which would have to be decided in the investigation of the above phenomena.
- Find some simple instances of the homogeneous and heterogeneous intermixture of effects, and of the methods of concomitant variations and residues.
- 9. Since 1842 there has been a great reform of the British tariff, and a great increase of British trade. Does this coincidence prove that the first circumstance is the cause of the second?
- 10. Supposing us to be unacquainted with the causes of the following phenomena, by what methods should we investigate each?
 - (1) The connection between the barometer and the weather.
 - (2) A person poisoned at a meal.
 - (3) The connection between the hands of a clock.
 - (4) The effect of the Gulf-stream upon the climate of Great Britain.

LESSON XXX.—Empirical and Deductive Methods.

- Define Empirical Law, and find a few additional instances of such laws.
- 2. What are the three steps of the Deductive Method?
- Trace some of the successive steps in the progress of the theory of gravitation, showing that it was established by this method.

LESSON XXXI.—Explanation, &c.

- 1. What do you ean by the explanation of a fact?
- State the three ways in which a law of nature ay be explained, and suggest some additional instances of each case.
- 3. Define tendency. Do all causes consist only of tendencies, or can you find examples to the contrary?
- 4. Give a definition of hypothesis. How may a valid be distinguished from an invalid hypothesis?
- 5. What place does hypothesis hold in the Deductive Method?
- Explain the ambiguities of the words theory and fact.

LESSON XXXII.—Classification.

- Define classification, and give the derivation of the word.
- 2. What do you mean by important characters in classification?
- State Dr Whewell's criterion of a good natural arrangement.
- Distinguish between a natural and artificial syste of classification.
- 5. What do you mean by a characteristic quality? Is it always an important quality?
- Define abstraction, generalization, d colligation of facts.
- 7. What are the characters of a notion properly abst cted?

LESSON XXXIII.—Requisites of a Philosophical Language.

I. What are the three purposes for which we use language? 2. What are the two chief requisites of a philosophical language?

By what considerations should we be guided in choosing between a new and old scientific term?

4. Distinguish a Descriptive Terminology and a Nomenclature; separate the following terms according as they belong to one or the other:

Rose, Rosace, Rose-like, Potassium, Alkaloid, Ruminant Animal, Ruminating, Ruby, Ruby-red

5. What does Mr Mill mean by the expression Na-

tural Kind?

INDEX,

AND CONCISE VOCABULARY OF LOGICAL AND PHILOSOPHICAL TERMS.

bacus, the lo ical, 199
bscissio In niti (the cutting off of the infinite or negative part), the process by which we determine the position of an object in a system of classes, by successive comparison and rejection of those classes to which it does not belong. bsolute terms, i.e. non-relative terms, 25; sometimes used as name of non-connotative terms, 41 bstract terms, 20, 43 bstraction, 285 ccent, fallacy of, 174 ccident, fallacy of, 176; the predicable, ro3 ccidental de nition is a definition which assigns the properties of a species, or the accidents of an individual; it is more commonly called a Description. cquired perceptions, 236 dded dete inants, inference by, 86 dequate knowledge, 56 dicto secundu quid, &c., fallacy of, 176 djectives, 21 dverbials, 93 ative propositions, 63 ebr c reasoning, 58, 219 bi uity of all, 20; of some, 79 of many old terms, 291; of terms in Political Economy, 292 biguous middle term, 130, 171 phibolo , fallacy of, 172 pliative propositions, 69 Amphibolo nalo ue, a thing analogous to some other thing. nalysis, method of, 205

alogy, the cause of ambiguity, 35, 50; reasoning by, 226—8 nalytics, (τα λααλυτικά,) the title given in the second century to portions of the Organon, or Logical Treatises of Aristotle; they were distinguished as the Prior and Posterior Analytics.

Analytic syllogis, a syllogism in which the conclusion is placed first, the premises following as the reasons. See Synthetic Syllogism; the distinction is unimportant.

Antecedent, of a hypothetical proposition, 160; of an event, 240 nticipation of nature, 229

Antino y (ἀντι, against; νόμος, law), the opposition of one law or rule to another. Kant.

A posteriori knowledge, 208
priori knowledge, 208
rbor Po hyriana, see Tree of

Porphyry.

gu ent, (Latin, argus, from apyos, clear, manifest,) the process of reasoning, the shewing or proving that which is doubtful by that which is known. See inference. The middle term of a syllogism is sometimes called specially the argument.

gu entu a fortiori, an ar ment in which we prove that the e in question is more strong or probable than one already conceded to be sufficiently so, rgu entu ad he ine,

r entu ad judiciu, an appeal to the common sense of mankind.

ent ad i or , an argument founded on the i o ce of adver es. gument ad populu ,

entu ad verecundi , an appeal to our respect for some great authority.

r entu ex concesso, a proof derived from a proposition already conceded.

stotle's icta, 123
Art and Science, distinction of, 7
Artifici Classification, 284

Assertion, (ad, to; sero, to join,)
a statement or proposition, affirma-

tive or negative.

ssociation of ideas, (associo, to accompany; socius, a companion.) the natural connection existing in the mind between impressions which have previously coexisted, or which are similar. Any idea tends to bring into the mind its associated ideas, in accordance with the two great laws of association, the Law of Contiguity, and the Law of Similarity.

Ass p on, (assumo, to take for granted,) any proposition taken as the basis of ar ment; in a special sense, the minor premise of a cate-

gorical syllogism.

ttribute, (attribuo, to give or ascribe to,) a quality or circumstance which y be affirmed (or denied) of a thing: opposed to Substance, which see.

t 'bute in grammar, 92
ttributive term, i.e. Connotative

Axio , defininition of, 125

aco method, 255; Philosophy, 229

b a, Celarent, &c., 145 egging the uestion, 179 elief, assent to a proposition, admitting of any degree of strength, from the slightest probability to the fullest certainty; see *Probability*, en , Geo e, new system of

Logic, 187
cole, George, his system of Logic,
101; his Laws of Thought, 197;

his logical works, 201

C ons of syllogism, 121-2: Hamilton's supreme Canon, 189

ons of Mill's Inductive Methods, First, 240; Second, 242; Third, 245; Fourth, 252; Fifth, 249

Categore atic words, 18
Catego cal propositions, 63
Categories, the summa genera, or
most extensive classes into which

most extensive classes into which things be distributed; they are ten in number, as follows:

Odola, Substance; Ποσον, Quantity; Ποίον, Quality; Πρόε τι, Relation; Ποίειν, Action: Πάσχειν, Passion, or suffering; Ποῦ, Place; Πότε, Time; Κεῖσθαι, Position; Έχειν, Habit or condition.

Everything which be affirmed must come under one or other of these highest predicates, which were described in the first treatise of Aristotle's Organon, called the Categories.

Cause, meaning of, 239

Aristotle distinguished four kinds of causes in the existence of a thing of. The Material Cause, the substance or matter composing it; a. The Formal Cause, the pattern, type or design, according to which it is shaped; 3. The Efficient Cause, the force employed in shaping it; 4. The Final Cause, the end, motive or purpose of the work.

hance, ignorance of the causes which are in action; see *Probability*.

h c r, derivation of the word,

Ch acteristics, 285 culus in definiendo, 110, 114 culus in probando, 179

lea ess of knowledge, 54
o i on, (cogrosco, to know,)
knowledge, or the action of mind in
acquiring knowledge.

Co gation of Facts, Dr Whewell's expression for the mental union of facts by some suitable conception, see 286

Collective te , 19 Co b ed or complete method of investigation, 258

Co p son, (com, together; par, equal or like,) the action of mind by which we judge whether two objects of thought are the same or different in certain points. See *Judgment*.

o patible terms are those which.

though distinct, are not contradictory, and can therefore be rmed of the same subject; as "large" and "heavy;" "bright-coloured" and "nauseous."

o plex concep on, inference by, 87

o plex sentence, 91; syllogism,

Co position of Causes, the principle which is exemplified in all cases in which the joint effect of several causes is identical with the sum of their separate effects. S. S. Mill. See pp. 252, 265

Composition, fallacy of, 173

Co pound sentence, co

Co prehension of terms, see Intension.

Co putation, 127

Concept, that which is conceived, the result of the act of conception; nearly synonymous with general notion, idea, thought.

Conception (con, together; capio, to take). An ambiguous term, meaning properly the action of mind in which it takes several things together, so as to form a general notion; or again, in which it forms "a mental image of the several attributes given in any word or combination of words." Mansel.

Conceptu sts, 13 Conclusion of syllogism, 15, 127; weakened, 140

Concrete terms, 20

Conditional propositions, 62, 160 Con sion of words, ambiguity

from, 31

Conju ate words, those which come from the same root or stock, as kn n, knowing, knowingly, known

onnotation of terms, 39, 4x; ought to be exactly fixed, 290 onsciousness, the immediate knowledge which the mind has of its sensations and thoughts, and, in general, of all its present operations. Reid.

onsect :

ledge.

= Corollary.

onsequence, the connection between antecedent and consequent; but often used ambiguously for the

onsequent of a hypothetical proposition, 161

onsequent or effect of a cause,

onsequent, fallacy of the, 181 onservation of energy, 263, 269 onsi ence of Inductions, the agreement of inductions derived from different and independent series of facts, as when we learn the motion of the earth by entirely different modes of observation and reasoning. Whenuell.

onsistency of propositions, 78 onsistent terms, see compatible

terms.

ontingent, (contingo, to touch,) that which may or may not happen; opposed to the necessary and imbossible.

ontin ent matter, 80

ontin entracter, so ontinuity, Law of, the principle that nothing can pass from one extreme to another without passing through all the intermediate degrees; motion, for instance, cannot be instananeously produced or destroyed.

ontradic on, Law of, 117, 193 ontradictory terms, 24, 119; propositions, 76

Contraposition, conversion by, 83, 186

Converse fallacy of accident, 176 Conversion of propositions, 82—85; with quantified predicate, 184

Conve end, 82 Coordinate propositions, 90 Copula, 16

Coroll y, a proposition which follows immediately from another which has been proved.

Co ection of observations, 253
Co ela Ve terms, 25

riterion (κριτηριον, from κρίνω, to judge), any fact, rule, knowledge, or means requisite to the formation of a judgment which shall decide a doubtful question.

ross division, 105

ata, (plural of datum, that which

is given,) the facts or assertions from which an inference is to be drawn. eduction and Induction, 212 educ ve or combined method. 258, 272 e facto, what actually or really happens: opposed to de jure, what ought to happen by law or right. on, the logical process, roo. 112; of logic, 1 ee, terms expressing, 24; questions of, 120. onstra on, (demonstro, to point out.) strictly the pointing out the connection between premises and conclusion. The term is more generally used for any argument or reasoning regarded as proving an asserted conclusion. A demonstration is either Direct or Indirect. In the latter case we prove the conclusion by disproving its contradictory. or shewing that the conclusion be supposed untrue. De ons a ve Induction, 220 's logical discoveries tings, 100 Denota on of terms, 39 ep of a notion, see Intension.

De vatives from the root spec, sight, 52 Desc es on Method, 116, 229 Desc p on, see Accidental Definition. olo , 292 esc `p ve c ve dilem ; hypothetical syllogism, 162-4 Desynonymization of te Dete ation, the distinguishing of parts of a genus by reunion of the genus and difference. See Division. evelop ent of a term, 193 s, of sentences, 93-7; of , 129-133, 142; of pro-

positions, 72-75

ia ectic (διαλεχτική τέκνη, the art

of discourse, from διαλέγεσθαι, to disco). The original name of

Logic, perhaps invented by Plato;

also used to denote the Logic of Probable Matter (Aristotle), the

the Science of Being; it is thus a

ichoto y, di on by, 107, 193

biguous te

n and Lan age,

syllogi

right use of R

highly

icta de omni et nullo, 123 i erence, the predicable, eren a on of terms, 40 ile a, 167 isbelief, the state of mind in which we are fully persuaded that some opinion is not true. J. S. Mill. It is equivalent to belief in the con dictory opinion or assertion, and is not to be confused with Doubt, which see. isco se, or reasoning, 15 iscove method of, 202 c ve, propositions, 62, 160; syllogism, 166, 194 is ct knowledge, 55 bution of terms, 19, 74-5, is sion, logical, 105; metaphysical, 108; fallacy of, 174 oubt, (dubito, to go two ys,) the state of mind in which we hesitate between two or more inconsistent opinions. See Disbelief. of a proposition, the varying y be attributed to meaning which the same sentence according to actuation. See Fallacy of accent. 174-5 piricis (έμπειρία, experience), the doctrine of those who consider that all knowledge is derived merely from experience. Law, 256 C e e, 153 pich e a, 155 pisy ogis , 155 VOC terms, 29 quivoca on, 30; causes of, 31; fallacy of, 171 ssence, (essentia, from esse, to be,) "the very being of anything, where-by it is what it is." Locke. It is an ancient scholastic word, which not be really defined, and should be banished from use. ssential propositions, er's diagrams, 72-5, 129-133, vidence, (e, and videre, to literally the seeing of anything The word now means any facts apprehended by the mind and

unds of knowledge and belief.

xa ples, use of, 227 xceptive propositions, 68 iddle, law of, 127. xcluded 119, 192 xclusive propositions, 68 xhaustive division, 107, 192 xperience, 228 xperi entu crucis, an experiment which decides between two rival theories, and shews which is to he adopted, as a finger-post shews which of two roads is to be taken. xplanation, of facts, 264; of laws, 265 xplicative propositions, 68 xposita, a proposition given to be treated by some logical process. xtension and intension, 37, 208 xtensive yllogis , 159 xtre es of a proposition, are its ends or terms, the subject and predicate.

Fact, 275
allacy, purely logical, 170; semilogical, 170—175; material, 176— 182; in hypothetical syllogism, 162; in dilemma, 168

False cause, fallacy of, 181
False propositions, 70

Figure of speech, fallacy of, 175
Figures of the syllogism, 138; their

uses, 143

For and matter of thought, 4

unda entu divisionis, 105

unda entu relationis, the

ground of relation, i.e. the series of

events or circumstances which es-

tablish a relation between two correlative terms. Funda ental principles of syllogism, 121

alenian, or 4th figure of the syllogism, 145
eneral notions, 13; terms, 18

eneralization, 286; of names,

eneric property, 102 enus, 98; generalissimum, 100 eo etrical reasoning, 58, 218; Pascal on, 115

Gra a cal predicate, 88; sentence, 89 ravitation, theory of, 260 a ilton, Sir W., Method of Notation, 187

Herschel, Sir J., on active and passive observation, 234

Heterogeneous, 101; intermixture of effects, 252

o ogeneous, 101; intermixture of effects, 252, 265

o ologue, whatever is homolo-

gous.

Ho ology, a special term for the analogy existing between parts of different plants and animals, as between the wing of a bird and the fore leg of a quadruped, or between the scales of a fish and the feathers of a bird.

o onymous terms, 30 ypothesis, 269, 270 ypothetical propositions, 62,160, syllogism, 161—2

Idea (lôśa, elôos, image), a term used ambiguously, but generally equivalent to thought, notion, concept. Defined by Locke as "Phantasm, notion, species, or whatever it is which the mind can be employed about in thinking." To have an idea of a thing is to think of that thing. Identity, law of, 117—8

Identity, law of, xx7-8
Idol (etōoλor, etōos, image), Bacon's Liguraive name for the sources of error; he enumerated four kinds; Idols of the Tribe, which affect all people; Idols of the Cave, which are peculiar to an individual; of the Forum, which arise in the intercourse of men; of the Theatre, which proceed from the systems of philosoproces of the Theatre, which are the systems of philosoproces of the Theatre, which proceed from the systems of philosoproces.

phers.

Ignoratio lenchi, 178

Illation (illatium, past participle of infero, to bring in). See Inference.

Illative, that which can be inferred.

Illicit process, of the minor term,

131; of the major term, x32, x39

I ediate inference, 85-7

I perfect res of the syllogism, x45

perfect Induction, 213
possible matter, 80

Inconsistent terms imply qualities which cannot coexist in the same thing. See compatible terms.

cons tent propositions, 76 d.e te propositions, 65 Inde te or infinite term, is a negative t which only marks an object by exclusion from a class. desi te propositions. See Indefinite propositions. Indirect d onstration. See Detrat ect . \mathbf{In} erence, method of, irect reduction of the syllo-

gism, 146, 148-9. di du , what not be divided without losing its n e and distinctive qualities, although generally capable of physical division or par-

tition, which see. Induction, 212

Inductive syllogism, 211, 214 ediate, Inference, defined, 81: 85-87; mediate, 126 as ecies, 100

ate ideas, see a priori truths, 208
ep able accident, 103 sep Inst ces, use of, 227 Intension and extension of ter , 37, 99, 2 ; law of relation, 40 Intensive syllogis , 159

Inten on, first and second, a disthus defined tinction between te by Hobbes :- " Of the first intention are the names of things, a stone, &c.; of the second the d speeches, as es of n es of es, d speeches, as univ al, part lar, genus, species, syllogism, and the like." A term of the second intention expresses the mode in which the mind regards or classifies those of the first intention. , explanation ter e ate

by, 267 Intui ve knowledge, 57 version of subject and predicate, t conclusion, fallacy of, ele⊽

178

e t, 12 Jud

e, the subject of logic, 10 e, requisi of philosophical, 290; three purposes of, 287 Laws of thought, i, 117; of nature, 239

tz on Knowledge, 53 a (λαμβάνω, to take or ase), a proposition, a premise ted; in geometry, a preliminary proposition. Limit on, version by, 82,87 Logic, derivation of ne, 6 abacus, slate and chine, Lo `c Logo achy, 292 Lowest species, 100

c ne, the logical, 199 ajor, te , 128; premise, 129 y questions, fallacy of, 182 ateri lacies, 170, 176 e atic induction, 220 atter of thought, 4; of proposier is defined by J. S. ill as
"the external cause to which we
be our se tions," or as Perent P bility of Se

ate inference, 126 videntia, the parts e bra into which a class is divided; the constituent species of a gen

e phor, 50 di on r etaphy etaphy CS (та цета та the works of Aristotle which followed or were studied af his Physics. First Philosophy, or the so-called science of thin in their ; ontology or the own na ۸f

d òòós, od (μέθοδος, μετα ient of way), mode, y or accomplishing an end.

e od, the fourth part of logic, 201; Pascal on, 114; De on, 116; of indirect infer-Disco ence, 192

ethods of Induction, Agreement, 240; Difference, 242; of Experiment, 243; Joint ethod, 245; Residues, 252; Concomitant Variament, 243; Joint tions, 249

etonymy (μετά, and ονομα,name), e for the transfer grammatical g of a word to a closely connected thing, as when we speak it. See T ifer of d e

ill, J. S., on Connotative terms, 41; on Induction, 214; on Analogy and Induction, 227; on Observation, 235; on Terminology and Nomenclature, 294

inor term, 128; premise, 129 ne onic verses, Barbara, &c.,

odal proposition, 69, 91
odus, ponens, 161; tellens, 162
odus, ponendo tellens, 166; tollendo ponens, 166
oods of the syllogism, 136; according to Hamilton, 188

a . c, or term, 17 atural Classification, 280 atural inds, 294

ecessary matter, 80 ecessity (me, not; and cesso, to ecess), that which always is and cannot but be.

egation, conversion by, 83 egative, terms, 22; propositions, 64, 84; premises, fallacy of, 133-4 owton's experiment, 253, 259 o enclature, 293

ominal definitions, 112 ominalists, 13

on causa pro causa, 181 on sequitur, 181

otion (nonco, to know), the action of apprehending or taking note of the various qualities of an object; or more commonly the result of that action. See Idea, Concept.

otiora nature, 204 ovum Organum, first aphor-

isans of, 220 umerically definite syllogian, 103

Object of verb, 94
Objective, that which belongs to
the object of thought, the nan-ego;
opposed to Subjective, which see.
Obscure knowledge, 84

Observation, 217, 45
bversion is a mane used by Profewar Alexander Bain to denote the process previously salled Immediate Informe by Privative Conception,85 pponito terms, 24, 429

prosition of propositions, 78 Organon (Spycros, Latin Organism,

Instrument), a name for Aristotle's logical treatises, first generally used in the 15th century, implying that they may be regarded as an instrument to assist the mind. The name was adopted by Bacon for his Novum Organium.

aradox (παρά, δόξα, contrary to opinion), an assertion contrary to common opinion, and which may or may not prove true: often wrongly used to mean what is self-contradictory and absurd.

alogis (παραλογίζομαι, to reason wrongly), a purely logical fallacy, or breach of the rules of deductive

logic.

arity of reasoning, an expression used to denote that when one case has been demonstrated, other similar cases can be demonstrated by a like course of reasoning.

ony ous words, see Conjugate words.

ticul propositions, 63—6,72,79 premises, fallacy of, 135,

artition or physical division, 108 er accidens, conversion, 82 erfect i ure of the Syllogism,

erfect owledge, characters of, 53

critodic changes, 250
cripatotic Philosophy (περιπατέω,
to walk about), the name usually
given to the doctrines of Aristotle
and his followers, who are said to
have carried on their studies and
discussions while walking about the
halls and promenades of the Lyceum.

Petitio Principii, 179 Piiono enon, 240 Philosophicai la guage, requisites of, 290

Physical definition assigns the parts into which a thing may be separated by partition or physical division.

lurative propositions, 191

Polylo a, an argument of the same form as a dilemma, but in which there are more than two alternatives, orplayry, tree of, 103

tified.

ort oy o c, III, 157

ostive te s, 22

ost oc, er o pr ter hoc,
181

ostulate (postulatum, a thing de
m ded), a proposition which is necessarily dem ded as a basis of argument; in geometry, the postulates
define the practical conditions re-

quired.
edicables, 98
redica ents (pradicamenta,
what be predicated), see Cate-

redicate, 62, 88, 92; q

e ise, or Pre's, 15, 127
i ary Laws of Thought, 117
nci le (principium, beginning),
the first source of anything; sometimes specially used to mean the
major pre'se of a syllogism.
Tivative concention, inference

rivative conception, inference by, 85 rivative t S. 24

rivative t s, 24
Probability, q tity or degree of belief, or more truly, quantity of information concerning an uncertain event, measured by the ratio of the number of es favourable to the event to the total n ber of es which are possible.

Probability, of propositions, 70; of

inductions, 223 **Proble** $(\pi\rho\delta\beta\lambda\eta\mu\alpha)$, that which is thrown do), an assertion put forward for proof or disproof.

roof, the assigning a reason or argument for the support of a given proposition.

o 'er names, 18

o ert or proprium, 41, 102, 109
ro ositions, 10, 16; several kinds
of, 60; affir tive and negative, 63;
categorical, 63; conditional, 62, 160;
disjunctive, 62, 160; essential or explicative, 68; exclusive, exceptive,
68; hypothetical, 62, 162; indefinite
or indesignate, 65; modal, 69, 91;
opposition of, 78; particular, 63, 72, 70; pure, 69; plurative, 191; irregular, 67; quality and quantity of,
63

Prosyllo s , 155 ro ate enus, 1 u tification of predicate, 183 u tity of propositions, 63; Questions of quantity, 120 uate to ter no , 170

e ee, see Tree of Poration, a equivalent to Syllogism or Deduction, adopted by I. S. Mill.

alis 13
eason (ratio, from reor, to think),
a term of wide and ambiguous meaning; it has sometimes been ecially
used to denote the minor premise of
a syllogism.

easoning, or d , 15 ecord, language as instrument of,

280
eductio ad abs d ad
impossibile, an indirect demo tration founded upon the impossibility
of a contradictory supposition, x46
eduction of the syllogistic figures,
x45; of hypothetical to categorical
syllogisms, 162—5

elation (relation, past participle of refero, to b back), y connection in thought or fact between two things, 21

elative terms, 25 esidu phenomena, 254 esidues, method of, 252 ules of the syllogism, 127

chol tic ilosophy, a general name for the syste of Philosophy taught during the middle ages from the 9th to the 16th century, flourishing chiefly in the 13th and 14th centuries. The subject we chiefly the logic of Aristotle, varied with theology, metaphysics, grange, or the property of the property of

econd tention, see Int. tion.
ecun adjacen s, of the second adjacent, an expression in incorrect Latin, applied to a grammatical sentence or proposition containing only two parts, the subject
and verb, without a distinct copula.
e -con a ctory terms, x93

e ilo c fallacies, 171 entence, grammatical, 61, 89 ep able accident, 103 Si ni cates of a term are things denoted or signified by it.

il s, substitution of, 124, 200 ple, apprehension, 11; conversion, 82, 184

terms, 18; propositions,64 ophis (σόφισμα, from σοφία, wisdom), a false argument; the name often implies that a false argument is consciously used for deception. orites, 156

pecialization of names, 45, 48 Species, in logic, 98; in natural history, 101

ubaltern, propositions, 77; genera and species, 100

Subalternans, subalternates, 77 ubcontr

y Propositions, 77 ubject of a proposition, 62, 92 ubjective, that which belongs to the thinking subject, the ego, or mind engaged in thought; opposed to objective, which see ubordinate propositions, 91

ce (sub, under; stans from stare, to stand), that which underlies and bears phenomena or attributes; strictly speaking it is either mind or matter, but it is more commonly used in the material sense.

Substitution of similars, 124, 200 ubsu p on (sub, under; sumo, to take or put), a name used by Sir W. Hamilton for the minor premise of a syllogism, because it brings or subsumes a special case under the rule expressed in the major premise or sumption.

Subsu ption of a law is Mr Mill's expression for the third mode of explaining a law by shewing it to be a particular case of a more general law, 268

cient eason, Principle or Law of, 125

ui generis, 101 genus, 100 ption (sumo, to take), Sir W. Hamilton's name for the major premise of a syllogism. upposition, 270

yllo s , 10, 127; inductive, 211, V bolic knowledge, 57

yncategore atic words, 18 ynthesis, 205 ynthetic syllogism, a syllogism in which the conclusion stands last; see Analytic syllogism. yste , (σύστημα, from συνίστημι, to put together), a connected body of knowledge.

acit pre ise, 153 autologous propositions, 60 endency, 266 inology, 292 er 8, 10, 16, 17 ertii adjacentis, of the third adjacent, an expression in incorrect Latin, applied to a grammatical sentence or proposition in which the subject, copula and predicate, are

all distinctly stated. heory (θεωρία, contemplation). knowledge of principles, as opposed to practice; ambiguously used, see p. 274

hesis (θέσις, from τίθημι, to place), an assertion or proposition which is put forth to be proved or supported by arguments.

houghts on things, the object of logic, 10 divisu

, a class or notion which is divided into parts by a difference

raduction, 212 ransfer of meaning of terms, 32 ree of Porphyry, 103

rile a, an argument resembling a dilemma, but in which there are three alternatives. ruis s, 69

ruth, conformity of our knowledge with the things known.

Ultra-total distribution, 191 nifor ity of nature, 217 Universal propositions, 63, 66; affirmative, 7x; negative, 73 nivocal terms, 20

Variations, method of, 249; periodic, 250 Verb, 88

eakened conclusion, 140 orse relation (Hamilton), 190